

## The University of Michigan

## Where am I?

Sensors and Methods for Mobile Robot Positioning

by

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## InTRODUCTION

Leonard and Durrant-Whyte [1991] summarized the general problem of mobile robot navigation by three questions: "Where am I?," "Where am I going?," and "How should I get there?." This report surveys the state-of-the-art in sensors, systems, methods, and technologies that aim at answering the first question, that is: robot positioning in its environment.

Perhaps the most important result from surveying the vast body of literature on mobile robot positioning is that to date there is no truly elegant solution for the problem. The many partial solutions can roughly be categorized into two groups: relative and absolute position measurements. Because of the lack of a single, generally good method, developers of automated guided vehicles (AGVs) and mobile robots usually combine two methods, one from each category. The two categories can be further divided into the following subgroups.

## Relative Position Measurements

a. Odometry This method uses encoders to measure wheel rotation and/or steering orientation. Odometry has the advantage that it is totally self-contained, and it is always capable of providing the vehicle with an estimate of its position. The disadvantage of odometry is that the position error grows without bound unless an independent reference is used periodically to reduce the error [Cox, 1991].
b. Inertial Navigation This method uses gyroscopes and sometimes accelerometers to measure rate of rotation and acceleration. Measurements are integrated once (or twice) to yield position. Inertial navigation systems also have the advantage that they are self-contained. On the downside, inertial sensor data drifts with time because of the need to integrate rate data to yield position; any small constant error increases without bound after integration. Inertial sensors are thus unsuitable for accurate positioning over an extended period of time. Another problem with inertial navigation is the high equipment cost. For example, highly accurate gyros, used in airplanes, are inhibitively expensive. Very recently fiber-optic gyros (also called laser gyros), which are said to be very accurate, have fallen dramatically in price and have become a very attractive solution for mobile robot navigation.

## Absolute Position Measurements

c. Active Beacons This method computes the absolute position of the robot from measuring the direction of incidence of three or more actively transmitted beacons. The transmitters, usually using light or radio frequencies, must be located at known sites in the environment.
d. Artificial Landmark Recognition In this method distinctive artificial landmarks are placed at known locations in the environment. The advantage of artificial landmarks is that they can be designed for optimal detectability even under adverse environmental conditions. As with active beacons, three or more landmarks must be "in view" to allow position estimation. Landmark positioning has the advantage that the position errors are bounded, but detection of external
landmarks and real-time position fixing may not always be possible. Unlike the usually pointshaped beacons, artificial landmarks may be defined as a set of features, e.g., a shape or an area. Additional information, for example distance, can be derived from measuring the geometric properties of the landmark, but this approach is computationally intensive and not very accurate.
e. Natural Landmark Recognition Here the landmarks are distinctive features in the environment. There is no need for preparation of the environment, but the environment must be known in advance. The reliability of this method is not as high as with artificial landmarks.
f. Model Matching In this method information acquired from the robot's onboard sensors is compared to a map or world model of the environment. If features from the sensor-based map and the world model map match, then the vehicle's absolute location can be estimated. Mapbased positioning often includes improving global maps based on the new sensory observations in a dynamic environment and integrating local maps into the global map to cover previously unexplored areas. The maps used in navigation include two major types: geometric maps and topological maps. Geometric maps represent the world in a global coordinate system, while topological maps represent the world as a network of nodes and arcs.

This book presents and discusses the state-of-the-art in each of the above six categories. The material is organized in two parts: Part I deals with the sensors used in mobile robot positioning, and Part II discusses the methods and techniques that make use of these sensors.

Mobile robot navigation is a very diverse area, and a useful comparison of different approaches is difficult because of the lack of commonly accepted test standards and procedures. The research platforms used differ greatly and so do the key assumptions used in different approaches. Further difficulty arises from the fact that different systems are at different stages in their development. For example, one system may be commercially available, while another system, perhaps with better performance, has been tested only under a limited set of laboratory conditions. For these reasons we generally refrain from comparing or even judging the performance of different systems or techniques. Furthermore, we have not tested most of the systems and techniques, so the results and specifications given in this book are merely quoted from the respective research papers or product spec-sheets.

Because of the above challenges we have defined the purpose of this book to be a survey of the expanding field of mobile robot positioning. It took well over 1.5 man-years to gather and compile the material for this book; we hope this work will help the reader to gain greater understanding in much less time.

## Part I

## Sensors for Mobile Robot Positioning



CARMEL, the University of Michigan's first mobile robot, has been in service since 1987. Since then, CARMEL has served as a reliable testbed for countless sensor systems. In the extra "shelf" underneath the robot is an 8086 XT compatible single-board computer that runs U of M's ultrasonic sensor firing algorithm. Since this code was written in 1987, the computer has been booting up and running from floppy disk. The program was written in FORTH and was never altered; should anything ever go wrong with the floppy, it will take a computer historian to recover the code...

## Chapter 1

## Sensors for Dead Reckoning

Dead reckoning (derived from "deduced reckoning" of sailing days) is a simple mathematical procedure for determining the present location of a vessel by advancing some previous position through known course and velocity information over a given length of time [Dunlap and Shufeldt, 1972]. The vast majority of land-based mobile robotic systems in use today rely on dead reckoning to form the very backbone of their navigation strategy, and like their nautical counterparts, periodically null out accumulated errors with recurring "fixes" from assorted navigation aids.

The most simplistic implementation of dead reckoning is sometimes termed odometry; the term implies vehicle displacement along the path of travel is directly derived from some onboard "odometer." A common means of odometry instrumentation involves optical encoders directly coupled to the motor armatures or wheel axles.

Since most mobile robots rely on some variation of wheeled locomotion, a basic understanding of sensors that accurately quantify angular position and velocity is an important prerequisite to further discussions of odometry. There are a number of different types of rotational displacement and velocity sensors in use today:

- Brush encoders.
- Potentiometers.
- Synchros.
- Resolvers.
- Optical encoders.
- Magnetic encoders.
- Inductive encoders.
- Capacitive encoders.

A multitude of issues must be considered in choosing the appropriate device for a particular application. Avolio [1993] points out that over 17 million variations on rotary encoders are offered by one company alone. For mobile robot applications incremental and absolute optical encoders are the most popular type. We will discuss those in the following sections.

### 1.1 Optical Encoders

The first optical encoders were developed in the mid-1940s by the Baldwin Piano Company for use as "tone wheels" that allowed electric organs to mimic other musical instruments [Agent, 1991]. Today's corresponding devices basically embody a miniaturized version of the break-beam proximity sensor. A focused beam of light aimed at a matched photodetector is periodically interrupted by a coded opaque/transparent pattern on a rotating intermediate disk attached to the shaft of interest. The rotating disk may take the form of chrome on glass, etched metal, or photoplast such as Mylar [Henkel, 1987]. Relative to the more complex alternating-current resolvers, the straightforward encoding scheme and inherently digital output of the optical encoder results in a lowcost reliable package with good noise immunity.

There are two basic types of optical encoders: incremental and absolute. The incremental version measures rotational velocity and can infer relative position, while absolute models directly measure angular position and infer velocity. If non volatile position information is not a consideration, incremental encoders generally are easier to interface and provide equivalent resolution at a much lower cost than absolute optical encoders.

### 1.1.1 Incremental Optical Encoders

The simplest type of incremental encoder is a single-channel tachometer encoder, basically an instrumented mechanical light chopper that produces a certain number of sine- or square-wave pulses for each shaft revolution. Adding pulses increases the resolution (and subsequently the cost) of the unit. These relatively inexpensive devices are well suited as velocity feedback sensors in medium- to high-speed control systems, but run into noise and stability problems at extremely slow velocities due to quantization errors [Nickson, 1985]. The tradeoff here is resolution versus update rate: improved transient response requires a faster update rate, which for a given line count reduces the number of possible encoder pulses per sampling interval. A very simple, do-it-yourself encoder is described in [Jones and Flynn, 1993]. More sophisticated single-channel encoders are typically limited to 2540 lines for a 5 -centimeter ( 2 in ) diameter incremental encoder disk [Henkel, 1987].

In addition to low-speed instabilities, single-channel tachometer encoders are also incapable of detecting the direction of rotation and thus cannot be used as position sensors. Phase-quadrature incremental encoders overcome these problems by adding a second channel, displaced from the first, so the resulting pulse trains are 90 degrees out of phase as shown in Figure 1.1. This technique allows the decoding electronics to determine which channel is leading the other and hence ascertain the direction of rotation, with the added benefit of increased resolution. Holle [1990] provides an in-depth discussion of output options (single-ended TTL or differential drivers) and various design issues (i.e., resolution, bandwidth, phasing, filtering) for consideration when interfacing phasequadrature incremental encoders to digital control systems.

The incremental nature of the phase-quadrature output signals dictates that any resolution of angular position can only be relative to some specific reference, as opposed to absolute. Establishing such a reference can be accomplished in a number of ways. For applications involving continuous 360 -degree rotation, most encoders incorporate as a third channel a special index output that goes high once for each complete revolution of the shaft (see Figure 1.1 above). Intermediate shaft


| State | Ch A | Ch B |
| :---: | :---: | :---: |
| $\mathrm{S}_{1}$ | High | Low |
| $\mathrm{S}_{2}$ | High | High |
| $\mathrm{S}_{3}$ | Low | High |
| $\mathrm{S}_{4}$ | Low | Low |

Figure 1.1: The observed phase relationship between Channel $A$ and $B$ pulse trains can be used to determine the direction of rotation with a phase-quadrature encoder, while unique output states $S_{1}-S_{4}$ allow for up to a four-fold increase in resolution. The single slot in the outer track generates one index pulse per disk rotation [Everett, 1995].
positions are then specified by the number of encoder up counts or down counts from this known index position. One disadvantage of this approach is that all relative position information is lost in the event of a power interruption.

In the case of limited rotation, such as the back-and-forth motion of a pan or tilt axis, electrical limit switches and/or mechanical stops can be used to establish a home reference position. To improve repeatability this homing action is sometimes broken into two steps. The axis is rotated at reduced speed in the appropriate direction until the stop mechanism is encountered, whereupon rotation is reversed for a short predefined interval. The shaft is then rotated slowly back into the stop at a specified low velocity from this designated start point, thus eliminating any variations in inertial loading that could influence the final homing position. This two-step approach can usually be observed in the power-on initialization of stepper-motor positioners for dot-matrix printer heads.

Alternatively, the absolute indexing function can be based on some external referencing action that is decoupled from the immediate servo-control loop. A good illustration of this situation involves an incremental encoder used to keep track of platform steering angle. For example, when the $K 2 A$ Navmaster [CYBERMOTION] robot is first powered up, the absolute steering angle is unknown, and must be initialized through a "referencing" action with the docking beacon, a nearby wall, or some other identifiable set of landmarks of known orientation. The up/down count output from the decoder electronics is then used to modify the vehicle heading register in a relative fashion.

A growing number of very inexpensive off-the-shelf components have contributed to making the phase-quadrature incremental encoder the rotational sensor of choice within the robotics research and development community. Several manufacturers now offer small DC gear-motors with incremental encoders already attached to the armature shafts. Within the U.S. automated guided vehicle (AGV) industry, however, resolvers are still generally preferred over optical encoders for their perceived superiority under harsh operating conditions, but the European AGV community seems to clearly favor the encoder [Manolis, 1993].

Interfacing an incremental encoder to a computer is not a trivial task. A simple state-based interface as implied in Figure 1.1 is inaccurate if the encoder changes direction at certain positions, and false pulses can result from the interpretation of the sequence of state changes [Pessen, 1989]. Pessen describes an accurate circuit that correctly interprets directional state changes. This circuit was originally developed and tested by Borenstein [1987].

A more versatile encoder interface is the HCTL 1100 motion controller chip made by Hewlett Packard [HP]. The HCTL chip performs not only accurate quadrature decoding of the incremental wheel encoder output, but it provides many important additional functions, including among others:

- closed-loop position control,
- closed-loop velocity control in P or PI fashion,
- 24-bit position monitoring.

At the University of Michigan's Mobile Robotics Lab, the HCTL 1100 has been tested and used in many different mobile robot control interfaces. The chip has proven to work reliably and accurately, and it is used on commercially available mobile robots, such as the TRC LabMate and HelpMate. The HCTL 1100 costs only $\$ 40$ and it comes highly recommended.

### 1.1.2 Absolute Optical Encoders

Absolute encoders are typically used for slower rotational applications that require positional information when potential loss of reference from power interruption cannot be tolerated. Discrete detector elements in a photovoltaic array are individually aligned in break-beam fashion with concentric encoder tracks as shown in Figure 1.2, creating in effect a non-contact implementation of a commutating brush encoder. The assignment of a dedicated track for each bit of resolution results in larger size disks (relative to incremental designs), with a corresponding decrease in shock and vibration tolerance. A general rule of thumb is that each additional encoder track doubles the resolution but quadruples the cost [Agent, 1991].


Figure 1.2: A line source of light passing through a coded pattern of opaque and transparent segments on the rotating encoder disk results in a parallel output that uniquely specifies the absolute angular position of the shaft. (Adapted from [Agent, 1991].)

Instead of the serial bit streams of incremental designs, absolute optical encoders provide a parallel word output with a unique code pattern for each quantized shaft position. The most common coding schemes are Gray code, natural binary, and binary-coded decimal [Avolio, 1993]. The Gray code (for inventor Frank Gray of Bell Labs) is characterized by the fact that only one bit changes at a time, a decided advantage in eliminating asynchronous ambiguities caused by electronic and mechanical component tolerances (see Figure 1.3a). Binary code, on the other hand, routinely involves multiple bit changes when incrementing or decrementing the count by one. For example, when going from position 255 to position 0 in Figure 1.3b, eight bits toggle from 1s to 0s. Since there is no guarantee all threshold detectors monitoring the detector elements tracking each bit will toggle at the same precise instant, considerable ambiguity can exist during state transition with a coding scheme of this form. Some type of handshake line signaling valid data available would be required if more than one bit were allowed to change between consecutive encoder positions.

Absolute encoders are best suited for slow and/or infrequent rotations such as steering angle encoding, as opposed to measuring high-speed continuous (i.e., drive wheel) rotations as would be required for calculating displacement along the path of travel. Although not quite as robust as resolvers for high-temperature, high-shock applications, absolute encoders can operate at temperatures over $125^{\circ} \mathrm{C}$, and medium-resolution (1000 counts per revolution) metal or Mylar disk designs can compete favorably with resolvers in terms of shock resistance [Manolis, 1993].
A potential disadvantage of absolute encoders is their parallel data output, which requires a more complex interface due to the large number of electrical leads. A 13-bit absolute encoder using
complimentary output signals for noise immunity would require a 28 -conductor cable (13 signal pairs plus power and ground), versus only six for a resolver or incremental encoder [Avolio, 1993].


Figure 1.3: Rotating an 8-bit absolute Gray code disk.
a. Counterclockwise rotation by one position increment will cause only one bit to change.
b. The same rotation of a binary-coded disk will cause all bits to change in the particular case ( 255 to 0 ) illustrated by the reference line at 12 o'clock.
[Everett, 1995].

### 1.2 Doppler Sensors

The rotational displacement sensors discussed above derive navigation parameters directly from wheel rotation, and are thus subject to problems arising from slippage, tread wear, and/or improper tire inflation. In certain applications, Doppler and inertial navigation techniques are sometimes employed to reduce the effects of such error sources.

Doppler navigation systems are routinely employed in maritime and aeronautical applications to yield velocity measurements with respect to the earth itself, thus eliminating dead-reckoning errors introduced by unknown ocean or air currents. The principle of operation is based on the Doppler shift in frequency observed when radiated energy reflects off a surface that is moving with respect to the emitter. Maritime systems employ acoustical energy reflected from the ocean floor, while airborne systems sense microwave RF energy bounced off the surface of the earth. Both configurations typically involve an array of four transducers spaced 90 degrees apart in azimuth and inclined downward at a common angle with respect to the horizontal plane [Dunlap and Shufeldt, 1972].

Due to cost constraints and the reduced likelihood of transverse drift, most robotic implementations employ but a single forward-looking transducer to measure ground speed in the direction of travel. Similar configurations are sometimes used in the agricultural industry, where tire slippage in soft freshly plowed dirt can seriously interfere with the need to release seed or fertilizer at a rate commensurate with vehicle advance. The M113-based Ground Surveillance Vehicle [Harmon, 1986] employed an off-the-shelf unit of this type manufactured by John Deere to compensate for track slippage.

The microwave radar sensor is aimed downward at a prescribed angle (typically $45^{\circ}$ ) to sense ground movement as shown in Figure 1.4. Actual ground speed $V_{A}$ is derived from the measured velocity $V_{D}$ according to the following equation [Schultz, 1993]:

$$
\begin{equation*}
V_{A}=\frac{V_{D}}{\cos \alpha}=\frac{c F_{D}}{2 F_{0} \cos \alpha} \tag{1.1}
\end{equation*}
$$

where
$V_{A}=$ actual ground velocity along path
$V_{D}=$ measured Doppler velocity
$\alpha=$ angle of declination
$c=$ speed of light
$F_{D}=$ observed Doppler shift frequency
$F_{0}=$ transmitted frequency.


Figure 1.4: A Doppler ground-speed sensor inclined at an angle $\alpha$ as shown measures the velocity component $V_{D}$ of true ground speed $V_{A}$. (Adapted from [Schultz, 1993].)

Errors in detecting true ground speed arise due to side-lobe interference, vertical velocity components introduced by vehicle reaction to road surface anomalies, and uncertainties in the actual angle of incidence due to the finite width of the beam. Byrne et al. [1992] point out another interesting scenario for potentially erroneous operation, involving a stationary vehicle parked over a stream of water. The Doppler ground-speed sensor in this case would misinterpret the relative motion between the stopped vehicle and the running water as vehicle travel.

### 1.2.1 Micro-Trak Trak-Star Ultrasonic Speed Sensor

One commercially available speed sensor that is based on Doppler speed measurements is the TrakStar Ultrasonic Speed Sensor [MICRO-TRAK]. This device, originally designed for agricultural applications, costs $\$ 420$. The manufacturer claims that this is the most accurate Doppler speed sensor available. The technical specifications are listed in Table 1.1.


Figure 1.5: The Trak-Star Ultrasonic Speed Sensor is based on the Doppler effect. This device is primarily targeted at the agricultural market. (Courtesy of Micro-Trak.)

### 1.2.2 Other Doppler-Effect Systems

A non-radar Doppler-effect device is the Monitor 1000, a distance and speed monitor for runners. This device was temporarily marketed by the sporting goods manufacturer [NIKE]. The Monitor 1000 was worn by the runner like a front-mounted fanny pack. The small and lightweight device used ultrasound as the carrier, and was said to have an accuracy of two to five percent, depending on the ground characteristics. The manufacturer of the Monitor 1000 is Applied Design Laboratories [ADL]. A microwave radar Doppler effect distance sensor has also been developed by ADL. This radar sensor is a prototype and is not commercially available. However, it differs from the Monitor 1000 only in its use of a radar sensor head as opposed to the ultrasonic sensor head used by the Monitor 1000. The prototype radar sensor measures $15 \times 10 \times 5$ centimeters ( $6 \times 4 \times 2$ in), weighs 250 grams ( 8.8 oz ), and consumes 0.9 W .

