## Computer Graphics PRINCIPLES AND PRACTICE

Foley • van Dam • Finer • Hughes SECOND EDITION


THE SYSTEMS PROGRAMMING SERIES

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To Marylou, Ht

To Debbie, my my children Eli

To Jenni, my pi

To my family, 1 my father in mt

And to all of ol

Cover: "Dutch Interior," after Vermeer, by J. Wallace, M. Cohen, and D. Greenberg, Cornell University (Copyright © 1987 Cornell University, Program of Computer Graphics.)

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| $\boldsymbol{M}_{1}$ | $\boldsymbol{M}_{2}$ |
| :--- | :--- |
| Translate | Translate |
| Scale | Scale |
| Rotate | Rotate |
| Scale (with $s_{z}=s_{y}$ ) | Rotate |

In these cases, we need not be concerned about the order of matrix manipulation.

### 5.4 THE WINDOW-TO-VIEWPORT TRANSFORMATION

Some graphics packages allow the programmer to specify output primitive coordinates in a floating-point world-coordinate system, using whatever units are meaningful to the application program: angstroms, microns, meters, miles, light-years, and so on. The term world is used because the application program is representing a world that is being interactively created or displayed to the user.

Given that output primitives are specified in world coordinates, the graphics subroutine package must be told how to map world coordinates onto screen coordinates (we use the specific term screen coordinates to relate this discussion specifically to SRGP, but that hardcopy output devices might be used, in which case the term device coordinates would be more appropriate). We could do this mapping by having the application programmer provide the graphics package with a transformation matrix to effect the mapping. Another way is to have the application programmer specify a rectangular region in world coordinates, called the world-coordinate window, and a corresponding rectangular region in screen coordinates, called the viewport, into which the world-coordinate window is to be mapped. The transformation that maps the window into the viewport is applied to all of the output primitives in world coordinates, thus mapping them into screen coordinates. Figure 5.10 shows this concept. As seen in this figure, if the window and viewport do not have the same height-to-width ratio, a nonuniform scaling occurs. If the application program changes the window or viewport, then new output primitives drawn onto the screen will be affected by the change. Existing output primitives are not affected by such a change.

The modifier world-coordinate is used with window to emphasize that we are not discussing a window-manager window, which is a different and more recent concept, and


Fig. 5.10 The window in world coordinates and the viewport in screen coordinates determine the mapping that is applied to all the output primitives in world coordinates.


Fig. 5.11 The efi primitives specifyin changed to viewpc package to draw th
which unfortunately of window is meant

If SRGP were tc the current canvas, be able to change $t$ specified output pri included a different in positions differen

A window man: which case not all c Chapter 10, we fi viewports, and wins

Given a windou from world coordi1 developed as a thri


Fig. 5.12 The s

## If matrix manipulation.

## RMATION

ttput primitive coordinates in a units are meaningful to the yht-years, and so on. The term ienting a world that is being
linates, the graphics subroutine screen coordinates (we use the specifically to SRGP, but that rm device coordinates would be g the application programmer to effect the mapping. Another rectangular region in world esponding rectangular region in rld-coordinate window is to be viewport is applied to all of the into screen coordinates. Figure ow and viewport do not have the rs. If the application program es drawn onto the screen will be affected by such a change.
, to emphasize that we are not it and more recent concept, and

viewport in screen coordinates primitives in world coordinates.


Fig. 5.11 The effect of drawing output primitives with two viewports. Output primitives specifying the house were first drawn with viewport 1 , the viewport was changed to viewport 2, and then the application program again called the graphics package to draw the output primitives.
which unfortunately has the same name. Whenever there is no ambiguity as to which type of window is meant, we will drop the modifier.

If SRGP were to provide world-coordinate output primitives, the viewport would be on the current canvas, which defaults to canvas 0 , the screen. The application program would be able to change the window or the viewport at any time, in which case subsequently specified output primitives would be subjected to a new transformation. If the change included a different viewport, then the new output primitves would be located on the canvas in positions different from those of the old ones, as shown in Fig. 5.11.

A window manager might map SRGP's canvas 0 into less than a full-screen window, in which case not all of the canvas or even of the viewport would necessarily be visible. In Chapter 10, we further discuss the relationships among world-coordinate windows, viewports, and window-manager windows.