### 1.3 Typical Mobility Configurations

The accuracy of odometry measurements for dead reckoning is to a great extent a direct function of the kinematic design of a vehicle. Because of this close relation between kinematic design and positioning accuracy, one must consider the kinematic design closely before attempting to improve dead-reckoning accuracy. For this reason, we will briefly discuss some of the more popular vehicle designs in the following sections. In Part II of this report, we will discuss some recently developed methods for reducing odometry errors (or the feasibility of doing so) for some of these vehicle designs.

### 1.3.1 Differential Drive

Figure 1.6 shows a typical differential drive mobile robot, the LabMate platform, manufactured by [TRC]. In this design incremental encoders are mounted onto the two drive motors to count the wheel revolutions. The robot can perform dead reckoning by using simple geometric equations to compute the momentary position of the vehicle relative to a known starting position.

Table 1.1: Specifications for the Trak-Star Ultrasonic Speed Sensor.

| Parameter | Value Units |
| :--- | ---: |
| Speed range | $17.7 \mathrm{~m} / \mathrm{s}$ |
|  | $0-40 \mathrm{mph}$ |
| Speed resolution | $1.8 \mathrm{~cm} / \mathrm{s}$ |
|  | $0.7 \mathrm{in} / \mathrm{s}$ |
| Accuracy | $\pm 1.5 \%+0.04 \mathrm{mph}$ |
| Transmit frequency | 62.5 kHz |
| Temperature range | -29 to $+500^{\circ} \mathrm{C}$ |
|  | -20 to $+120^{\circ} \mathrm{F}$ |
| Weight | 1.3 kg |
|  | 3 lb |
| Power requirements | 12 VDC |
|  | 0.03 A |

a


Figure 1.6: A typical differential-drive mobile robot (bottom view).

For completeness, we rewrite the well-known equations for odometry below (also, see [Klarer, 1988; Crowley and Reignier, 1992]). Suppose that at sampling interval $I$ the left and right wheel encoders show a pulse increment of $N_{L}$ and $N_{R}$, respectively. Suppose further that
$c_{m}=\pi D_{n} / n C_{e}$
where
$c_{\mathrm{m}}=$ conversion factor that translates encoder pulses into linear wheel displacement
$D_{n}=$ nominal wheel diameter (in mm )
$C_{e} \quad=$ encoder resolution (in pulses per revolution)
$n \quad=$ gear ratio of the reduction gear between the motor (where the encoder is attached) and the drive wheel.

We can compute the incremental travel distance for the left and right wheel, $\Delta U_{L, i}$ and $\Delta U_{R, i}$, according to
$\Delta U_{L R, i}=c_{m} N_{L R, i}$
and the incremental linear displacement of the robot's centerpoint $C$, denoted $\Delta U_{i}$, according to
$\Delta U_{i}=\left(\Delta U_{R}+\Delta U_{L}\right) / 2$.
Next, we compute the robot's incremental change of orientation
$\Delta \theta_{i}=\left(\Delta U_{R}-\Delta U_{L}\right) / b$
where $b$ is the wheelbase of the vehicle, ideally measured as the distance between the two contact points between the wheels and the floor.

The robot's new relative orientation $\theta_{i}$ can be computed from
$\theta_{i}=\theta_{i-l}+\Delta \theta_{i}$
and the relative position of the centerpoint is
$x_{i}=x_{i-1}+\Delta U_{i} \cos \theta_{i}$
$y_{i}=y_{i-1}+\Delta U_{i} \sin \theta_{i}$
where
$x_{i}, y_{i}=$ relative position of the robot's centerpoint $c$ at instant $i$.

### 1.3.2 Tricycle Drive

Tricycle-drive configurations (see Figure 1.7) employing a single driven front wheel and two passive rear wheels (or vice versa) are fairly common in AGV applications because of their inherent simplicity. For odometry instrumentation in the form of a steering-angle encoder, the dead-reckoning solution is equivalent to that of an Ackerman-steered vehicle, where the steerable wheel replaces the imaginary center wheel discussed in Section 1.3.3. Alternatively, if rear-axle differential odometry is used to determine heading, the solution is identical to the differential-drive configuration discussed in Section 1.3.1.

One problem associated with the tricycle-drive configuration is that the vehicle's center of gravity tends to move away from the front wheel when traversing up an incline, causing a loss of traction. As in the case of Ackerman-steered designs, some surface damage and induced heading errors are possible when actuating the steering while the platform is not moving.


Figure 1.7: Tricycle-drive configurations employing a steerable driven wheel and two passive trailing wheels can derive heading information directly from a steering angle encoder or indirectly from differential odometry [Everett, 1995].

### 1.3.3 Ackerman Steering

Used almost exclusively in the automotive industry, Ackerman steering is designed to ensure that the inside front wheel is rotated to a slightly sharper angle than the outside wheel when turning, thereby eliminating geometrically induced tire slippage. As seen in Figure 1.8, the extended axes for the two front wheels intersect in a common point that lies on the extended axis of the rear axle. The locus of points traced along the ground by the center of each tire is thus a set of concentric arcs about this centerpoint of rotation $P_{1}$, and (ignoring for the moment any centrifugal accelerations) all instantaneous velocity vectors will subsequently be tangential to these arcs. Such a steering geometry is said to satisfy the Ackerman equation [Byrne et al., 1992]:

$$
\begin{equation*}
\cot \theta_{i}-\cot \theta_{o}=\frac{d}{l} \tag{1.8}
\end{equation*}
$$

where
$\theta_{\mathrm{i}}=$ relative steering angle of the inner wheel
$\theta_{\mathrm{o}}=$ relative steering angle of the outer wheel
1 = longitudinal wheel separation
$\mathrm{d}=$ lateral wheel separation.
For the sake of convenience, the vehicle steering angle $\theta_{\mathrm{SA}}$ can be thought of as the angle (relative to vehicle heading) associated with an imaginary center wheel located at a reference point $P_{2}$ as shown in the figure above. $\theta_{\mathrm{SA}}$ can be expressed in terms of either the inside or outside steering angles $\left(\theta_{\mathrm{i}}\right.$ or $\left.\theta_{\mathrm{o}}\right)$ as follows [Byrne et al., 1992]:

$$
\begin{equation*}
\cot \theta_{\mathrm{SA}}=\frac{\mathrm{d}}{2 l}+\cot \theta_{\mathrm{i}} \tag{1.9}
\end{equation*}
$$

or, alternatively,

$$
\begin{equation*}
\cot \theta_{\mathrm{SA}}=\cot \theta_{\mathrm{o}}-\frac{\mathrm{d}}{21} . \tag{1.10}
\end{equation*}
$$

Ackerman steering provides a fairly accurate odometry solution while supporting the traction and ground clearance needs of all-terrain operation. Ackerman steering is thus the method of choice for outdoor autonomous vehicles. Associated drive implementations typically employ a gasoline or diesel engine coupled to a manual or automatic transmission, with power applied to four wheels through


Figure 1.8: In an Ackerman-steered vehicle, the extended axes for all wheels intersect in a common point. (Adapted from [Byrne et al., 1992].)
a transfer case, a differential, and a series of universal joints. A representative example is seen in the HMMWV-based prototype of the USMC Tele-Operated Vehicle (TOV) Program [Aviles et al., 1990]. From a military perspective, the use of existing-inventory equipment of this type simplifies some of the logistics problems associated with vehicle maintenance. In addition, reliability of the drive components is high due to the inherited stability of a proven power train. (Significant interface problems can be encountered, however, in retrofitting off-the-shelf vehicles intended for human drivers to accommodate remote or computer control.)

### 1.3.4 Synchro Drive

An innovative configuration known as synchro drive features three or more wheels (Figure 1.9) mechanically coupled in such a way that all rotate in the same direction at the same speed, and similarly pivot in unison about their respective steering axes when executing a turn. This drive and steering "synchronization" results in improved odometry accuracy through reduced slippage, since all wheels generate equal and parallel force vectors at all times.

The required mechanical synchronization can be accomplished in a number of ways, the most common being a chain, belt, or gear drive. Carnegie Mellon University has implemented an electronically synchronized version on one of their Rover series robots, with dedicated drive motors for each of the three wheels. Chain- and belt-drive configurations experience some degradation in steering accuracy and alignment due to uneven distribution of slack, which varies as a function of loading and direction of rotation. In addition, whenever chains (or timing belts) are tightened to reduce such slack, the individual wheels must be realigned. These problems are eliminated with a completely enclosed gear-drive approach. An enclosed gear train also significantly reduces noise as well as particulate generation, the latter being very important in clean-room applications.

An example of a three-wheeled belt-drive implementation is seen in the Denning Sentry formerly manufactured by Denning Mobile Robots, Woburn, MA [Kadonoff, 1986] and now by Denning Branch Robotics International [DBIR]. Referring to Figure 1.9, drive torque is transferred down through the three steering columns to polyurethane-filled rubber tires. The drive-motor output shaft is mechanically coupled to each of the steering-column power shafts by a heavy-duty timing belt to ensure synchronous operation. A second timing belt transfers the rotational output of the steering motor to the three steering columns, allowing them to synchronously pivot throughout a full 360-


Figure 1.9: A four-wheel synchro-drive configuration:
a. Bottom view. b. Top view.
(Adapted from Holland [1983].)
degree range [Everett, 1985]. The Sentry's upper head assembly is mechanically coupled to the steering mechanism in a manner similar to that illustrated in Figure 1.9, and thus always points in the direction of forward travel. The three-point configuration ensures good stability and traction, while the actively driven large-diameter wheels provide more than adequate obstacle climbing capability for indoor scenarios. The disadvantages of this particular implementation include odometry errors introduced by compliance in the drive belts as well as by reactionary frictional forces exerted by the floor surface when turning in place.

To overcome these problems, the Cybermotion K2A Navmaster robot employs an enclosed geardrive configuration with the wheels offset from the steering axis as shown in Figure 1.10 and Figure 1.11. When a foot pivots during a turn, the attached wheel rotates in the appropriate direction to minimize floor and tire wear, power consumption, and slippage. Note that for correct compensation, the miter gear on the wheel axis must be on the opposite side of the power shaft gear from the wheel as illustrated. The governing equation for minimal slippage is [Holland, 1983]

$$
\begin{equation*}
\frac{A}{B}=\frac{r^{\prime}}{r} \tag{1.11}
\end{equation*}
$$

where
$\mathrm{A}=$ number of teeth on the power shaft gear
$B=$ number of teeth on the wheel axle gear
$r^{\prime}=$ wheel offset from steering pivot axis
$\mathrm{r}=$ wheel radius.

One drawback of this approach is seen in the decreased lateral stability that results when one wheel is turned in under the vehicle. Cybermotion's improved K3A design solves this problem (with an even smaller wheelbase) by incorporating a dual-wheel arrangement on each foot [Fisher et al., 1994]. The two wheels turn in opposite directions in differential fashion as the foot pivots during a turn, but good stability is maintained in the foregoing example by the outward swing of the additional wheel.

The odometry calculations for the synchro drive are almost trivial; vehicle heading is simply derived from the steering-angle encoder, while displacement in the direction of travel is given as follows:


Figure 1.10: Slip compensation during a turn is accomplished through use of an offset foot assembly on the three-wheeled K2A Navmaster robot. (Adapted from [Holland, 1983].)


Figure 1.11: The Denning Sentry (foreground) incorporates a three-point synchro-drive configuration with each wheel located directly below the pivot axis of the associated steering column. In contrast, the Cybermotion K2A (background) has wheels that swivel around the steering column. Both robots were extensively tested at the University of Michigan's Mobile Robotics Lab. (Courtesy of The University of Michigan.)
$D=\frac{2 \pi N}{C_{e}} R_{e}$
where
$D=$ vehicle displacement along path
$N=$ measured counts of drive motor shaft encoder
$C_{e}=$ encoder counts per complete wheel revolution
$R_{e}=$ effective wheel radius.

### 1.3.5 Omnidirectional Drive

The odometry solution for most multi-degree-of-freedom (MDOF) configurations is done in similar fashion to that for differential drive, with position and velocity data derived from the motor (or wheel) shaft encoders. For the three-wheel example illustrated in Figure 1.12, the equations of motion relating individual motor speeds to velocity components $V_{x}$ and $V_{y}$ in the reference frame of the vehicle are given by [Holland, 1983]:


Figure 1.12: a. Schematic of the wheel assembly used by the Veterans Administration [La et al., 1981] on an omnidirectional wheelchair.
b. Top view of base showing relative orientation of components in the three-wheel configuration. (Adapted from [Holland, 1983].)
$\mathrm{V}_{1}=\omega_{1} \mathrm{r}=\mathrm{V}_{\mathrm{x}}+\omega_{\mathrm{p}} \mathrm{R}$
$\mathrm{V}_{2}=\omega_{2} \mathrm{r}=-0.5 \mathrm{~V}_{\mathrm{x}}+0.867 \mathrm{~V}_{\mathrm{y}}+\omega_{\mathrm{p}} \mathrm{R}$
$\mathrm{V}_{3}=\omega_{3} \mathrm{r}=-0.5 \mathrm{~V}_{\mathrm{x}}-0.867 \mathrm{~V}_{\mathrm{y}}+\omega_{\mathrm{p}} \mathrm{R}$
where
$\mathrm{V}_{\mathrm{i}}=$ tangential velocity of wheel number i
$\omega_{\mathrm{i}}=$ rotational speed of motor number i
$\omega_{\mathrm{p}}=$ rate of base rotation about pivot axis
$\omega_{\mathrm{r}}=$ effective wheel radius
$\omega_{R}=$ effective wheel offset from pivot axis.

### 1.3.6 Multi-Degree-of-Freedom Vehicles

Multi-degree-of-freedom (MDOF) vehicles have multiple drive and steer motors. Different designs are possible. For example, HERMIES-III, a sophisticated platform designed and built at the Oak Ridge National Laboratory [Pin et al., 1989; Reister et al., 1991; Reister, 1991] has two powered wheels that are also individually steered (see Figure 1.13). With four independent motors, HERMIES-III is a 4-degree-of-freedom vehicle.

MDOF configurations display exceptional maneuverability in tight quarters in comparison to conventional 2-DOF mobility systems, but have been found to be difficult to control due to their overconstrained nature [Reister et al., 1991; Killough and Pin, 1992; Pin and Killough, 1994; Borenstein, 1995]. Resulting problems include increased wheel slippage and thus reduced odometry accuracy. Recently, Reister and Unseren [1992; 1993] introduced a new control algorithm based on Force Control. The researchers reported on a substantial reduction in wheel


Figure 1.13: A 4-degree-of-freedom vehicle platform can travel in all directions, including sideways and diagonally. The difficulty lies in coordinating all four motors so as to avoid slippage.
slippage for their two-wheel drive/two-wheel steer platform, resulting in a reported 20 -fold improvement of accuracy. However, the experiments on which these results were based avoided simultaneous steering and driving of the two steerable drive wheels. In this way, the critical problem of coordinating the control of all four motors simultaneously and during transients was completely avoided.

Unique Mobility, Inc. built an 8-DOF vehicle for the U.S. Navy under an SBIR grant (see Figure 1.14). In personal correspondence, engineers from that company mentioned to us difficulties in controlling and coordinating all eight motors.


Figure 1.14: An 8-DOF platform with four wheels individually driven and steered. This platform was designed and built by Unique Mobility, Inc. (Courtesy of [UNIQUE].)

### 1.3.7 MDOF Vehicle with Compliant Linkage

To overcome the problems of control and the resulting excessive wheel slippage described above, researchers at the University of Michigan designed the unique Multi-Degree-of-Freedom (MDOF) vehicle shown in Figures 1.15 and 1.16 [Borenstein, 1992; 1993; 1994c; 1995]. This vehicle comprises two differential-drive LabMate robots from [TRC]. The two LabMates, here referred to as "trucks," are connected by a compliant linkage and two rotary joints, for a total of three internal degrees of freedom.

The purpose of the compliant linkage is to accommodate momentary controller errors without transferring any mutual force reactions between the trucks, thereby eliminating the excessive wheel slippage reported for other MDOF vehicles. Because it eliminates excessive wheel slippage, the MDOF vehicle with compliant linkage is one to two orders of magnitude more accurate than other MDOF vehicles, and as accurate as conventional, 2-DOF vehicles.


Figure 1.15: The compliant linkage is instrumented with two absolute rotary encoders and a linear encoder to measure the relative orientations and separation distance between the two trucks.

### 1.3.8 Tracked Vehicles

Yet another drive configuration for mobile robots uses tracks instead of wheels. This very special implementation of a differential drive is known as skid steering and is routinely implemented in track form on bulldozers and armored vehicles. Such skid-steer configurations intentionally rely on track or wheel slippage for normal operation (Figure 1.17), and as a consequence provide rather poor dead-reckoning information. For this reason, skid steering is generally employed only in tele-operated as opposed to autonomous robotic applications, where the ability to surmount significant floor discontinuities is more desirable than accurate odometry information. An example is seen in the track drives popular with remote-controlled robots intended for explosive ordnance disposal. Figure 1.18 shows the Remotec Andros $V$ platform being converted to fully autonomous operation (see Sec. 5.3.1.2).


Figure 1.18: A Remotec Andros $V$ tracked vehicle is outfitted with computer control at the University of Michigan. Tracked mobile platforms are commonly used in teleoperated applications. However, because of the lack of odometry feedback they are rarely (if at all) used in fully autonomous applications. (Courtesy of The University of Michigan.)

## Chapter 2 Heading Sensors

Heading sensors are of particular importance to mobile robot positioning because they can help compensate for the foremost weakness of odometry: in an odometry-based positioning method, any small momentary orientation error will cause a constantly growing lateral position error. For this reason it would be of great benefit if orientation errors could be detected and corrected immediately. In this chapter we discuss gyroscopes and compasses, the two most widely employed sensors for determining the heading of a mobile robot (besides, of course, odometry). Gyroscopes can be classified into two broad categories: (a) mechanical gyroscopes and (b) optical gyroscopes.

### 2.1 Mechanical Gyroscopes

The mechanical gyroscope, a well-known and reliable rotation sensor based on the inertial properties of a rapidly spinning rotor, has been around since the early 1800s. The first known gyroscope was built in 1810 by G.C. Bohnenberger of Germany. In 1852, the French physicist Leon Foucault showed that a gyroscope could detect the rotation of the earth [Carter, 1966]. In the following sections we discuss the principle of operation of various gyroscopes.

Anyone who has ever ridden a bicycle has experienced (perhaps unknowingly) an interesting characteristic of the mechanical gyroscope known as gyroscopic precession. If the rider leans the bike over to the left around its own horizontal axis, the front wheel responds by turning left around the vertical axis. The effect is much more noticeable if the wheel is removed from the bike, and held by both ends of its axle while rapidly spinning. If the person holding the wheel attempts to yaw it left or right about the vertical axis, a surprisingly violent reaction will be felt as the axle instead twists about the horizontal roll axis. This is due to the angular momentum associated with a spinning flywheel, which displaces the applied force by 90 degrees in the direction of spin. The rate of precession $\Omega$ is proportional to the applied torque $T$ [Fraden, 1993]:

[^0]$T=I \omega$
where
$T=$ applied input torque
$I=$ rotational inertia of rotor
$\omega=$ rotor spin rate
$\Omega=$ rate of precession.

Gyroscopic precession is a key factor involved in the concept of operation for the north-seeking gyrocompass, as will be discussed later.

Friction in the support bearings, external influences, and small imbalances inherent in the construction of the rotor cause even the best mechanical gyros to drift with time. Typical systems employed in inertial navigation packages by the commercial airline industry may drift about $0.1^{\circ}$ during a 6-hour flight [Martin, 1986].

### 2.1.1 Space-Stable Gyroscopes

The earth's rotational velocity at any given point on the globe can be broken into two components: one that acts around an imaginary vertical axis normal to the surface, and another that acts around an imaginary horizontal axis tangent to the surface. These two components are known as the vertical earth rate and the horizontal earth rate, respectively. At the North Pole, for example, the component acting around the local vertical axis (vertical earth rate) would be precisely equal to the rotation rate of the earth, or $15^{\circ} / \mathrm{hr}$. The horizontal earth rate at the pole would be zero.

As the point of interest moves down a meridian toward the equator, the vertical earth rate at that particular location decreases proportionally to a value of zero at the equator. Meanwhile, the horizontal earth rate, (i.e., that component acting around a horizontal axis tangent to the earth's surface) increases from zero at the pole to a maximum value of $15^{\circ} / \mathrm{hr}$ at the equator.

There are two basic classes of rotational sensing gyros: 1) rate gyros, which provide a voltage or frequency output signal proportional to the turning rate, and 2) rate integrating gyros, which indicate the actual turn angle [Udd, 1991]. Unlike the magnetic compass, however, rate integrating gyros can only measure relative as opposed to absolute angular position, and must be initially referenced to a known orientation by some external means.

A typical gyroscope configuration is shown in Figure 2.1. The electrically driven rotor is suspended in a pair of precision low-friction bearings at either end of the rotor axle. The rotor bearings are in turn supported by a circular ring, known as the inner gimbal ring; this inner gimbal ring pivots on a second set of bearings that attach it to the outer gimbal ring. This pivoting action of the inner gimbal defines the horizontal axis of the gyro, which is perpendicular to the spin axis of the rotor as shown in Figure 2.1. The outer gimbal ring is attached to the instrument frame by a third set of bearings that define the vertical axis of the gyro. The vertical axis is perpendicular to both the horizontal axis and the spin axis.

Notice that if this configuration is oriented such that the spin axis points east-west, the horizontal axis is aligned with the north-south meridian. Since the gyro is space-stable (i.e., fixed in the inertial reference frame), the horizontal axis thus reads the horizontal earth rate component of the planet's rotation, while the vertical axis reads the vertical earth rate component. If the spin axis is rotated 90 degrees to a north-south alignment, the earth's rotation does not affect the gyro's horizontal axis, since that axis is now orthogonal to the horizontal earth rate component.


Figure 2.1: Typical two-axis mechanical gyroscope configuration [Everett, 1995].

### 2.1.2 Gyrocompasses

The gyrocompass is a special configuration of the rate integrating gyroscope, employing a gravity reference to implement a north-seeking function that can be used as a true-north navigation reference. This phenomenon, first demonstrated in the early 1800s by Leon Foucault, was patented in Germany by Herman Anschutz-Kaempfe in 1903, and in the U.S. by Elmer Sperry in 1908 [Carter, 1966]. The U.S. and German navies had both introduced gyrocompasses into their fleets by 1911 [Martin, 1986].

The north-seeking capability of the gyrocompass is directly tied to the horizontal earth rate component measured by the horizontal axis. As mentioned earlier, when the gyro spin axis is oriented in a north-south direction, it is insensitive to the earth's rotation, and no tilting occurs. From this it follows that if tilting is observed, the spin axis is no longer aligned with the meridian. The direction and magnitude of the measured tilt are directly related to the direction and magnitude of the misalignment between the spin axis and true north.

### 2.1.3 Commercially Available Mechanical Gyroscopes

Numerous mechanical gyroscopes are available on the market. Typically, these precision machined gyros can cost between $\$ 10,000$ and $\$ 100,000$. Lower cost mechanical gyros are usually of lesser quality in terms of drift rate and accuracy. Mechanical gyroscopes are rapidly being replaced by modern high-precision - and recently — low-cost fiber-optic gyroscopes. For this reason we will discuss only a few low-cost mechanical gyros, specifically those that may appeal to mobile robotics hobbyists.

### 2.1.3.1 Futaba Model Helicopter Gyro

The Futaba FP-G154 [FUTABA] is a lowcost low-accuracy mechanical rate gyro designed for use in radio-controlled model helicopters and model airplanes. The Futaba FP-G154 costs less than $\$ 150$ and is available at hobby stores, for example [TOWER]. The unit comprises of the mechanical gyroscope (shown in Figure 2.2 with the cover removed) and a small control amplifier. Designed for weight-sensitive model helicopters, the system weighs only 102 grams ( 3.6 oz ). Motor and amplifier run off a 5 V DC supply and consume only 120 mA . However, sensitivity and accuracy are orders


Figure 2.2: The Futaba FP-G154 miniature mechanical gyroscope for radio-controlled helicopters. The unit costs less than $\$ 150$ and weighs only $102 \mathrm{~g} \mathrm{( } 3.6 \mathrm{oz}$ ). of magnitude lower than "professional" mechanical gyroscopes. The drift of radio-control type gyroscopes is on the order of tens of degrees per minute.

### 2.1.3.2 Gyration, Inc.

The GyroEngine made by Gyration, Inc. [GYRATION], Saratoga, CA, is a low-cost mechanical gyroscope that measures changes in rotation around two independent axes. One of the original applications for which the GyroEngine was designed is the GyroPoint, a three-dimensional pointing device for manipulating a cursor in three-dimensional computer graphics. The GyroEngine model GE9300-C has a typical drift rate of about $9^{\circ} / \mathrm{min}$. It weighs only 40 grams ( 1.5 oz ) and compares in size with that of a roll of 35 millimeter film (see Figure 2.3). The sensor can be pow-


Figure 2.3: The Gyration GyroEngine compares in size favorably with a roll of 35 mm film (courtesy Gyration, Inc.). ered with 5 to 15 VDC and draws only 65 to 85 mA during operation. The open collector outputs can be readily interfaced with digital circuits. A single GyroEngine unit costs $\$ 295$.

### 2.2 Piezoelectric Gyroscopes

Piezoelectric vibrating gyroscopes use Coriolis forces to measure rate of rotation. in one typical design three piezoelectric transducers are mounted on the three sides of a triangular prism. If one of the transducers is excited at the transducer's resonance frequency (in the Gyrostar it is 8 kHz ),
the vibrations are picked up by the two other transducers at equal intensity. When the prism is rotated around its longitudinal axis, the resulting Coriolis force will cause a slight difference in the intensity of vibration of the two measuring transducers. The resulting analog voltage difference is an output that varies linearly with the measured rate of rotation.


Figure 2.4: The Murata Gyrostar ENV-05H is a piezoelectric vibrating gyroscope. (Courtesy of [Murata]).

One popular piezoelectric vibrating gyroscope is the ENV-05 Gyrostar from [MURATA], shown in Fig. 2.4. The Gyrostar is small, lightweight, and inexpensive: the model ENV-05H measures $47 \times 40 \times 22 \mathrm{~mm}$ ( $1.9 \times 1.6 \times 0.9$ inches), weighs 42 grams ( 1.5 oz ) and costs $\$ 300$. The drift rate, as quoted by the manufacturer, is very poor: $9^{\circ} / \mathrm{s}$. However, we believe that this number is the worst case value, representative for extreme temperature changes in the working environment of the sensor. When we tested a Gyrostar Model ENV-05H at the University of Michigan, we measured drift rates under typical room temperatures of $0.05^{\circ} / \mathrm{s}$ to $0.25^{\circ} / \mathrm{s}$, which equates to 3 to $15^{\circ} / \mathrm{min}$ (see [Borenstein and Feng, 1996]). Similar drift rates were reported by Barshan and Durrant-Whyte [1995], who tested an earlier model: the Gyrostar ENV-05S (see Section 5.4.2.1 for more details on this work). The scale factor, a measure for the useful sensitivity of the sensor, is quoted by the manufacturer as $22.2 \mathrm{mV} / \mathrm{deg} / \mathrm{sec}$.

### 2.3 Optical Gyroscopes

Optical rotation sensors have now been under development as replacements for mechanical gyros for over three decades. With little or no moving parts, such devices are virtually maintenance free and display no gravitational sensitivities, eliminating the need for gimbals. Fueled by a large
market in the automotive industry, highly linear fiber-optic versions are now evolving that have wide dynamic range and very low projected costs.

The principle of operation of the optical gyroscope, first discussed by Sagnac [1913], is conceptually very simple, although several significant engineering challenges had to be overcome before practical application was possible. In fact, it was not until the demonstration of the heliumneon laser at Bell Labs in 1960 that Sagnac's discovery took on any serious implications; the first operational ring-laser gyro was developed by Warren Macek of Sperry Corporation just two years later [Martin, 1986]. Navigation quality ring-laser gyroscopes began routine service in inertial navigation systems for the Boeing 757 and 767 in the early 1980s, and over half a million fiber-optic navigation systems have been installed in Japanese automobiles since 1987 [Reunert, 1993]. Many technological improvements since Macek's first prototype make the optical rate gyro a potentially significant influence on mobile robot navigation in the future.

The basic device consists of two laser beams traveling in opposite directions (i.e., counter propagating) around a closed-loop path. The constructive and destructive interference patterns formed by splitting off and mixing parts of the two beams can be used to determine the rate and direction of rotation of the device itself.

Schulz-DuBois [1966] idealized the ring laser as a hollow doughnut-shaped mirror in which light follows a closed circular path. Assuming an ideal 100-percent reflective mirror surface, the optical energy inside the cavity is theoretically unaffected by any rotation of the mirror itself. The counterpropagating light beams mutually reinforce each other to create a stationary standing wave of intensity peaks and nulls as depicted in Figure 2.5, regardless of whether the gyro is rotating [Martin, 1986].
A simplistic visualization based on the Schulz-DuBois idealization is perhaps helpful at this point in understanding the fundamental concept of operation before more detailed treatment of the subject is presented. The light and dark fringes of the nodes are analogous to the reflective stripes or slotted holes in the rotating disk of an incremental optical encoder, and can be theoretically counted in similar fashion by a light detector mounted on the cavity wall. (In this analogy, however, the standing-wave "disk" is fixed in the inertial reference frame, while the normally stationary detector revolves around it.) With each full rotation of the mirrored doughnut, the detector would see a number of node peaks equal to twice the optical path length of the beams divided by the wavelength of the light.


Figure 2.5: Standing wave created by counter-propagating light beams in an idealized ring-laser gyro. (Adapted from [Schulz-DuBois, 1966].)

Obviously, there is no practical way to implement this theoretical arrangement, since a perfect mirror cannot be realized in practice. Furthermore, the introduction of light energy into the cavity (as well as the need to observe and count the nodes on the standing wave) would interfere with the mirror's performance, should such an ideal capability even exist. However, many practical embodiments of optical rotation sensors have been developed for use as rate gyros in navigation applications. Five general configurations will be discussed in the following subsections:

- Active optical resonators (2.3.1).
- Passive optical resonators (2.3.2).
- Open-loop fiber-optic interferometers (analog) (2.3.3).
- Closed-loop fiber-optic interferometers (digital) (2.3.4).
- Fiber-optic resonators (2.3.5).

Aronowitz [1971], Menegozzi and Lamb [1973], Chow et al. [1985], Wilkinson [1987], and Udd [1991] provide in-depth discussions of the theory of the ring-laser gyro and its fiber-optic derivatives. A comprehensive treatment of the technologies and an extensive bibliography of preceding works is presented by Ezekial and Arditty [1982] in the proceedings of the First International Conference on Fiber-Optic Rotation Sensors held at MIT in November, 1981. An excellent treatment of the salient features, advantages, and disadvantages of ring laser gyros versus fiber optic gyros is presented by $\operatorname{Udd}[1985,1991]$.

### 2.3.1 Active Ring Laser Gyros

The active optical resonator configuration, more commonly known as the ring laser gyro, solves the problem of introducing light into the doughnut by filling the cavity itself with an active lazing medium, typically helium-neon. There are actually two beams generated by the laser, which travel around the ring in opposite directions. If the gyro cavity is caused to physically rotate in the counterclockwise direction, the counterclockwise propagating beam will be forced to traverse a slightly longer path than under stationary conditions. Similarly, the clockwise propagating beam will see its closed-loop path shortened by an identical amount. This phenomenon, known as the Sagnac effect, in essence changes the length of the resonant cavity. The magnitude of this change is given by the following equation [Chow et al., 1985]:

$$
\begin{equation*}
\Delta L=\frac{4 \pi r^{2} \Omega}{c} \tag{2.2}
\end{equation*}
$$

where

```
\(\Delta L=\) change in path length
\(r=\) radius of the circular beam path
\(\Omega=\) angular velocity of rotation
\(c=\) speed of light.
```

Note that the change in path length is directly proportional to the rotation rate $\Omega$ of the cavity. Thus, to measure gyro rotation, some convenient means must be established to measure the induced change in the optical path length.

This requirement to measure the difference in path lengths is where the invention of the laser in the early 1960s provided the needed technological breakthrough that allowed Sagnac's observations to be put to practical use. For lazing to occur in the resonant cavity, the round-trip beam path must
be precisely equal in length to an integral number of wavelengths at the resonant frequency. This means the wavelengths (and therefore the frequencies) of the two counter- propagating beams must change, as only oscillations with wavelengths satisfying the resonance condition can be sustained in the cavity. The frequency difference between the two beams is given by [Chow et al., 1985]:

$$
\begin{equation*}
\Delta f=\frac{2 f r \Omega}{c}=\frac{2 r \Omega}{\lambda} \tag{2.3}
\end{equation*}
$$

where
$\Delta f=$ frequency difference
$r=$ radius of circular beam path
$\Omega=$ angular velocity of rotation
$\lambda=$ wavelength.
In practice, a doughnut-shaped ring cavity would be hard to realize. For an arbitrary cavity geometry, the expression becomes [Chow et al., 1985]:
$\Delta f=\frac{4 A \Omega}{P \lambda}$
where
$\Delta f=$ frequency difference
$A=$ area enclosed by the closed-loop beam path
$\Omega=$ angular velocity of rotation
$P=$ perimeter of the beam path
$\lambda$ = wavelength.
For single-axis gyros, the ring is generally formed by aligning three highly reflective mirrors to create a closed-loop triangular path as shown in Figure 2.6. (Some systems, such as Macek's early prototype, employ four mirrors to create a square path.) The mirrors are usually mounted to a monolithic glass-ceramic block with machined ports for the cavity bores and electrodes. Most modern three-axis units employ a square block cube with a total of six mirrors, each mounted to the center of a block face as shown in Figure 2.6. The most stable systems employ linearly polarized light and minimize circularly polarized components to avoid magnetic sensitivities [Martin, 1986].

The approximate quantum noise limit for the ring-laser gyro is due to spontaneous emission in the gain medium [Ezekiel and Arditty, 1982]. Yet, the ring-laser gyro represents the "best-case" scenario of the five general gyro configurations outlined above. For this reason the active ring-laser gyro offers the highest sensitivity and is perhaps the most accurate implementation to date.

The fundamental disadvantage associated with the active ring laser is a problem called frequency lock-in, which occurs at low rotation rates when the counter-propagating beams "lock" together in frequency [Chao et al., 1984]. This lock-in is attributed to the influence of a very small amount of backscatter from the mirror surfaces, and results in a deadband region (below a certain threshold of rotational velocity) for which there is no output signal. Above the lock-in threshold, output approaches the ideal linear response curve in a parabolic fashion.

The most obvious approach to solving the lock-in problem is to improve the quality of the mirrors to reduce the resulting backscatter. Again, however, perfect mirrors do not exist, and some finite
amount of backscatter will always be present. Martin [1986] reports a representative value as $10^{-12}$ of the power of the main beam; enough to induce frequency lock-in for rotational rates of several hundred degrees per hour in a typical gyro with a 20 -centimeter ( 8 -in) perimeter.


Figure 2.6: Six-mirror configuration of three-axis ring-laser gyro. (Adapted from [Koper, 1987].)

An additional technique for reducing lock-in is to incorporate some type of biasing scheme to shift the operating point away from the deadband zone. Mechanical dithering is the least elegant but most common biasing means, introducing the obvious disadvantages of increased system complexity and reduced mean time between failures due to the moving parts. The entire gyro assembly is rotated back and forth about the sensing axis in an oscillatory fashion. State-of-the-art dithered active ring laser gyros have a scale factor linearity that far surpasses the best mechanical gyros.

Dithered biasing, unfortunately, is too slow for high-performance systems (i.e., flight control), resulting in oscillatory instabilities [Martin, 1986]. Furthermore, mechanical dithering can introduce crosstalk between axes on a multi-axis system, although some unibody three-axis gyros employ a common dither axis to eliminate this possibility [Martin, 1986].

Buholz and Chodorow [1967], Chesnoy [1989], and Christian and Rosker [1991] discuss the use of extremely short duration laser pulses (typically $1 / 15$ of the resonator perimeter in length) to reduce the effects of frequency lock-in at low rotation rates. The basic idea is to reduce the crosscoupling between the two counter-propagating beams by limiting the regions in the cavity where the two pulses overlap. Wax and Chodorow [1972] report an improvement in performance of two orders of magnitude through the use of intracavity phase modulation. Other techniques based on non-linear optics have been proposed, including an approach by Litton that applies an external magnetic field to the cavity to create a directionally dependent phase shift for biasing [Martin, 1986]. Yet another solution to the lock-in problem is to remove the lazing medium from the ring altogether, effectively forming what is known as a passive ring resonator.

### 2.3.2 Passive Ring Resonator Gyros



Figure 2.7: Passive ring resonator gyro with laser source external to the ring cavity. (Adapted from [Udd, 1991].)