Given a window and viewport, what is the transformation matrix that maps the window from world coordinates into the viewport in screen coordinates? This matrix can be developed as a three-step transformation composition, as suggested in Fig. 5.12. The


Fig. 5.12 The steps in transforming a world-coordinate window into a viewport.

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Fig. 5.13 Output primitives in world coordinates are clipped against the window. Those that remain are displayed in the viewport.
window, specified by its lower-left and upper-right corners, is first translated to the origin of world coordinates. Next, the size of the window is scaled to be equal to the size of the viewport. Finally, a translation is used to position the viewport. The overall matrix $M_{\mathrm{wv}}$ is:

$$
\begin{align*}
& M_{\mathrm{wv}}=T\left(u_{\min }, v_{\min }\right) \cdot S\left(\frac{u_{\max }-u_{\min }}{x_{\max }-x_{\min }}, \frac{v_{\max }-v_{\min }}{y_{\max }-y_{\min }}\right) \cdot T\left(-x_{\min },-y_{\min }\right) \\
& =\left[\begin{array}{ccc}
1 & 0 & u_{\min } \\
0 & 1 & v_{\min } \\
0 & 0 & 1
\end{array}\right] \cdot\left[\begin{array}{ccc}
\frac{u_{\max }-u_{\min }}{x_{\max }-x_{\min }} \\
0 & 0 & 0 \\
0 & \frac{v_{\max }-v_{\min }}{y_{\max }-y_{\min }} & 0 \\
0 & 1
\end{array}\right] \cdot\left[\begin{array}{ccc}
1 & 0 & -x_{\min } \\
0 & 1 & -y_{\min } \\
0 & 0 & 1
\end{array}\right] \\
& =\left[\begin{array}{ccc}
\frac{u_{\max }-u_{\min }}{x_{\max }-x_{\min }} & 0 & -x \cdot \frac{u_{\max }-u_{\min }}{x_{\max }-x_{\min }}+u_{\min } \\
0 & \frac{v_{\max }-v_{\min }}{y_{\max }-y_{\min }} & -y \cdot \frac{v_{\max }-v_{\min }}{y_{\max }-y_{\min }}+v_{\min } \\
0 & 0 & 1
\end{array}\right] . \tag{5.33}
\end{align*}
$$

Multiplying $P=M_{\mathrm{wv}}\left[\begin{array}{lll}x & y & 1\end{array}\right]^{\mathrm{T}}$ gives the expected result:

$$
\begin{equation*}
P=\left[\left(x-x_{\min }\right) \cdot \frac{u_{\max }-u_{\min }}{x_{\max }-x_{\min }}+u_{\min } \quad\left(y-y_{\min }\right) \cdot \frac{v_{\max }-v_{\min }}{y_{\max }-y_{\min }}+v_{\min } \quad 1\right] \tag{5.34}
\end{equation*}
$$

Many graphics packages combine the window-viewport transformation with clipping of output primitives against the window. The concept of clipping was introduced in Chapter 3; Fig. 5.13 illustrates clipping in the context of windows and viewports.

### 5.5 EFFICIENCY

The most general composition of $R, S$, and $T$ operations produces a matrix of the form

$$
M=\left[\begin{array}{ccc}
r_{11} & r_{12} & t_{x}  \tag{5.35}\\
r_{21} & r_{22} & t_{y} \\
0 & 0 & 1
\end{array}\right] .
$$

## 5.6

The upper $2 \times 2$ are composite translat nine multiplies and $s$ simplifies the actual
reducing the process since the operation Thus, although $3 \times$ tions, we can use th structure. Some harc diminishing or remo

Another area wl such as a molecule o: view can be created object will appear ts each individual poin (Eq. (5.6)) require f recognizing that, be approximation, Eq.
which requires just significant on comp

Equation (5.37) small error is built i error gets a bit large correct values, and $t$ lines.

A better approx

$$
y^{\prime}=x^{\prime}
$$

This is a better : corresponding $2 \times$ unchanged.

### 5.6 MATRIX I

Just as 2D transfo coordinates, so 3D homogeneous coor representing a poi

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