The passive ring resonator gyro makes use of a laser source external to the ring cavity (Figure 2.7), and thus avoids the frequency lock-in problem which arises when the gain medium is internal to the cavity itself. The passive configuration also eliminates problems arising from changes in the optical path length within the interferometer due to variations in the index of refraction of the gain medium [Chow et al., 1985]. The theoretical quantum noise limit is determined by photon shot noise and is slightly higher (i.e., worse) than the theoretical limit seen for the active ring-laser gyro [Ezekiel and Arditty, 1982].

The fact that these devices use mirrored resonators patterned after their active ring predecessors means that their packaging is inherently bulky. However, fiber-optic technology now offers a low volume alternative. The fiber-optic derivatives also allow longer length multi-turn resonators, for increased sensitivity in smaller, rugged, and less expensive packages. As a consequence, the Resonant Fiber-Optic Gyro (RFOG), to be discussed in Section 2.1.2.5, has emerged as the most popular of the resonator configurations [Sanders, 1992].

### 2.3.3 Open-Loop Interferometric Fiber Optic Gyros

The concurrent development of optical fiber technology, spurred mainly by the communications industry, presented a potential low-cost alternative to the high-tolerance machining and clean-room assembly required for ring-laser gyros. The glass fiber in essence forms an internally reflective waveguide for optical energy, along the lines of a small-diameter linear implementation of the doughnut-shaped mirror cavity conceptualized by Schulz-DuBois [1966].

Recall the refractive index $n$ relates the speed of light in a particular medium to the speed of light in a vacuum as follows:

$$
\begin{equation*}
\mathrm{n}=\frac{\mathrm{c}}{\mathrm{c}_{\mathrm{m}}} \tag{2.5}
\end{equation*}
$$

where
$\mathrm{n}=$ refractive index of medium
$\mathrm{c}=$ speed of light in a vacuum
$\mathrm{c}_{\mathrm{m}}=$ speed of light in medium.
Step-index multi-mode fiber (Figure 2.8) is made up of a core region of glass with index of refraction $n_{c o}$, surrounded by a protective cladding with a lower index of refraction $n_{1}$ [Nolan and Blaszyk, 1991]. The lower refractive index in the cladding is necessary to ensure total internal reflection of the light propagating through the core region. The terminology step index refers to this "stepped" discontinuity in the refractive index that occurs at the core-cladding interface.
Referring now to Figure 2.8, as long as the entry angle (with respect to the waveguide axis) of an incoming ray is less than a certain critical angle $\theta_{c}$, the ray will be guided down the fiber, virtually without loss. The numerical aperture of the fiber quantifies this parameter of acceptance (the lightcollecting ability of the fiber) and is defined as follows [Nolan and Blaszyk, 1991]:

$$
\begin{equation*}
\mathrm{NA}=\sin \theta_{\mathrm{c}}=\sqrt{\mathrm{n}_{\mathrm{co}}^{2}-\mathrm{n}_{\mathrm{cl}}^{2}} \tag{2.6}
\end{equation*}
$$

where
$\mathrm{NA}=$ numerical aperture of the fiber
$\theta_{c}=$ critical angle of acceptance
$\mathrm{n}_{\mathrm{co}}=$ index of refraction of glass core
$\mathrm{n}_{\mathrm{cl}}=$ index of refraction of cladding.


Figure 2.8: Step-index multi-mode fiber. (Adapted from [Nolan et al., 1991].)

As illustrated in Figure 2.9, a number of rays following different-length paths can simultaneously propagate down the fiber, as long as their respective entry angles are less than the critical angle of acceptance $\theta_{c}$. Multiple-path propagation of this nature occurs where the core diameter is much larger than the wavelength of the guided energy, giving rise to the term multi-mode fiber. Such multi-mode operation is clearly undesirable in gyro applications, where the objective is to eliminate all nonreciprocal conditions other than that imposed by the Sagnac effect itself. As the diameter of the core is reduced to approach the operating wavelength, a cutoff condition is reached where just a single mode is allowed to propagate, constrained to travel only along the waveguide axis [Nolan and Blaszyk, 1991].

Light can randomly change polariza tion states as it propagates through standard single-mode fiber. The use of special polarization-maintaining fiber, such as PRSM Corning, maintains the original polarization state of the light along the path of travel [Reunert, 1993]. This is important, since light of different polarization states travels through an optical fiber at different speeds.

Numerical aperture


Figure 2.9: Entry angles of incoming rays 1 and 2 determine propagation paths in fiber core. (Adapted from [Nolan et al., 1991].)

A typical block diagram of the "minimum-reciprocal" IFOG configuration is presented in Figure 2.10. Polarization-maintaining single-mode fiber [Nolan and Blaszyk, 1991] is employed to ensure the two counter-propagating beams in the loop follow identical paths in the absence of rotation.

An interesting characteristic of the IFOG is the absence of any laser source [Burns et al., 1983], the enabling technology allowing the Sagnac effect to reach practical implementation in the first place. A low-coherence source, such as a super-luminescent diode (SLD), is typically employed instead to reduce the effects of noise [Tai et al., 1986], the primary source of which is backscattering within the fiber and at any interfaces. As a result, in addition to the two primary counter-propagating waves in the loop, there are also a number of parasitic waves that yield secondary interferometers [Lefevre, 1992]. The limited temporal coherence of the broadband SLD causes any interference due to backscattering to average to zero, suppressing the contrast of these spurious interferometers. The detection system becomes sensitive only to the interference between waves that followed identical paths [Ezekiel and Arditty, 1982; Lefevre, 1992].

The Sagnac phase shift introduced by rotation is given by [Ezekiel and Arditty, 1982]

$$
\begin{equation*}
\Delta \phi=\frac{2 \pi \mathrm{LD}}{\lambda \mathrm{c}} \tag{2.7}
\end{equation*}
$$

where
$\Delta \phi=$ measured phase shift between counter-propagating beams
$\mathrm{L}=$ length of fiber-optic cable in loop
D = diameter of loop
$\lambda \quad=$ wavelength of optical energy
c = speed of light in a vacuum.
The stability of the scale factor relating $\Delta \phi$ to the rotational velocity in the equation above is thus limited to the stability of L, D, and $\lambda$ [Ezekiel and Arditty, 1982]. Practical implementations usually operate over plus or minus half a fringe (i.e., $\pm \pi$ rad of phase difference), with a theoretical sensitivity of $10^{-6}$ radians or less of phase shift [Lefevre, 1992].

IFOG sensitivity may be improved by increasing L (i.e., adding turns of fiber in the sensing loop). This effect peaks at an optimal length of several kilometers, after which the fiber attenuation (typically $1 \mathrm{~dB} / \mathrm{km}$ ) begins to degrade performance. This large amount of fiber represents a significant percentage of overall system cost.


Figure 2.10: Block diagram of "minimum-reciprocal" integrated fiber-optic gyro. (Adapted from [Lefevre, 1992].)

In summary, the open-loop IFOG is attractive from the standpoint of reduced manufacturing costs. Additional advantages include high tolerance to shock and vibration, insensitivity to gravity effects, quick start-up, and good sensitivity in terms of bias drift rate and the random walk coefficient. Coil geometry is not critical, and no path length control is needed. Some disadvantages are that a long optical cable is required, dynamic range is limited with respect to active ring-laser gyros, and the scale factor is prone to vary [Adrian, 1991]. Open-loop configurations are therefore most suited to the needs of low-cost systems in applications that require relatively low accuracy (i.e., automobile navigation).

For applications demanding higher accuracy, such as aircraft navigation ( 0.01 to $0.001^{\circ} / \mathrm{hr}$ ), the closed-loop IFOG to be discussed in the next section offers significant promise.

### 2.3.4 Closed-Loop Interferometric Fiber Optic Gyros

This new implementation of a fiber-optic gyro provides feedback to a frequency or phase shifting element. The use of feedback results in the cancellation of the rotationally induced Sagnac phase shift. However, closed-loop digital signal processing is considerably more complex than the analog signal processing employed on open-loop IFOG configurations [Adrian, 1991]. Nonetheless, it now seems that the additional complexity is justified by the improved stability of the gyro: closed-loop IFOGs are now under development with drifts in the 0.001 to $0.01^{\circ} / \mathrm{hr}$ range, and scale-factor stabilities greater than 100 ppm (parts per million) [Adrian, 1991].

### 2.3.5 Resonant Fiber Optic Gyros

The resonant fiber optic gyro (RFOG) evolved as a solid-state derivative of the passive ring resonator gyro discussed in Section 2.1.2.2. In the solid-state implementation, a passive resonant cavity is formed from a multi-turn closed loop of optical fiber. An input coupler provides a means for injecting frequency-modulated light from a laser source into the resonant loop in both the clockwise and counterclockwise directions. As the frequency of the modulated light passes through a value such that the perimeter of the loop precisely matches an integral number of wavelengths at that frequency, input energy is strongly coupled into the loop [Sanders, 1992]. In the absence of loop rotation, maximum coupling for both beam directions occurs in a sharp peak centered at this resonant frequency.

If the loop is caused to rotate in the clockwise direction, of course, the Sagnac effect causes the perceived loop perimeter to lengthen for the clockwise-traveling beam, and to shorten for the counterclockwise-traveling beam. The resonant frequencies must shift accordingly, and as a result, energy is coupled into the loop at two different frequencies and directions during each cycle of the sinusoidal FM sweep. An output coupler samples the intensity of the energy in the loop by passing a percentage of the two counter-rotating beams to their respective detectors. The demodulated output from these detectors will show resonance peaks, separated by a frequency difference $f$ given by the following [Sanders, 1992]:
$\Delta f=\frac{D}{\lambda n} \Omega$
where
$\Delta f=$ frequency difference between counter-propagating beams
$D=$ diameter of the resonant loop
$\Omega=$ rotational velocity
$\lambda=$ freespace wavelength of laser
$n$ = refractive index of the fiber.
Like the IFOG, the all-solid-state RFOG is attractive from the standpoint of high reliability, long life, quick start-up, and light weight. The principle advantage of the RFOG, however, is that it requires significantly less fiber (from 10 to 100 times less) in the sensing coil than the IFOG configuration, while achieving the same shot-noise-limited performance [Sanders, 1992]. Sanders attributes this to the fact that light traverses the sensing loop multiple times, as opposed to once in the IFOG counterpart. On the down side are the requirements for a highly coherent source and extremely low-loss fiber components [Adrian, 1991].

### 2.3.6 Commercially Available Optical Gyroscopes

Only recently have optical fiber gyros become commercially available at a price that is suitable for mobile robot applications. In this section we introduce two such systems.

### 2.3.6.1 The Andrew "Autogyro"

Andrew Corp. [ANDREW] offers the low-cost Autogyro, shown in Figure 2.11, for terrestrial navigation. It is a single-axis interferometric fiber-optic gyroscope (see Sec. 2.1.2.3) based on polarization-maintaining fiber and precision fiber-optic gyroscope technology. Model 3ARG-A (\$950) comes with an analog output, while model 3ARG-D $(\$ 1,100)$ has an RS-232 output for connection to a computer. Technical specifications for the 3ARG-D are given in Table 2.1. Specifications for the 3ARG-A are similar. A more detailed discussion of the Autogyro is given

Table 2.1: Selected specifications for the Andrew Autogyro Model 3ARG-D. (Courtesy of [Andrew Corp].)

| Parameter | Value | Units |
| :--- | ---: | :--- |
| Input rotation rate | $\pm 100$ | $\% / \mathrm{s}$ |
| Minimum detectable | $\pm 0.05$ | $\% / \mathrm{s}$ |
| rotation rate | $\pm 180$ | $\% / \mathrm{hr}$ |
| Rate bandwidth | 100 Hz |  |
| Bias drift (at stabilized | $0.005 \% / \mathrm{s} \mathrm{rms}$ |  |
| temperature) - RMS | 18 | $\% / \mathrm{hr} \mathrm{rms}$ |
| Size | 77 dia $\times 88 \mathrm{~mm}$ |  |
| (excluding connector) | 3.0 dia $\times 3.5 \mathrm{in}$ |  |
| Weight (total) | 0.63 kg |  |
|  | 1.38 | lb |
| Power | 9 to 18 VDC |  |
|  | 630 mA |  |



Figure 2.11: The Andrew Autogyro Model 3ARG. (Courtesy of [Andrew Corp].)

Table 2.1: Selected specifications for the Andrew Autogyro Navigator (Courtesy of [Andrew Corp].)

| Parameter | Value | Units |
| :--- | ---: | :--- |
| Input rotation rate | $\pm 100$ | $\% / \mathrm{s}$ |
| Instantaneous |  |  |
| bandwidth | 100 Hz |  |
| Bias drift (at stabilized |  |  |
| temperature) - RMS | 0.005 | $\% / \mathrm{s} \mathrm{rms}$ |
| Size | 18 | $\% / \mathrm{hr} \mathrm{rms}$ |
| (excluding connector) | $4.5 \times 30 \times 41 \mathrm{~mm}$ |  |
| Weight (total) | 0.25 in |  |
|  | 0.55 | lb |
| Power Analog | $<2$ | W |
| Power Digital | $<3$ | W |

in [Allen et al., 1994; Bennett and Emge, 1994].

In fall 1995 Andrew Corporation announced a newer model, called the AUTOGYRO Navigator. This laser gyro, shown in Fig. 2.12, is only one third the weight, consume only half the power, and cost $15 \%$ less than its predecessor, the AUTOGYRO.


Figure 2.12: The Andrew AUTOGYRO Navigator. (Courtesy of [Andrew Corp].)

### 2.3.6.2 Hitachi Cable Ltd. OFG-3

Hitachi Cable Ltd. markets an optical fiber gyroscope called OFG-3 (see Figure 2.13). Komoriya and Oyama [1994] tested that sensor and found its drift rate to be quite linear with $0.00317^{\circ} / \mathrm{s}\left(11.4^{\circ} / \mathrm{hr}\right)$. This result is close to the advertised specification of $10^{\circ} / \mathrm{hr}$. This low drift rate is substantially better than that provided by conventional (mechanical) gyros. Table 2.2 shows technical specifications of the OFG-3 gyro, as reported by Komoriya and Oyama [1994].

One point to keep in mind when considering the use of fiber optic gyros in mobile robot applications is the minimum detectable rotation rate. This rate happens to be the same for both the Andrew 3ARG-A and the Hitachi OFG-3 gyros: $0.05^{\circ} / \mathrm{s}$. If either gyro was installed on a robot with a systematic error (e.g., due to unequal wheel diameters; see Sec. 5.1 for more details) of 1 degree per 10 meter linear travel, then neither gyro would detect this systematic error at speeds lower than $0.5 \mathrm{~m} / \mathrm{s}$.

Table 2.2: Selected specifications for the Hitachi Cable Ltd. OFG-3 fiber optic gyroscope. (Reprinted with permission from [Komoriya and Oyama, 1994].)

| Parameter | Value Units |
| :--- | ---: |
| Input rotation rate | $\pm 100 \% / \mathrm{s}$ |
| Minimum | $\pm 0.05 \% / \mathrm{s}$ |
| detectable rotation | $\pm 60 \% / \mathrm{hr}$ |
| rate | 10 ms |
| Min. sampl. interval | $0.0028 \% / \mathrm{s}$ |
| Zero drift (rate | $10 \% / \mathrm{hr}$ |
| integration) | $88(\mathrm{~W}) \times 88(\mathrm{~L}) \times 65(\mathrm{H}) \mathrm{mm}$ |
| Size | $3.5(\mathrm{~W}) \times 3.5(\mathrm{~L}) \times 2.5(\mathrm{H}) \mathrm{in}$ |
|  | 0.48 kg |
| Weight (total) | 1.09 lb |
|  | 12 VDC |
| Power | $150-250 \mathrm{~mA}$ |



Figure 2.13: The OFG-3 optical fiber gyro made by Hitachi Cable Ltd. (Courtesy of Hitachi Cable America, Inc. [HITACHI].)

### 2.4 Geomagnetic Sensors

Vehicle heading is the most significant of the navigation parameters ( $\mathrm{x}, \mathrm{y}$, and $\theta$ ) in terms of its influence on accumulated dead-reckoning errors. For this reason, sensors which provide a measure of absolute heading or relative angular velocity are extremely important in solving the real world navigation needs of an autonomous platform. The most commonly known sensor of this type is probably the magnetic compass. The terminology normally used to describe the intensity of a magnetic field is magnetic flux density $B$, measured in Gauss (G). Alternative units are the Tesla (T), and the gamma ( $\gamma$ ), where 1 Tesla $=10^{4}$ Gauss $=10^{9}$ gamma.

The average strength of the earth's magnetic field is 0.5 Gauss and can be represented as a dipole that fluctuates both in time and space, situated roughly 440 kilometers off center and inclined 11 degrees to the planet's axis of rotation [Fraden, 1993]. This difference in location between true north and magnetic north is known as declination and varies with both time and geographical location. Corrective values are routinely provided in the form of declination tables printed directly on the maps or charts for any given locale.

Instruments which measure magnetic fields are known as magnetometers. For application to mobile robot navigation, only those classes of magnetometers which sense the magnetic field of the earth are of interest. Such geomagnetic sensors, for purposes of this discussion, will be broken down into the following general categories:

- Mechanical magnetic compasses.
- Fluxgate compasses.
- Hall-effect compasses.
- Magnetoresistive compasses.
- Magnetoelastic compasses.

Before we introduce different types of compasses, a word of warning: the earth's magnetic field is often distorted near power lines or steel structures [Byrne et al., 1992]. This makes the straightforward use of geomagnetic sensors difficult for indoor applications. However, it may be possible to overcome this problem in the future by fusing data from geomagnetic compasses with data from other sensors.

### 2.4.1 Mechanical Magnetic Compasses

The first recorded use of a magnetic compass was in 2634 B.C., when the Chinese suspended a piece of naturally occurring magnetite from a silk thread and used it to guide a chariot over land [Carter, 1966]. Much controversy surrounds the debate over whether the Chinese or the Europeans first adapted the compass for marine applications, but by the middle of the $13^{\text {th }}$ century such usage was fairly widespread around the globe. William Gilbert [1600] was the first to propose that the earth itself was the source of the mysterious magnetic field that provided such a stable navigation reference for ships at sea.

The early marine compasses were little more that magnetized needles floated in water on small pieces of cork. These primitive devices evolved over the years into the reliable and time proven systems in use today, which consist of a ring magnet or pair of bar magnets attached to a graduated mica readout disk. The magnet and disk assembly floats in a mixture of water and alcohol or glycerine, such that it is free to rotate around a jeweled pivot. The fluid acts to both support the weight of the rotating assembly and to dampen its motion under rough conditions.

The sealed vessel containing the compass disk and damping fluid is typically suspended from a 2-degree-of-freedom gimbal to decouple it from the ship's motion. This gimbal assembly is mounted in turn atop a floor stand or binnacle. On either side of the binnacle are massive iron spheres that, along with adjustable permanent magnets in the base, are used to compensate the compass for surrounding magnetic abnormalities that alter the geomagnetic lines of flux. The error resulting from such external influences (i.e., the angle between indicated and actual bearing to magnetic north) is known as compass deviation, and along with local declination, must be added or subtracted as appropriate for true heading:
$H_{t}=H_{i} \pm C F_{\mathrm{dev}} \pm C F_{\mathrm{dec}}$
where
$H_{t} \quad=$ true heading
$H_{i} \quad$ indicated heading
$C F_{\text {dev }}=$ correction factor for compass deviation
$C F_{\text {dec }}=$ correction factor for magnetic declination.
Another potential source of error which must be taken into account is magnetic dip, a term arising from the "dipping" action observed in compass needles attributed to the vertical component of the geomagnetic field. The dip effect varies with latitude, from no impact at the equator where the flux lines are horizontal, to maximum at the poles where the lines of force are entirely vertical. For this reason, many swing-needle instruments have small adjustable weights that can be moved radially to balance the needle for any given local area of operation. Marine compasses ensure alignment in the horizontal plane by floating the magnet assembly in an inert fluid.

## Dinsmore Starguide Magnetic Compass

An extremely low-cost configuration of the mechanical magnetic compass suitable for robotic applications is seen in a product recently announced by the Dinsmore Instrument Company, Flint, MI. The heart of the Starguide compass is the Dinsmore model 1490 digital sensor [Dinsmore Instrument Company, 1991], which consists of a miniaturized permanent-magnet rotor mounted in low-friction jeweled bearings. The sensor is internally damped such that if momentarily displaced 90 degrees, it will return to the indicated direction in 2.5 seconds, with no overshoot.

Four Hall-effect switches corresponding to the cardinal headings (N, E, W, S) are arranged around the periphery of the rotor and activated by the south pole of the magnet as the rotor aligns itself with the earth's magnetic field. Intermediate headings (NE, NW, SE, SW) are indicated through simultaneous activation of the adjacent cardinal-heading switches. The Dinsmore Starguide is not a true Hall-effect compass (see Sec. 2.4.3), in that the Hall-effect devices are not directly sensing the geomagnetic field of the earth, but rather the angular position of a mechanical rotor.

The model 1490 digital sensor measures 12.5 millimeters ( 0.5 in ) in diameter by 16 millimeters ( 0.63 in ) high, and is available separately from Dinsmore for around $\$ 12$. Current consumption is 30 mA , and the open-collector NPN outputs can sink 25 mA per channel. Grenoble [1990] presents a simple circuit for interfacing the device to eight indicator LEDs. An alternative analog sensor (model 1525) with a ratiometric sine-cosine output is also available for around $\$ 35$. Both sensors may be subjected to unlimited magnetic flux without damage.

### 2.4.2 Fluxgate Compasses

There currently is no practical alternative to the popular fluxgate compass for portability and long missions [Fenn et al., 1992]. The term fluxgate is actually a trade name of Pioneer Bendix for the saturable-core magnetometer, derived from the gating action imposed by an AC-driven excitation coil that induces a time varying permeability in the sensor core. Before discussing the principle of operation, it is probably best to review briefly the subject of magnetic conductance, or permeability.

The permeability $\mu$ of a given material is a measure of how well it serves as a path for magnetic lines of force, relative to air, which has an assigned permeability of one. Some examples of highpermeability materials are listed in Table 2.3.

Permeability is the magnetic circuit analogy to electrical conductivity, and relates magnetic flux density to the magnetizing force as follows:
$B=\mu H$
where
$B=$ magnetic flux density
$\mu=$ permeability
$H=$ magnetizing force.

Table 2.3: Permeability ranges for selected materials. Values vary with proportional make-up, heat treatment, and mechanical working of the material [Bolz and Tuve, 1979].

| Material | Permeability $\boldsymbol{\mu}$ |
| :--- | ---: |
| Supermalloy | $100,000-1,000,000$ |
| Pure iron | $25,000-300,000$ |
| Mumetal | $20,000-100,000$ |
| Permalloy | $2,500-25,000$ |
| Cast iron | $100-600$ |

Since the magnetic flux in a magnetic circuit is analogous to current $I$ in an electrical circuit, it follows that magnetic flux density $B$ is the parallel to electrical current density.

A graphical plot of the above equation is known as the normal magnetizing curve, or $\mathrm{B}-\mathrm{H}$ curve, and the permeability $\mu$ is the slope. An example plot is depicted in Figure 2.14 for the case of mild
steel. In actuality, due to hysteresis, $\mu$ depends not only on the current value of $H$, but also the history of previous values and the sign of $\mathrm{d} H / \mathrm{d} t$, as will be seen later. The important thing to note at this point in the discussion is the $B-H$ curve is not linear, but rather starts off with a fairly steep slope, and then flattens out suddenly as $H$ reaches a certain value. Increasing $H$ beyond this "knee" of the $B-H$ curve yields little increase in $B$; the material is effectively saturated, with a near-zero permeability.


Figure 2.14: The slope of the B-H curve, shown here for cast iron and sheet steel, describes the permeability of a magnetic material, a measure of its ability (relative to air) to conduct a magnetic flux. (Adapted from [Carlson and Gisser, 1981].)

When a highly permeable material is introduced into a uniform magnetic field, the lines of force are drawn into the lower resistance path presented by the material as shown in Figure 2.15. However, if the material is forced into saturation by some additional magnetizing force $H$, the lines of flux of the external field will be relatively unaffected by the presence of the saturated material, as indicated in Figure 2.15b. The fluxgate magnetometer makes use of this saturation phenomenon in order to directly measure the strength of a surrounding static magnetic field.

Various core materials have been employed in different fluxgate designs over the past 50 years, with the two most common being permalloy (an alloy of iron and nickel) and mumetal (iron, nickel,


Figure 2.15: External lines of flux for: a. unsaturated core, b. saturated core. (Adapted from [Lenz, 1990].)
copper, and chromium). The permeable core is driven into and out of saturation by a gating signal applied to an excitation coil wound around the core. For purposes of illustration, let's assume for the moment a square-wave drive current is applied. As the core moves in and out of saturation, the flux lines from the external B field to be measured are drawn into and out of the core, alternating in turn between the two states depicted in Figure 2.15. (This is somewhat of an oversimplification, in that the B-H curve does not fully flatten out with zero slope after the knee.) These expanding and collapsing flux lines will induce positive and negative EMF surges in a sensing coil properly oriented around the core. The magnitude of these surges will vary with the strength of the external magnetic field, and its orientation with respect to the axis of the core and sensing coil of the fluxgate configuration. The fact that the permeability of the sensor core can be altered in a controlled fashion by the excitation coil is the underlying principle which enables the DC field being measured to induce a voltage in the sense coil. The greater the differential between the saturated and unsaturated states (i.e., the steeper the slope), the more sensitive the instrument will be.

An idealized B-H curve for an alternating H-field is shown in Figure 2.16. The permeability (i.e., slope) is high along the section b-c of the curve, and falls to zero on either side of the saturation points $\mathrm{H}_{\mathrm{s}}$ and $-\mathrm{H}_{\mathrm{s}}$, along segments $\mathrm{c}-\mathrm{d}$ and $\mathrm{a}-\mathrm{b}$, respectively. Figure 2.16 shows a more representative situation: the difference between the left- and right-hand traces is due to hysteresis caused by some finite amount of permanent magnetization of the material. When a positive magnetizing force $\mathrm{H}_{\mathrm{s}}$ is applied, the material will saturate with flux density $B_{s}$ at point $P_{1}$ on the curve. When the magnetizing force is removed (i.e., $\mathrm{H}=0$ ), the flux density drops accordingly, but does not return to zero. Instead, there remains some residual magnetic flux density $\mathrm{B}_{\mathrm{r}}$, shown at point $\mathrm{P}_{2}$, known as the retentivity.

A similar effect is seen in the application of an H -field of opposite polarity. The flux density goes into saturation at point $P_{3}$, then passes through point $P_{4}$ as the field reverses. This hysteresis effect can create what is known as a zero offset (i.e., some DC bias is still present when the external B-field is zero) in fluxgate magnetometers. Primdahl (1970) provides an excellent mathematical analysis of the actual gating curves for fluxgate devices.

The effective permeability $\mu_{\mathrm{a}}$ of a material is influenced to a significant extent by its geometry. Bozorth and Chapin [1942] showed how $\mu_{\mathrm{a}}$ for a cylindrical rod falls off with a decrease in the length-to-diameter ratio. This relationship can be attributed to the so-called demagnetization factor [Hine, 1968]. When a ferrous rod is coaxially aligned with the lines of flux of a magnetic field, a magnetic dipole is developed in the rod itself. The associated field introduced by the north and south poles of this dipole opposes the ambient field, with a corresponding reduction of flux density through the rod. The lowered value of $\mu_{\mathrm{a}}$ results in a less sensitive magnetometer, in that the "flux-gathering"


Figure 2.16: a. Ideal B-H curve.
b. Some minor hysteresis in the actual curve results in a residual non-zero value of B when H is reduced to zero, known as the retentivity. (Adapted from Halliday and Resnick, 1974; Carlson and Gisser, 1981).
capability of the core is substantially reduced.
Consider again the cylindrical rod sensor presented in Figure 2.17, now in the absence of any external magnetic field $\mathrm{B}_{\mathrm{e}}$. When the drive coil is energized, there will be a strong coupling between the drive coil and the sense coil. Obviously, this will be an undesirable situation since the output signal is supposed to be related to the strength of the external field only.

One way around this problem is seen in the Vacquier configuration developed in the early 1940s, where two parallel rods collectively form the core, with a common sense coil [Primdahl, 1979] as illustrated in Figure 2.17. The two rods are simultaneously forced into and out of saturation, excited in antiphase by identical but oppositely wound solenoidal drive windings. In this fashion, the magnetization fluxes of the two drive windings effectively cancel each other, with no net effect on the sense coil.

Bridges of magnetic material may be employed to couple the ends of the two coils together in a closed-loop fashion for more complete flux linkage through the core. This configuration is functionally very similar to the ring-core design first employed in 1928 by Aschenbrenner and Goubau [Geyger, 1957]. An alternative technique for decoupling the pickup coil from the drive coil is to arrange the two in an orthogonal fashion. In practice, there are a number of different implementations of various types of sensor cores and coil configurations as described by Stuart [1972] and Primdahl [1979]. These are generally divided into two classes, parallel and orthogonal, depending on whether the


Figure 2.17: Identical but oppositely wound drive windings in the Vacquier configuration cancel the net effect of drive coupling into the surrounding sense coil, while still saturating the core material. (Adapted from [Primdahl, 1979].)
excitation H -field is parallel or perpendicular to the external B-field being measured. Alternative excitation strategies (sine wave, square wave, sawtooth ramp) also contribute to the variety of implementations seen in the literature. Hine [1968] outlines four different classifications of saturable inductor magnetometers based on the method of readout (i.e., how the output EMF is isolated for evaluation):

- Fundamental frequency.
- Second harmonic.
- Peak output.
- Pulse difference.

Unambiguous 360-degree resolution of


Figure 2.18: Two channel ring core fluxgate with toroidal excitation. (Adapted from [Acuna and Pellerin, 1969].) the earth's geomagnetic field requires two sensing coils at right angles to each other. The ring-core geometry lends itself to such dual-axis applications in that two orthogonal pickup coils can be configured in a symmetrical fashion around a common core. A follow-up version developed by Gordon and Lundsten [1970] employed a toroidal excitation winding as shown in Figure 2.19. Since there are no distinct poles in a closed-ring design, demagnetization effects, although still present [Stuart, 1972], are less severe. The use of a ring geometry also leads to more complete flux linkage throughout the core, implying less required drive excitation for lower power operation, and the zero offset can be minimized by rotating the circular core. For these reasons, along with ease of manufacture, toroidal ring-core sensors are commonly employed in many of the low-cost fluxgate compasses available today.

The integrated DC output voltages $\mathrm{V}_{\mathrm{x}}$ and $\mathrm{V}_{\mathrm{y}}$ of the orthogonal sensing coils vary as sine and cosine functions of $\theta$, where $\theta$ is the angle of the sensor unit relative to the earth's magnetic field. The instantaneous value of $\theta$ can be easily derived by performing two successive $A / D$ conversions on these voltages and taking the arctangent of their quotient:


Figure 2.19: The Sperry Flux Valve consisted of a common drive winding $P$ in the center of three sense windings $S$ symmetrically arranged $120^{\circ}$ apart. (Adapted from [Hine, 1968].)
$\theta=\arctan \frac{\mathrm{V}_{\mathrm{x}}}{\mathrm{V}_{\mathrm{y}}}$.

Another popular two-axis core design is seen in the Flux Valve magnetometer developed by Sperry Corp. [SPERRY] and shown in Figure 2.19. This three-legged spider configuration employs three horizontal sense coils 120 degrees apart, with a common vertical excitation coil in the middle [Hine, 1968]. Referring to Figure 2.20, the upper and lower "arms" of the sense coil S are excited by the driving coil D , so that a magnetizing force $\mathrm{H}_{\mathrm{x}}$ developed as indicated by the arrows. In the absence of an external field $\mathrm{H}_{\mathrm{e}}$, the flux generated in the upper and lower arms by the excitation coil is equal and opposite due to symmetry.

When this assembly is placed in an axial magnetic field $\mathrm{H}_{\mathrm{e}}$, however, the instantaneous excitation field $\mathrm{H}_{\mathrm{x}}$ complements the flow in one arm, while opposing the flow in the other. This condition is periodically reversed in the arms, of course, due to the alternating nature of the driving function. A second-harmonic output is induced in the sensing coil S, proportional to the strength and orientation of the ambient field. By observing the relationships between the magnitudes of the output signals from each of the three sense coils (see Figure 2.20), the angular relationship of the Flux Valve with respect to the external field can be unambiguously determined.


Figure 2.20: The Flux Valve magnetometer developed by Sperry Corporation uses a spider-core configuration. (Adapted from [Lenz, 1990].)

When maintained in a level attitude, the fluxgate compass will measure the horizontal component of the earth's magnetic field, with the decided advantages of low power consumption, no moving parts, intolerance to shock ad vibration, rapid start-up, and relatively low cost. If the vehicle is expected to operate over uneven terrain, the sensor coil should be gimbal-mounted and mechanically dampened to prevent serious errors introduced by the vertical component of the geomagnetic field.

### 2.4.2.1 Zemco Fluxgate Compasses

The Zemco fluxgate compass [ZEMCO] was used in earlier work by Everett et al. [1990] on their robot called ROBART II. The sensor was a fluxgate compass manufactured by Zemco Electronics, San Ramon, CA, model number DE-700. This very low-cost (around \$40) unit featured a rotating analog dial and was originally intended for 12 VDC operation in automobiles.

A system block diagram is presented in Figure 2.21. The sensor consists of two orthogonal pickup coils arranged around a toroidal excitation coil, driven in turn by a local oscillator. The outputs $V_{x}$ and $V_{\mathrm{y}}$ of amplifier channels A and B are applied across an air-core resolver to drive the display indicator. The standard resolver equations [ILC Corporation, 1982] for these two voltages are
$V_{\mathrm{x}}=K_{\mathrm{x}} \sin \theta \sin \left(\omega t+a_{\mathrm{x}}\right)$
$V_{y}=K_{\mathrm{y}} \cos \theta \sin \left(\omega t+a_{y}\right)$
where
$\theta=$ the resolver shaft angle
$\omega=2 \pi f$, where $f$ is the excitation frequency.
$K_{x}$ and $K_{y}$ are ideally equal transfer-function constants, and $a_{x}$ and $a_{y}$ are ideally zero time-phase shifts.

Thus, for any static spatial angle $\theta$, the equations reduce to
$V_{\mathrm{x}}=K_{\mathrm{x}} \sin \theta$
$V_{\mathrm{y}}=K_{\mathrm{y}} \cos \theta$
which can be combined to yield
$\frac{V_{x}}{V_{Y}}=\frac{\sin \theta}{\cos \theta}=\tan \theta$.

The magnetic heading $\theta$ therefore is simply the arctangent of $V_{x}$ over $V_{y}$.

Everett [1995] recounts his experience with two models of the Zemco fluxgate compass on ROBART II as follows:

Problems associated with the use of this particular fluxgate compass on ROBART, however, included a fairly high current consumption (250 mA), and stiction in the resolver reflecting back as a load into the drive circuitry, introducing some error for minor


Figure 2.21: Block diagram of ZEMCO Model DE-700 fluxgate compass. (Courtesy of ZEMCO, Inc.)
changes in vehicle heading. In addition, the sensor itself was affected by surrounding magnetic anomalies, some that existed on board the robot (i.e., current flow in nearby cable runs, drive and head positioning motors), and some present in the surrounding environment (metal desks, bookcases, large motors, etc.).

The most serious interference turned out to be the fluctuating magnetic fields due to power cables in close proximity - on the order of 30 centimeters ( 12 in) - to the fluxgate sensor. As various auxiliary systems on board the robot were turned on when needed and later deactivated to save power, the magnetic field surrounding the sensor would change accordingly. Serious errors could be introduced as well by minor changes in the position of cable runs, which occurred as a result of routine maintenance and trouble shooting. These problems were minimized by securing all cable runs with plastic tie-downs, and adopting a somewhat standardized protocol regarding which auxiliary systems would be activated when reading the compass.
There was no solution, however, for the interference effects of large metallic objects within the operating environment, and deviations of approximately four degrees were observed when passing within 30 centi-meters ( 12 in ) of a large metal cabinet, for example. A final source of error was introduced by virtue of the fact that the fluxgate compass had been mounted on the robot's head, so as to be as far away as possible from the effects of the drive motors and power distribution lines discussed above. The exact head position could only be read to within 0.82 degrees due to the limited resolution of the 8 -bit $A / D$ converter. In any event, an overall system error of $\pm 10$ degrees was typical, and grossly insufficient for reliable dead-reckoning calculations, which was not the original intent of the compass.

This analog compass was later replaced by a newer digital version produced by Zemco, model DE-710, which cost approximately $\$ 90$. The system block diagram is shown in Figure 2.22. This unit contained a built-in ADC0834 A/D converter to read the amplified outputs of the two sensor channels, and employed its own COP 421-MLA microprocessor, which drove a liquid crystal display (LCD). All communication between the A/D converter, microprocessor, and display driver was serial in nature, with a resulting slow update rate of 0.25 Hz . The built-in LCD simulated an analog dial with an extremely coarse resolution of $20^{\circ}$ between display increments, but provision


Figure 2.22: Block diagram of ZEMCO model DE-710 fluxgate compass (courtesy ZEMCO, Inc.).
was made for serial output to an optional external shift register and associated three-digit numerical display.

All things considered, it was determined to be more practical to discard the built-in microprocessor, $A / D$ converter, and $L C D$ display, and interface an external $A / D$ converter directly to the amplifier outputs as before with the analog version. This resulted in a decrease in supply current from 168 to 94 mA . Power consumption turned out to be less of a factor when it was discovered the circuitry could be powered up for a reading, and then deactivated afterwards with no noticeable effect on accuracy.

Overall system accuracy for this configuration was typically $\pm 6$ degrees, although a valid comparison to the analog version is not possible since the digital model was mounted in a different location to minimize interference from nearby circuitry. The amount of effort put into the calibration of the two systems must also be taken into account; the calibration procedure as performed was an iterative process not easily replicated from unit to unit with any quantitative measure.

### 2.4.2.2 Watson Gyrocompass

A combination fluxgate compass and solid-state rate gyro package (part number FGM-G100DHSRS232) is available from Watson Industries, Eau Claire, WI [WATSON]. The system contains its own microprocessor that is intended to integrate the information from both the rate gyro and the compass to provide a more stable output less susceptible to interference, with an update rate of 40 Hz . An overall block diagram is presented in Figure 2.23.


Figure 2.22: Block diagram of Watson fluxgate compass and rate gyro combination. (Courtesy of [WATSON].)

The Watson fluxgate/rate gyro combination balances the shortcomings of each type of device: the gyro serves to filter out the effects of magnetic anomalies in the surrounding environment, while the compass counters the long-term drift of the gyro. Furthermore, the toroidal ring-core fluxgate sensor is gimbal-mounted for improved accuracy.

The Watson unit measures $6.3 \times 4.4 \times 7.6$ centimeters ( $2.5 \times 1.75 \times 3.0 \mathrm{in}$ ) and weighs only 275 grams $(10 \mathrm{oz})$. This integrated package is a much more expensive unit $(\$ 2,500)$ than the low-cost Zemco fluxgate compass, but is advertised to have higher accuracy $\left( \pm 2^{\circ}\right)$. Power supply requirements are 12 VDC at 200 mA , and the unit provides an analog voltage output as well as a 12-bit digital output over a 2400 -baud RS- 232 serial link.

### 2.4.2.3 KVH Fluxgate Compasses

KVH Industries, Inc., Middletown, RI, offers a complete line of fluxgate compasses and related accessories, ranging from inexpensive units targeted for the individual consumer up through sophisticated systems intended for military applications [KVH]. The C100 COMPASS ENGINE (see Figure 2.24) is a versatile low-cost (less than $\$ 700$ ) developer's kit that includes a microprocessorcontrolled stand-alone fluxgate sensor subsystem based on a two-axis toroidal ring-core sensor.


Figure 2.24: The C -100 fluxgate compass engine was tested at the University of Michigan in a flying robot prototype. (Courtesy of [KVH].)

Two different sensor options are offered with the C-100: 1) the SE-25 sensor, recommended for applications with a tilt range of $\pm 16$ degrees and 2 ) the SE-10 sensor, for applications anticipating a tilt angle of up to $\pm 45$ degrees. The SE- 25 sensor provides internal gimballing by floating the sensor coil in an inert fluid inside the lexan housing. The SE-10 sensor provides an additional 2-degree-offreedom pendulous gimbal in addition to the internal fluid suspension. The SE- 25 sensor mounts on top of the sensor PC board, while the SE-10 is suspended beneath it. The sensor PC board can be
separated as much as 122 centimeters ( 48 in ) from the detachable electronics PC board with an optional cable if so desired.

The resolution of the C100 is $\pm 0.1$ degrees, with an advertised accuracy of $\pm 0.5$ degrees (after compensation, with the sensor card level) and a repeatability of $\pm 0.2$ degrees. Separate $\pm 180$ degree adjustments are provided for declination as well as index offset (in the event the sensor unit cannot be mounted in perfect alignment with the vehicle's axis of travel). System damping can be userselected, anywhere in the range of 0.1 to 24 seconds settling time to final value.

An innovative automatic compensation algorithm employed in the C100 is largely responsible for the high accuracy obtained by such a relatively low-priced system. This software routine runs on the controlling microprocessor mounted on the electronics board and corrects for magnetic anomalies associated with the host vehicle. Three alternative user-selectable procedures are offered:

- Eight-Point Auto-Compensation - starting from an arbitrary heading, the platform turns full circle, pausing momentarily at approximately 45 -degree intervals. No known headings are required.
- Circular Auto-Compensation - Starting from an arbitrary position, the platform turns slowly through a continuous 360 -degree circle. No known headings are required.
- Three-Point Auto-Compensation - Starting from an arbitrary heading, the platform turns and pauses on two additional known headings approximately 120 degrees apart.

Correction values are stored in a look-up table in non-volatile EEPROM memory. The automatic compensation routine also provides a quantitative indicator of the estimated quality of the current compensation and the magnitude of any magnetic interference present [KVH Industries, 1993].

The C100 configured with an SE-25 coil assembly weighs just 62 grams ( 2.25 oz ) and draws 40 mA at 8 to 18 VDC (or 18 to 28 VDC ). The combined sensor and electronics boards measure $4.6 \times 11$ centimeters ( $1.8 \times 4.5 \mathrm{in}$ ). RS-232 ( 300 to 9600 baud) and NMEA 0183 digital outputs are provided, as well as linear and sine/cosine analog voltage outputs. Display and housing options are also available.

### 2.4.3 Hall-Effect Compasses

Hall-effect sensors are based on E. H. Hall's observation (in 1879) that a DC voltage develops across a conductor or semiconductor when in the presence of an external magnetic field. One advantage of this technology (i.e., relative to the fluxgate) is the inherent ability to directly sense a static flux, resulting in much simpler readout electronics. Early Hall magnetometers could not match the sensitivity and stability of the fluxgate [Primdahl, 1979], but the sensitivity of Hall devices has improved significantly. The more recent indium-antimonide devices have a lower sensitivity limit of $10^{-3}$ Gauss [Lenz, 1990].

The U.S. Navy in the early 1960s showed considerable interest in a small solid-state Hall-effect compass for low-power extended operations in sonobuoys [Wiley, 1964]. A number of such prototypes were built and delivered by Motorola for evaluation. The Motorola Hall-effect compass employed two orthogonal Hall elements for temperature-nulled non-ambiguous resolution of the geomagnetic field vector. Each sensor element was fabricated from a $2 \times 2 \times 0.1$ millimeter indium-arsenide-ferrite sandwich, and inserted between two wing-like mumetal flux concentrators as shown in Figure 2.25. It is estimated the 5 centimeter ( 2 in ) magnetic concentrators increased the flux density through the sensing elements by two orders of magnitude [Wiley, 1964]. The output of the Motorola unit was a variable-width pulse train, the width of the pulse being proportional to the


Figure 2.25: A pair of indium-arsenide-ferrite Hall-effect sensors (one shown) are positioned between flux concentrating wings of mumetal in this early Motorola prototype. (Adapted from [Wiley, 1964].)
sensed magnetic heading. Excellent response linearity was reported down to flux densities of 0.001 Gauss [Willey, 1962].

Maenaka et al. [1990] report on the development of a monolithic silicon magnetic compass at the Toyohashi University of Technology in Japan, based on two orthogonal Hall-effect sensors. Their use of the terminology "magnetic compass" is perhaps an unfortunate misnomer in that the prototype device was tested with an external field of 1,000 Gauss. Contrast this with the strength of the earth's magnetic field, which varies from only about 0.1 Gauss at the equator to about 0.9 Gauss at the poles. Silicon-based Hall-effect sensors have a lower sensitivity limit of around 10 Gauss [Lenz, 1990]. It is likely the Toyohashi University device was intended for other than geomagnetic applications, such as remote position sensing of rotating mechanical assemblies.

This prototype Hall-effect magnetometer is still of interest in that it represents a fully selfcontained implementation of a two-axis magnetometer in integrated circuit form. Two vertical Hall cells [Maenaka et al., 1987] are arranged at right angles (see Figure 2.25) on a $4.7 \mathrm{~mm}^{2}$ chip, with their respective outputs coupled to a companion signal processing IC of identical size. (Two separate chips were fabricated for the prototype instead of a single integrated unit to enhance production yield.) The sensor and signal processing ICs are interconnected (along with some external variable resistors for calibration purposes) on a glass-epoxy printed circuit board.

The dedicated signal-processing circuitry converts the B-field components $B_{x}$ and $B_{y}$ measured by the Hall sensors into an angle $\theta$ by means of the analog operation [Maenaka et al., 1990]:
$\theta=\arctan \frac{B_{x}}{B_{y}}$
where
$\theta=$ angle between B-field axis and sensor
$B_{x}=x$-component of B-field
$B_{y}=y$-component of B-field.
The analog output of the signal-processing IC is a DC voltage which varies linearly with vector orientation of the ambient magnetic field in a plane parallel to the chip surface. Reported test results show a fairly straight-line response (i.e., $\pm 2$ percent full scale) for external field strengths ranging from 8,000 Gauss down to 500 Gauss; below this level performance begins to degrade rapidly [Maenaka et al., 1990]. A second analog output on the IC provides an indication of the absolute value of field intensity.

While the Toyohashi "magnetic compass" prototype based on silicon Hall-effect technology is incapable of detecting the earth's magnetic field, it is noteworthy nonetheless. A two-axis monolithic device of a similar nature employing the more sensitive indium-antimonide Hall devices could potentially have broad appeal for low-cost applications on mobile robotic platforms. An alternative possibility would be to use magnetoresistive sensor elements, which will be discussed in the next section.

### 2.4.4 Magnetoresistive Compasses

The general theory of operation for AMR and GMR magnetoresistive sensors for use in short-range proximity detection is beyond the scope of this text. However, there are three specific properties of the magnetoresistive magnetometer that make it well suited for use as a geomagnetic sensor: 1) high sensitivity, 2) directionality, and, in the case of AMR sensors, 3) the characteristic "flipping" action associated with the direction of internal magnetization.

AMR sensors have an open-loop sensitivity range of $10^{-2}$ Gauss to 50 Gauss (which easily covers the 0.1 to 1.0 Gauss range of the earth's horizontal magnetic field component), and limitedbandwidth closed-loop sensitivities approaching $10^{-6}$ Gauss [Lenz, 1990]. Excellent sensitivity, low power consumption, small package size, and decreasing cost make both AMR and GMR sensors increasingly popular alternatives to the more conventional fluxgate designs used in robotic vehicle applications.

### 2.4.4.1 Philips AMR Compass

One of the earliest magnetoresistive sensors to be applied to a magnetic compass application is the KMZ10B offered by Philips Semiconductors BV, The Netherlands [Dibburn and Petersen, 1983; Kwiatkowski and Tumanski, 1986; Petersen, 1989]. The limited sensitivity of this device (approximately $0.1 \mathrm{mV} / \mathrm{A} / \mathrm{m}$ with a supply voltage of 5 VDC ) in comparison to the earth's maximum horizontal magnetic field ( $15 \mathrm{~A} / \mathrm{m}$ ) means that considerable attention must be given to error-inducing effects of temperature and offset drift [Petersen, 1989].

One way around these problems is to exploit the "flipping" phenomenon by driving the device back and forth between its two possible magnetization states with square-wave excitation pulses applied to an external coil (Figure 2.26). This switching action toggles the sensor's axial magnetic field as shown in Figure 2.26a, resulting in the alternating response characteristics depicted in Figure 2.26b. Since the sensor offset remains unchanged while the signal output due to the external magnetic field $H_{\mathrm{y}}$ is inverted (Figure 2.26a), the undesirable DC offset voltages can be easily isolated from the weak AC signal.

A typical implementation of this strategy is shown in Figure 2.27 . A 100 Hz square wave generator is capacitively coupled to the external excitation coil L which surrounds two orthogonally mounted magnetoresistive sensors. The sensors' output signals are amplified and AC-coupled to a


Figure 2.26: External current pulses set and reset the direction of magnetization, resulting in the "flipped" response characteristics shown by the dashed line. Note the DC offset of the device remains constant, while the signal output is inverted. (Adapted from [Petersen, 1989].)
synchronous detector driven by the same square-wave source. The rectified DC voltages $\mathrm{V}_{\mathrm{H} 1}$ and $\mathrm{V}_{\mathrm{H} 2}$ are thus proportional to the measured magnetic field components $\mathrm{H}_{1}$ and $\mathrm{H}_{2}$. The applied field direction is dependant on the ratio of V to H , not their absolute values. This means that as long as the two channels are calibrated to the same sensitivity, no temperature correction is required [Fraden, 1993].

### 2.4.5 Magnetoelastic Compasses

A number of researchers have recently investigated the use of magnetoelastic (also known as magnetostrictive) materials as sensing elements for high-resolution magnetometers. The principle of operation is based on the changes in Young's modulus experienced by magnetic alloys when exposed to an external magnetic field. The modulus of elasticity $E$ of a given material is basically a measure of its stiffness, and directly relates stress to strain as follows:

$$
\begin{equation*}
E=\frac{\sigma}{\epsilon} \tag{2.16}
\end{equation*}
$$

where
$\mathrm{E}=$ Young's modulus of elasticity
$\sigma=$ applied stress
$\epsilon=$ resulting strain.
Any ferromagnetic material will experience some finite amount of strain (expansion or shrinkage) in the direction of magnetization due to this magnetostriction phenomenon. It stands to reason that if the applied stress $\sigma$ remains the same, strain $\epsilon$ will vary inversely with any change in Young's modulus E. In certain amorphous metallic alloys, this effect is very pronounced.

Barrett et al. [1973] proposed a qualitative explanation, wherein individual atoms in the crystal lattice are treated as tiny magnetic dipoles. The forces exerted by these dipoles on one another depend upon their mutual orientation within the lattice; if the dipoles are aligned end to end, the opposite


Figure 2.27: Block diagram of a two-axis magnetic compass system based on a commercially available anisotropic magnetoresistive sensor from Philips [Petersen, 1989].
poles attract, and the material shrinks ever so slightly. The crystal is said to exhibit a negative magnetostriction constant in this direction. Conversely, if the dipoles are rotated into side-by-side alignment through the influence of some external field, like poles will repel, and the result is a small expansion.

It follows that the strength of an unknown magnetic field can be accurately measured if a suitable means is employed to quantify the resulting change in length of some appropriate material displaying a high magnetostriction constant. There are currently at least two measurement technologies with the required resolution allowing the magnetoelastic magnetometer to be a realistic contender for highsensitivity low-cost performance: 1) interferometric displacement sensing, and 2) tunneling-tip displacement sensing.

Lenz [1990] describes a magnetoelastic magnetometer which employs a Mach-Zender fiber-optic interferometer to measure the change in length of a magnetostrictive material when exposed to an external magnetic field. A laser source directs a beam of light along two optical fiber paths by way of a beam splitter as shown in Figure 2.28. One of the fibers is coated with a material (nickel iron was used) exhibiting a high magnetostrictive constant. The length of this fiber is stretched or compressed


Figure 2.28: Fiber-optic magnetometers, basically a Mach-Zender interferometer with one fiber coated or attached to a magnetoelastic material, have a sensitivity range of $10^{-7}$ to 10 Gauss. (Adapted from [Lenz, 1990].)
in conjunction with any magnetoelastic expansion or contraction of its coating. The output beam from this fiber-optic cable is combined in a light coupler with the output beam from the uncoated reference fiber and fed to a pair of photodetectors.

Constructive and destructive interferences caused by differences in path lengths associated with the two fibers will cause the final output intensity as measured by the photodetectors to vary accordingly. This variation is directly related to the change in path length of the coated fiber, which in turn is a function of the magnetic field strength along the fiber axis. The prototype constructed by Lenz [1990] at Honeywell Corporation measured $10 \times 2.5$ centimeters ( $4 \times 1 \mathrm{in}$ ) and was able to detect fields ranging from $10^{-7}$ Gauss up to 10 Gauss.

Researchers at the Naval Research Laboratory (NRL) have developed a prototype magnetoelastic magnetometer capable of detecting a field as small as $6 \times 10^{-5}$ Gauss [Brizzolara et al., 1989] using the tunneling-tip approach. This new displacement sensing technology, invented in 1982 at IBM Zürich, is based on the measurement of current generated by quantum mechanical tunneling of electrons across a narrow gap (Figure 2.29). An analog feedback circuit compares the measured tunnel current with a desired value and outputs a drive signal to suitably adjust the distance between the tunneling electrodes with an electromechanical actuator [Kenny et al., 1991]. The instantaneous tunneling current is directly proportional to the exponential of electrode displacement. The most common actuators employed in this role are piezoelectric and electrostatic, the latter lending itself more readily to silicon micro-machining techniques.


Figure 2.29: Scanning tunneling microscopy, invented at IBM Zürich in 1982, uses quantum mechanical tunneling of electrons across a barrier to measure separation distance at the gap. (Courtesy of T. W. Kenny, NASA JPL).

The active sense element in the NRL magnetometer is a 10 centimeter ( 4 in ) metallic glass ribbon made from METGLAS 2605S2, annealed in a transverse magnetic field to yield a high magnetomechanical coupling [Brizzolara et al., 1989]. (METGLAS is an alloy of iron, boron, silicon, and carbon, and is a registered trademark of Allied Chemical.) The magnetoelastic ribbon elongates when exposed to an axial magnetic field, and the magnitude of this displacement is measured by a tunneling transducer as illustrated in Figure 2.30.

An electrochemically etched gold tip is mounted on a tubular piezoelectric actuator and positioned within about one nanometer of the free end of the METGLAS ribbon. The ribbon and tip are electrically biased with respect to each other, establishing a tunneling current that is fed back to the piezo actuator to maintain a constant gap separation. The degree of magnetically induced elongation of the ribbon can thus be inferred from the driving voltage applied to the piezoelectric actuator. The solenoidal coil shown in the diagram supplies a bias field of 0.85 oersted to shift the sensor into its region of maximum sensitivity.


Figure 2.30: The NRL tunneling-transducer magnetometer employed a 10 cm (4 in) magnetoelastic ribbon vertically supported in a quartz tube [Brizzolara et al., 1989].

Fenn et al. [1992] propose an alternative tunneling-tip magnetoelastic configuration with a predicted sensitivity of $2 \times 10^{-11}$ Gauss, along the same order of magnitude as the cryogenically cooled SQUID. A small cantilevered beam of METGLAS 2605S2, excited at its resonant frequency by a gold-film electrostatic actuator, is centered between two high-permeability magnetic flux concentrators as illustrated in Figure 2.31. Any changes in the modulus of elasticity of the beam will directly affect its natural frequency; these changes in natural frequency can then be measured and directly related to the strength of the ambient magnetic field. The effective shift in natural frequency is rather small, however (Fenn et al. [1992] report only a 6 Hz shift at saturation), again necessitating a very precise method of measurement.


Figure 2.31: Top view of the single cantilevered design. (Adapted from [Fenn, et al., 1992].)
A second (non-magnetic) cantilever element is employed to track the displacement of the METGLAS reed with sub-angstrom resolution using tunneling-tip displacement sensing as illustrated in Figure 2.32. A pair of electrostatic actuator plates dynamically positions the reed follower to maintain a constant tunneling current in the probe gap, thus ensuring a constant lateral separation between the probe tip and the vibrating reed. The frequency of the excitation signal applied to the reed-follower actuator is therefore directly influenced by any resonant frequency changes occurring in the METGLAS reed. The magnetometer provides an analog voltage output which is proportional to this excitation frequency, and therefore indicative of the external magnetic field amplitude.


Figure 2.32: Side view of the double cantilevered design. (Adapted from [Fenn et al., 1992].)

## Chapter 3 <br> Ground-Based RF-Beacons and GPS

In this chapter we discuss sensors used for active beacon navigation. Active beacons have been used for many centuries as a reliable and accurate means for navigation. Stars can be considered as active beacons with respect to navigation; and lighthouses were early man-made beacon systems. Typical non-robotics applications for active beacon navigation include marine navigation, aircraft navigation, race car performance analysis, range instrumentation, unmanned mobile target control, mine localization, hazardous materials mapping, dredge positioning, geodetic surveys, and most recently, position location and range information for golfers [Purkey, 1994].

Modern technology has vastly enhanced the capabilities of active beacon systems with the introduction of laser, ultrasonic, and radio-frequency (RF) transmitters. It should be noted, though, that according to our conversations with manufacturers, none of the RF systems can be used reliably in indoor environments. Ground-based RF systems will be discussed in Section 3.1.
However, the most revolutionary technology for outdoor navigation is the recently completed Global Positioning System (GPS). Because of the rapidly increasing popularity of GPSs we have dedicated a large portion of this chapter to this subject. Section 3.2 explains GPS technology, Section 3.3 includes a major comparative study of five different GPS receivers [Byrne, 1993], and Section 3.4 presents some state-of-the-art commercially available systems.

### 3.1 Ground-Based RF Systems

Ground-based RF position location systems are typically of two types:

- Passive hyperbolic line-of-position phase-measurement systems that compare the time-of-arrival phase differences of incoming signals simultaneously emitted from surveyed transmitter sites.
- Active radar-like trilateration systems that measure the round-trip propagation delays for a number of fixed-reference transponders. Passive systems are generally preferable when a large number of vehicles must operate in the same local area, for obvious reasons.


### 3.1.1 Loran

An early example of the first category is seen in Loran (short for long range navigation). Developed at MIT during World War II, such systems compare the time of arrival of two identical signals broadcast simultaneously from high-power transmitters located at surveyed sites with a known separation baseline. For each finite time difference (as measured by the receiver) there is an associated hyperbolic line of position as shown in Figure 3.1. Two or more pairs of master/slave stations are required to get intersecting hyperbolic lines resulting in a two-dimensional (latitude and longitude) fix.

The original implementation (Loran A) was aimed at assisting convoys of liberty ships crossing the North Atlantic in stormy winter weather. Two 100 kW slave transmitters were located about 200 miles on either side of the master station. Non-line-of-sight ground-wave propagation at around 2 MHz was employed, with pulsed as opposed to continuous-wave transmissions to aid in sky-wave


Figure 3.1: For each hyperbolic line-of-position, length ABC minus length AC equals some constant K. (Adapted from [Dodington, 1989].)
discrimination. The time-of-arrival difference was simply measured as the lateral separation of the two pulses on an oscilloscope display, with a typical accuracy of around $1 \mu \mathrm{~s}$. This numerical value was matched to the appropriate line of position on a special Loran chart of the region, and the procedure then repeated for another set of transmitters. For discrimination purposes, four different frequencies were used, 50 kHz apart, with 24 different pulse repetition rates in the neighborhood of 20 to 35 pulses per second [Dodington, 1989]. In situations where the hyperbolic lines intersected more or less at right angles, the resulting (best-case) accuracy was about 1.5 kilometers.

Loran A was phased out in the early ' 80 s in favor of Loran C, which achieves much longer over-the-horizon ranges through use of 5 MW pulses radiated from 400 -meter ( 1300 ft ) towers at a lower carrier frequency of 100 kHz . For improved accuracy, the phase differences of the first three cycles of the master and slave pulses are tracked by phase-lock-loops in the receiver and converted to a digital readout, which is again cross-referenced to a preprinted chart. Effective operational range is about 1000 miles, with best-case accuracies in the neighborhood of 100 meters ( 330 ft ). Coverage is provided by about 50 transmitter sites to all U.S. coastal waters and parts of the North Atlantic, North Pacific, and the Mediterranean.

### 3.1.2 Kaman Sciences Radio Frequency Navigation Grid

The Unmanned Vehicle Control Systems Group of Kaman Sciences Corporation, Colorado Springs, CO, has developed a scaled-down version of a Loran-type hyperbolic position-location system known as the Radio Frequency Navigation Grid (RFNG). The original application in the late 1970s involved autonomous route control of unmanned mobile targets used in live-fire testing of the laserguided Copperhead artillery round [Stokes, 1989]. The various remote vehicles sense their position by measuring the phase differences in received signals from a master transmitter and two slaves situated at surveyed sites within a $30 \mathrm{~km}^{2}\left(18.75 \mathrm{mi}^{2}\right)$ area as shown in Figure 3.2. System resolution is 3 centimeters ( 1.5 in ) at a 20 Hz update rate, resulting in a vehicle positioning repeatability of 1 meter ( 3.3 ft ).

Path trajectories are initially taught by driving a vehicle over the desired route and recording the actual phase differences observed. This file is then played back at run time and compared to
measured phase difference values, with vehicle steering servoed in an appropriate manner to null any observed error signal. Velocity of advance is directly controlled by the speed of file playback. Vehicle speeds in excess of $50 \mathrm{~km} / \mathrm{h}(30 \mathrm{mph})$ are supported over path lengths of up to 15 kilometers ( 9.4 mi ) [Stokes, 1989]. Multiple canned paths can be stored and changed remotely, but vehicle travel must always begin from a known start point due to an inherent 6.3 meters ( 20 ft ) phase ambiguity interval associated with the grid [Byrne et al., 1992].

The Threat Array Control and Tracking Information Center (TACTIC) is offered by Kaman Sciences to augment the RFNG by tracking and displaying the location and orientation of up to 24 remote vehicles [Kaman, 1991]. Real-time telemetry and recording of vehicle heading, position, velocity, status, and other designated parameters (i.e., fuel level, oil pressure, battery voltage) are supported at a 1 Hz update rate. The TACTIC operator has direct control over engine start, automatic path playback, vehicle pause/resume, and emergency halt functions. Non-line-of-sight operation is supported through use of a 23.825 MHz grid frequency in conjunction with a 72 MHz control and communications channel.


Figure 3.2: Kaman Sciences 1500 W navigation grid is a scaled-down version of the LORAN concept, covering an area 8 to 15 km on a side with a position-location repeatability of 1 m . (Courtesy of Kaman Sciences Corporation.)

### 3.1.3 Precision Location Tracking and Telemetry System

Precision Technology, Inc., of Saline, MI, has recently introduced to the automotive racing world an interesting variation of the conventional phase-shift measurement approach (type 1 RF system). The company's Precision Location tracking and telemetry system employs a number of receive-only antennae situated at fixed locations around a racetrack to monitor a continuous sine wave transmission from a moving vehicle. By comparing the signals received by the various antennae to a common reference signal of identical frequency generated at the base station, relative changes in vehicle position with respect to each antenna can be inferred from resulting shifts in the respective
phase relationships. The 58 MHz VHF signal allows for non-line-of-sight operation, with a resulting precision of approximately 1 to 10 centimeters ( 0.4 to 4 in ) [Duchnowski, 1992]. From a robotics perspective, problems with this approach arise when more than one vehicle must be tracked. The system costs $\$ 200,000$ to $\$ 400,000$, depending on the number of receivers used. According to Duchnowski, the system is not suitable for indoor operations.

### 3.1.4 Motorola Mini-Ranger Falcon

An example of the active transponder category of ground-based RF position-location techniques is seen in the Mini-Ranger Falcon series of range positioning systems offered by the Government and Systems Technology Group of Motorola, Inc, Scottsdale, AZ [MOTOROLA]. The Falcon 484 configuration depicted in Figure 3.3 is capable of measuring line-of-sight distances from 100 meters ( 328 ft ) out to 75 kilometers ( 47 miles). An initial calibration is performed at a known location to determine the turn-around delay (TAD) for each transponder (i.e., the time required to transmit a response back to the interrogator after receipt of interrogation). The actual distance between the interrogator and a given transponder is found by [Byrne et al., 1992]:


Figure 3.7: Motorola's Mini-Ranger Falcon $484 R$ position-location system provides $2 \mathrm{~m}(6.5 \mathrm{ft})$ accuracy over ranges of 100 m to 75 km ( 328 ft to 47 mi ). (Courtesy of [MOTOROLA].)

$$
\begin{equation*}
D=\frac{\left(T_{e}-T_{d}\right) c}{2} \tag{3.1}
\end{equation*}
$$

where
$D=$ separation distance
$T_{\mathrm{e}}=$ total elapsed time
$T_{\mathrm{d}}=$ transponder turn-around delay
$c=$ speed of light.
The MC6809-based range processor performs a least-squares position solution at a $1-\mathrm{Hz}$ update rate, using range inputs from two, three, four, or 16 possible reference transponders. The individual reference stations answer only to uniquely coded interrogations and operate in C-band (5410 to 5890 MHz ) to avoid interference from popular X-band marine radars [Motorola, undated]. Up to 20
mobile users can time share the Falcon 484 system ( 50 ms per user maximum). System resolution is in tenths of units ( $\mathrm{m}, \mathrm{ft}$, or yd ) with a range accuracy of 2 meters ( 6.5 ft ) probable.

Power requirements for the fixed-location reference stations are 22 to 32 VDC at 13 W nominal, 8.5 W standby, while the mobile range processor and its associated transmitter-receiver and display unit draw 150 W at 22 to 32 VDC . The Falcon system comes in different, customized configurations. Complete system cost is $\$ 75,000$ to $\$ 100,000$.

### 3.1.5 Harris Infogeometric System

Harris Technologies, Inc., [HTI], Clifton, VA, is developing a ground-based R position location and communications strategy wherein moderately priced infogeometric (IG) devices cooperatively form self-organizing instrumentation and communication networks [Harris, 1994]. Each IG device in the network has full awareness of the identity, location, and orientation of all other IG devices and can communicate with other such devices in both party-line and point-to-point communication modes.

The IG devices employ digital code-division-multiple-access (CDMA) spread-spectrum R hardware that provides the following functional capabilities:

- Network level mutual autocalibration.
- Associative location and orientation tracking.
- Party-line and point-to-point data communications (with video and audio options).
- Distributed sensor data fusion.

Precision position location on the move is based on high-speed range trilateration from fixed reference devices, a method commonly employed in many instrumentation test ranges and other tracking system applications. In this approach, each beacon has an extremely accurate internal clock that is carefully synchronized with all other beacon clocks. A time-stamped (coded) R signal is periodically sent by each transmitter. The receiver is also equipped with a precision clock, so that it can compare the timing information and time of arrival of the incoming signals to its internal clock. This way, the system is able to accurately measure the signals' time of flight and thus the distance between the receiver and the three beacons. This method, known as "differential location regression" [Harris, 1994] is essentially the same as the locating method used in global positioning systems (GPS).

To improve accuracy over current range-lateration schemes, the HTI system incorporates mutual data communications, permitting each mobile user access to the time-tagged range measurements made by fixed reference devices and all other mobile users. This additional network-level range and timing information permits more accurate time synchronization among device clocks, and automatic detection and compensation for uncalibrated hardware delays.

Each omnidirectional CDMA spread-spectrum "geometric" transmission uniquely identifies the identity, location, and orientation of the transmitting source. Typically the available geometric measurement update rate is in excess of 1000 kHz . Harris quotes a detection radius of 500 meters (1640 ft) with 100 mW peak power transmitters. Larger ranges can be achieved with stronger transmitters. Harris also reports on "centimeter-class repeatability accuracy" obtained with a modified transmitter called an "Interactive Beacon." Tracking and communications at operating ranges of up to 20 kilometers ( 12.5 mi ) are also supported by higher transmission power levels of 1 to 3 W . Typical "raw data" measurement resolution and accuracies are cited in Table 3.1.

Enhanced tracking accuracies for selected applications can be provided as cited in Table 3.2. This significant improvement in performance is provided by sensor data fusion algorithms that exploit the
high degree of relational redundancy that is characteristic for infogeometric network measurements and communications.

Infogeometric enhancement algorithms also provide the following capabilities:

- Enhanced tracking in multipath and clutter - permits precision robotics tracking even when operating indoors.
- Enhanced near/far interference reduction - permits shared-spectrum operations in potentially large user networks (i.e., hundreds to thousands).

Table 3.1: Raw data measurement resolution and accuracy [Everett, 1995].

| Parameter | Resolution | Biasing |
| :--- | ---: | ---: |
| Range | 1 | 5 m |
|  | 3.3 | 16.4 ft |
| Bearing (Az, El) | 2 | $2^{\circ}$ |
| Orientation (Az) | 2 | $2^{\circ}$ |

Table 3.2: Enhanced tracking resolution and accuracies obtained through sensor data fusion [Everett, 1995].

| Parameter | Resolutio <br> n | Biasing |
| :--- | ---: | :--- |
| Range | $0.1-0.3$ | $0.1-0.3 \mathrm{~m}$ |
|  | $0.3-0.9$ | $0.3-0.9 \mathrm{ft}$ |
| Bearing | $0.5-1.0$ | $0.5-1.0^{\circ}$ |
| Orientation | $0.5-1.0$ | $0.5-1.0^{\circ}$ |

Operationally, mobile IG networks support precision tracking, communications, and command and control among a wide variety of potential user devices. A complete Infogeometric Positioning System is commercially available from [HTI], at a cost of $\$ 30,000$ or more (depending on the number of transmitters required). In conversation with HTI we learned that the system requires an almost clear "line of sight" between the transmitters and receivers. In indoor applications, the existence of walls or columns obstructing the path will dramatically reduce the detection range and may result in erroneous measurements, due to multi-path reflections.

### 3.2 Overview of Global Positioning Systems (GPSs)

The recent Navstar Global Positioning System (GPS) developed as a Joint Services Program by the Department of Defense uses a constellation of 24 satellites (including three spares) orbiting the earth every 12 hours at a height of about 10,900 nautical miles. Four satellites are located in each of six planes inclined 55 degrees with respect to the plane of the earth's equator [Getting, 1993]. The absolute three-dimensional location of any GPS receiver is determined through simple trilateration techniques based on time of flight for uniquely coded spread-spectrum radio signals transmitted by the satellites. Precisely measured signal propagation times are converted to pseudoranges representing the line-of-sight distances between the receiver and a number of reference satellites in known orbital positions. The measured distances have to be adjusted for receiver clock offset, as will be discussed later, hence the term pseudoranges. Knowing the exact distance from the ground receiver to three satellites theoretically allows for calculation of receiver latitude, longitude, and altitude.

Although conceptually very simple (see [Hurn, 1993]), this design philosophy introduces at least four obvious technical challenges:

- Time synchronization between individual satellites and GPS receivers.
- Precise real-time location of satellite position.
- Accurate measurement of signal propagation time.
- Sufficient signal-to-noise ratio for reliable operation in the presence of interference and possible jamming.
The first of these problems is addressed through the use of atomic clocks (relying on the vibration period of the cesium atom as a time reference) on each of the satellites to generate time ticks at a frequency of 10.23 MHz . Each satellite transmits a periodic pseudo-random code on two different frequencies (designated L1 and L2) in the internationally assigned navigational frequency band. The L 1 and L2 frequencies of 1575.42 and 1227.6 MHz are generated by multiplying the cesium-clock time ticks by 154 and 128, respectively. The individual satellite clocks are monitored by dedicated ground tracking stations operated by the Air Force, and continuously advised of their measured offsets from the ground master station clock. High precision in this regard is critical since electromagnetic radiation propagates at the speed of light, roughly 0.3 meters ( 1 ft ) per nanosecond.

To establish the exact time required for signal propagation, an identical pseudocode sequence is generated in the GPS receiver on the ground and compared to the received code from the satellite. The locally generated code is shifted in time during this comparison process until maximum correlation is observed, at which point the induced delay represents the time of arrival as measured by the receiver's clock. The problem then becomes establishing the relationship between the atomic clock on the satellite and the inexpensive quartz-crystal clock employed in the GPS receiver. This $\Delta T$ is found by measuring the range to a fourth satellite, resulting in four independent trilateration equations with four unknowns. Details of the mathematics involved are presented by Langley [1991].

The precise real-time location of satellite position is determined by a number of widely distributed tracking and telemetry stations at surveyed locations around the world. Referring to Figure 3.4, all measured and received data are forwarded to a master station for analysis and referenced to universal standard time. Change orders and signal-coding corrections are generated by the master station and then sent to the satellite control facilities for uploading [Getting, 1993]. In this fashion the satellites are continuously advised of their current position as perceived by the earth-based tracking stations, and encode this ephemeris information into their L1 and L2 transmissions to the GPS receivers. (Ephemeris is the space vehicle orbit characteristics, a set of numbers that precisely describe the vehicle's orbit when entered into a specific group of equations.)

In addition to its own timing offset and orbital information, each satellite transmits data on all other satellites in the constellation to enable any ground receiver to build up an almanac after a "cold start." Diagnostic information with respect to the status of certain onboard systems and expected range-measurement accuracy is also included. This collective "housekeeping" message is superimposed on the pseudo-random code modulation at a very low ( $50 \mathrm{bits} / \mathrm{s}$ ) data rate, and requires 12.5 minutes for complete downloading [Ellowitz, 1992]. Timing offset and ephemeris information is repeated at 30 second intervals during this procedure to facilitate initial pseudorange measurements.

To further complicate matters, the sheer length of the unique pseudocode segment assigned to each individual Navstar Satellite (i.e., around 6.2 trillion bits) for repetitive transmission can potentially cause initial synchronization by the ground receiver to take considerable time. For this and other reasons, each satellite broadcasts two different non-interfering pseudocodes. The first of these is called the coarse acquisition, or C/A code, and is transmitted on the L1 frequency to assist in acquisition. There are 1023 different C/A codes, each having 1023 chips (code bits) repeated 1000 times a second [Getting, 1993] for an effective chip rate of 1.023 MHz (i.e., one-tenth the cesium clock rate). While the C/A code alone can be employed by civilian users to obtain a fix, the resultant


Figure 3.4: The Navstar Global Positioning System consists of three fundamental segments: Space, Control, and User. (Adapted from [Getting, 1993].)
positional accuracy is understandably somewhat degraded. The Y code (formerly the precision or P code prior to encryption on January 1st, 1994) is transmitted on both the L1 and L2 frequencies and scrambled for reception by authorized military users only with appropriate cryptographic keys and equipment. This encryption also ensures bona fide recipients cannot be "spoofed" (i.e., will not inadvertently track false GPS-like signals transmitted by unfriendly forces).

Another major difference between the Y and $\mathrm{C} / \mathrm{A}$ code is the length of the code segment. While the C/A code is 1023 bits long and repeats every millisecond, the Y code is $2.35 \times 10^{14}$ bits long and requires 266 days to complete [Ellowitz, 1992]. Each satellite uses a one-week segment of this total code sequence; there are thus 37 unique Y codes (for up to 37 satellites) each consisting of $6.18 \times 10^{12}$ code bits set to repeat at midnight on Saturday of each week. The higher chip rate of 10.23 MHz (equal to the cesium clock rate) in the precision Y code results in a chip wavelength of 30 meters for the Y code as compared to 300 meters for the C/A code [Ellowitz, 1992], and thus facilitates more precise time-of-arrival measurement for military purposes.

Brown and Hwang [1992] discuss a number of potential pseudorange error sources as summarized below in Table 3.3. Positional uncertainties related to the reference satellites are clearly a factor, introducing as much as 3 meters ( 9.8 ft ) standard deviation in pseudo-range measurement accuracy. As the radiated signal propagates downward toward the earth, atmospheric refraction and multi-path reflections (i.e., from clouds, land masses, water surfaces) can increase the perceived time of flight beyond that associated with the optimal straight-line path (Figure 3.5).

Additional errors can be attributed to group delay uncertainties introduced by the processing and passage of the signal through the satellite electronics. Receiver noise and resolution must also be
taken into account. Motazed [1993] reports fairly significant differences of 0.02 to 0.07 arc minutes in calculated latitudes and longitudes for two identical C/A-code receivers placed side by side. And finally, the particular dynamics of the mobile vehicle that hosts the GPS receiver plays a noteworthy role, in that best-case conditions are associated with a static platform, and any substantial velocity and acceleration will adversely affect the solution.

For commercial applications using the C/A code, small errors in timing and satellite position have been deliberately introduced by the master station to prevent a hostile nation from using GPS in support of precision weapons delivery. This intentional degradation in positional accuracy to around 100 meters ( 328 ft ) best case

Table 3.3: Summary of potential error sources for measured pseudoranges [Brown and Hwang, 1992].

| Error Source | $\begin{array}{c}\text { Standard } \\ {[\mathrm{m}]}\end{array}$ |  |
| :--- | :---: | :---: |
| Satellite position | 3 | 29 |
| $[\mathrm{ft}]$ |  |  |$]$| Deviation |  |  |
| :--- | :---: | :---: |
| Ionospheric refraction | 5 | 16.4 |
| Tropospheric refraction | 2 | 6.6 |
| Multipath reflection | 5 | 16.4 |
| Selective availability | 30 | 98.4 | and 200 meters ( 656 ft ) typical spherical error probable (SEP) is termed selective availability [Gothard, 1993]. Selective availability has been on continuously (with a few exceptions) since the end of Operation Desert Storm. It was turned off during the war from August 1990 until July 1991 to improve the accuracy of commercial hand-held GPS receivers used by coalition ground forces.

There are two aspects of selective availability: epsilon and dither. Epsilon is intentional error in the navigation message regarding the location (ephemeris) of the satellite. Dither is error in the timing source (carrier frequency) that creates uncertainty in velocity measurements (Doppler). Some GPS receivers (for example, the Trimble ENSIGN) employ running-average filtering to statistically reduce the epsilon error over time to a reported value of 15 meters SEP [Wormley, 1994].

At another occasion (October 1992) SA was also turned off for a brief period while the Air Force was conducting tests. Byrne [1993] conducted tests at that time to compare the accuracy of GPS with SA turned on and off. The static measurements of the GPS error as a function of time shown in Figure 3.6 were taken before the October 1992 test, i.e., with SA "on" (note the slowly varying error in Figure 3.6, which is caused by SA). By contrast, Figure 3.7 shows measurements from the October 1992 period when SA was briefly "off."


Figure 3.5: Contributing factors to pseudorange measurement errors: a. atmospheric refraction; b. multi-path reflections [Everett, 1995].


Figure 3.6: Typical GPS static position error with SA "On." (Courtesy of [Byrne, 1993].)


Figure 3.7: Typical GPS static position error with SA "Off". (Courtesy of Byrne [1993]).

All of the error sources listed in Table 3.3 are further influenced by the particular geometry of the four reference satellites at time of sighting. Ignoring time synchronization needs for the moment (i.e., so only three satellites are required), the most accurate three-dimensional trilater-ation solutions will result when the bearing or sight lines extending from the receiver to the respective satellites are mutually orthogonal. If the satellites are spaced close together in a tight cluster or otherwise arranged in a more or less collinear fashion with respect to the receiver as shown in Figure 3.8, the desired orthogonality is lost and the solution degrades accordingly.

Terms used to describe the strength of the position fix based on the geometry include: Dilution of Precision (DOP), Horizontal Dilution of Precision (HDOP), Geometric Dilution of Precision (GDOP), Position Dilution of Precision (PDOP), Time Dilution of Precision (TDOP), and Vertical Dilution of Precision (VDOP). The various DOPs are error multipliers that indicate the accuracy of a particular type of position fix based on a certain pseudo-range error. For instance, if the pseudorange measurements are accurate to 10 meters ( 33 ft ) and the HDOP is equal to 3.5 , the horizontal position accuracy would be $10 \times 3.5=35$ meters ( 100 ft ). A PDOP of 2 or 3 is fairly good, while a PDOP of 10 is not so good. Certain geometries can cause the DOP to become very large (infinite). Two useful DOP identities are shown in Equations (3.2) and (3.3).
$\mathrm{PDOP}^{2}=\mathrm{VDOP}^{2}+\mathrm{HDOP}^{2}$

Kihara and Okada [1984] show that the minimum achievable (best-case) value for GDOP is 1.5811 . This optimal constellation occurs when the four required GPS satellites are symmetrically located with an angle of 109.47 degrees between adjacent bearing lines as shown in

Acronyms used in this section DOP dilution of precision GDOP geometric dilution of precision
HDOP horizontal dilution of precision PDOP position dilution of precision TDOP Time dilution of precision VDOP vertical dilution of precision SA selective availability Figure 3.9.

With the exception of multi-path effects, all of the error sources listed in Table 3.3 above can be essentially eliminated through use of a practice known as differential GPS (DGPS). The concept is based on the premise that a second GPS receiver in fairly close proximity (i.e., within $10 \mathrm{~km}-6.2 \mathrm{mi}$ ) to the first will experience basically the same error effects when viewing the same reference satellites. If this second receiver is fixed at a precisely


Figure 3.8: Worst-case geometric dilution of precision (GDOP) errors occur when the receiver and satellites approach a collinear configuration as shown [Everett, 1995].
surveyed location, its calculated solution can be compared to the known position to generate a composite error vector representative of prevailing conditions in that immediate locale. This differential correction can then be passed to the first receiver to null out the unwanted effects, effectively reducing position error for commercial systems to well under 10 meters.

The fixed DGPS reference station transmits these correction signals every two to four minutes to any differential-capable receiver within range. Many commercial GPS receivers are available with differential capability, and most now follow the RTCM-104 standard developed by the Radio Technical Commission for Maritime Services to promote interoperability. Prices for DGPS-capable mobile receivers run about $\$ 2 \mathrm{~K}$, while the reference stations cost somewhere between $\$ 10 \mathrm{~K}$ and $\$ 20 \mathrm{~K}$. Magnavox is working with CUE Network Corporation to market a nationwide network to pass differential corrections over an FM link to paid subscribers [GPS Report, 1992].

Typical DGPS accuracies are around 4 to 6 meters (13 to 20 ft ) SEP, with better performance seen as the distance between the mobile receivers and the fixed reference station is decreased. For example, the Coast Guard is in the process of implementing differential GPS in all major U.S. harbors, with an expected accuracy of around 1 meter ( 3.3 ft ) SEP [Getting, 1993]. A differential GPS system already in operation at O'Hare International Airport in Chicago has demonstrated that aircraft and service vehicles can be located to 1 meter ( 3.3 ft ). Surveyors use differential GPS to achieve centimeter accuracy, but this practice requires significant postprocessing of the collected data [Byrne, 1993].

An interesting variant of conventional DGPS is reported by Motazed [1993] in conjunction with the Non-Line-of-Sight Leader/Follower (NLOSLF) program underway at RedZone Robotics, Inc., Pittsburgh, PA. The NLOSLF operational scenario involves a number of vehicles in a convoy configuration that autonomously follow a lead vehicle driven by a human operator, both on-road and off-road at varying speeds and separation distances. A technique to which Motazed refers as intermittent stationary base differential GPS is used to provide global referencing for purposes of bounding the errors of a sophisticated Kalman-filter-based GPS/INS position estimation system.

Under this innovative concept, the lead and final vehicle in the convoy alternate as fixedreference differential GPS base stations. As the convoy moves out from a known location, the final vehicle remains behind to provide differential corrections to the GPS receivers in the rest of the vehicles. After traversing a predetermined distance in this fashion, the convoy is halted and the lead vehicle assumes the role of a differential reference station, providing enhanced accuracy to the trailing vehicle as it catches up to the pack. During this time, the lead vehicle takes advantage of onsite dwell to further improve the accuracy of its own fix. Once the last vehicle joins up with the rest, the base-station roles are reversed again, and the convoy resumes transit in "inchworm" fashion along its intended route. Disadvantages to this approach include the need for intermittent stops and the accumulating ambiguity in actual location of the appointed reference station.

Recall the Y-code chip rate is directly equal to the satellite cesium clock rate, or 10.23 MHz . Since the L 1 carrier frequency of 1575.42 MHz is generated by multiplying the clock output by 154 , there are consequently 154 carrier cycles for every Y-code chip. This implies even higher measurement precision is possible if the time of arrival is somehow referenced to the carrier instead of the pseudocode itself. Such codeless interferometric differential GPS schemes measure the phase of the L1 and L2 carrier frequencies to achieve centimeter accuracies, but they must start at a known geodetic location and typically require long dwell times. The Army's Engineer Topographic Laboratories (ETL) is in the process of developing a carrier-phase-differential system of this type that is expected to provide 1 to 3 centimeters ( 0.4 to 1.2 in ) accuracy at a $60-\mathrm{Hz}$ rate when finished sometime in 1996 [McPherson, 1991].

A reasonable extraction from the open literature of achievable position accuracies for the various GPS configurations is presented in Table 3.4. The Y code has dual-frequency estimation for atmospheric refraction and no S/A error component, so accuracies are better than stand-alone singlefrequency C/A systems. Commercial DGPS accuracy, however, exceeds stand-alone military Y-code accuracy, particularly for small-area applications such as airports. Differential Y code is currently under consideration and may involve the use of a satellite to disseminate the corrections over a wide area.

Table 3.4: Summary of achievable position accuracies for various implementations of GPS.

| GPS Implementation Method | Position Accuracy |
| :--- | :--- |
| C/A-code stand alone | 100 m SEP |
|  | $(328 \mathrm{ft})$ |
| Y-code stand alone | 16 m SEP |
|  | $(52 \mathrm{ft})$ |
| Differential (C/A-code) | 3 m SEP |
|  | $(10 \mathrm{ft})$ |
| Differential (Y-code) | unknown (TBD) |
| Phase differential (codeless) | 1 cm SEP |
|  | $(0.4 \mathrm{in})$ |

A typical non-differential GPS was tested by Cooper and Durrant-White [1994] and yielded an accumulated position error of over 40 meters ( 131 ft ) after extensive filtering.

Systems likely to provide the best accuracy are those that combine GPS with Inertial Navigation Systems (INS), because the INS position drift is bounded by GPS corrections [Motazed, 1993]. Similarly, the combination of GPS with odometry and a compass was proposed by Byrne [1993].

In summary, the fundamental problems associated with using GPS for mobile robot navigation are as follows:

- Periodic signal blockage due to foliage and hilly terrain.
- Multi-path interference.
- Insufficient position accuracy for primary (stand-alone) navigation systems.

Arradondo-Perry [1992] provides a comprehensive listing of GPS receiver equipment, while Byrne [1993] presents a detailed evaluation of performance for five popular models. Parts of Byrne's performance evaluation has been adapted from the original report for inclusion in this survey as Section 3.3.

### 3.3 Evaluation of Five GPS Receivers by Byrne [1993]

In 1992 and 1993 Raymond H. Byrne at the Advanced Vehicle Development Department, Sandia National Laboratories, Albuquerque, New Mexico conducted a series of in-depth comparison tests with five different GPS receivers. His results were originally published in September 1993 as Sandia Report SAND93-0827 UC-515. With permission of the author we have reproduced and adapted parts of that report in this section.

### 3.3.1 Project Goals

The intent of Byrne's study was to compare the performance of a particular two-channel, sequencing GPS receiver (a 10 year old, outdated Magnavox 6400) to that of newer five- and sixchannel parallel receivers. The parallel channel receivers used in this study were selected based upon availability, cost, size, and receiver specifications.

The receivers tested are listed in Table 3.5. The "original equipment manufacturer" (OEM) receivers are single board GPS devices that are meant to be integrated into a system or product. The Trimble and Magnavox 6400 receivers are "integrated" commercial products.

Table 3.5: GPS receivers tested. (Courtesy of Byrne [1993]).

| Receiver | Description |
| :--- | :--- |
| Magnavox 6400 (10-year old <br> system, outdated) | 2-channel, sequencing receiver, receiver in <br> current system, integrated system |
| Magellan OEM GPS Module | 5-channel GPS receiver, OEM type |
| Magnavox GPS Engine | 6-channel GPS receiver, OEM type |
| Rockwell NavCore V | 5-channel GPS receiver, OEM type |
| Trimble Placer | 6-channel receiver, Integrated System |

The performance of the current GPS receiver was tested along with four commercially available receivers. The experiments included static as well as dynamic testing. The results of these tests are presented in the following section.

### 3.3.2 Test Methodology

Many parameters may be measured when comparing GPS receivers. Section 3.3.2.1 discusses the parameters that were chosen to compare the performance of Sandia's old Magnavox 6400 GPS receiver to newer commercial off the-shelf units. Section 3.3.2.2 describes the test fixture hardware developed to gather GPS data from the five different receivers, and the post processing of the gathered data is discussed in Section 3.3.2.3.

### 3.3.2.1 Parameters tested

In the experiments performed at Sandia National Laboratories testing focused on receiver sensitivity, static accuracy, dynamic accuracy, number of satellites tracked, and time-to-first-fix. The tests aimed at evaluating the five different GPS receivers in both static and dynamic environments. This section discusses the parameters tested and the rationalization for choosing these parameters.

For many navigation applications time-to-first-fix is an important parameter. The older Magnavox 6400 receiver can take up to 30 minutes to initialize and lock onto the satellite signals before it starts navigating. However, all of the newer receivers advertise fast position fixes, usually under one minute, if the receiver knows its position to within several hundred miles. This is often referred to as a "warm start." The difference between a 30 -second first fix and a 2 -minute first fix is not that important for most applications. However, 1 to 2 minutes is a great improvement over 30 minutes. Although this parameter was not explicitly measured, attention was paid to time-to-first-fix to confirm that the newer receivers were meeting the quoted specification.

The number of satellites tracked and receiver sensitivity are also important parameters. The more satellites tracked, the less likely an obstruction of one or more satellites will result in a loss of navigation. Also, a more sensitive receiver is less likely to be affected by foliage and other obstructions that reduce signal strengths. The receiver sensitivity is affected by the type of antenna used and the type of cabling. Some antennas have higher gains than others, different cables have different attenuation characteristics, and longer cables cause greater signal attenuation. The navigation mode, two-dimensional (2D-mode) or three-dimensional (3D-mode), is affected by the number of satellites visible. Provided that the geometry results in an acceptable DOP, a minimum of four satellites are necessary for three-dimensional navigation. Additional satellites may be used to achieve a more robust position fix. If four satellites are in view, but the DOP is higher than a certain threshold, many receivers will switch to two-dimensional navigation.

Ideally, measuring the signal-to-noise ratio in the receiver and the number of satellites being tracked would yield the most insight into receiver performance. However, this information is usually buried in several different data packets for any given receiver. For some receivers, this information is not always available (the Trimble Placer does not output signal-to-noise ratio or the number of satellites tracked for example). Therefore, a compromise was made and packets were requested that contained the position fix as well as the navigation mode or number of satellites tracked. Usually this data was contained in the same data packet. This reduced the amount of data stored and simplified the data analysis. The information gathered from each receiver is listed in Table 3.6.

Differences in navigation modes can be caused by several factors; these include differences in number of satellites being tracked, differences in the DOP value that cause a switch from 3D-mode to 2D-mode navigation, and differences in satellite mask angles and receiver/antenna sensitivity. The DOP settings and mask angles are known for each receiver, so the navigation mode data will allow comparing the number of satellites tracked and receiver/antenna sensitivity as one performance criterion. Although the navigation mode data lumps several factors together, it does give a comparison of overall receiver/antenna performance.

As mentioned in the previous section, the antenna and cable choice affects the performance of the GPS receiver. The antennas used for the GPS testing were supplied with the receiver or OEM evaluation kit, The cabling was also supplied with the exception of the Magnavox GPS Engine. Therefore, the performance of the antenna and cabling was lumped together with the overall GPS system because each manufacturer recommends (or provides) antennas and cabling.

Table 3.6: Summary of data analyzed (Courtesy of [Byrne, 1993].)

| Receiver | Data Gathered |
| :--- | :--- |
| Magellan | Latitude, longitude. <br> Number of satellites used - implies navigation mode (none, 2-D, or 3-D). |
| Magnavox GPS Engine | Latitude, longitude. <br> Navigation Mode (none, 2-D, or 3-D). |
| Rockwell NavCore V | Latitude, longitude, navigation mode (none, 2-D, or 3-D). <br> Number of satellites tracked also available from raw data. |
| Magnavox 6400 | Latitude, longitude <br> Number of satellites tracked. |
| Trimble Placer | Latitude, longitude. <br> Navigation Mode (none, 2-D, or 3-D). |

Other performance factors include the amount of filtering in a GPS receiver. Excessive filtering reduces the amount of variance in the position and velocity data, but also slows the response of the receiver. Excessive filtering will cause a receiver to output incorrect positions when starting, stopping, or turning sharply. In applications where the GPS data is processed off board and needs to be transmitted via RF-link to a central computer, this type of error is not very important because the delay introduced by the communication link will probably be much greater than the delay introduced by filtering in the receiver.

Parameters that were not analyzed in the Sandia experiments are velocity and heading accuracy, because in Sandia's application (and many other typical mobile robot navigation tasks) accurate velocity information was already available from odometry. Heading information that would be required for dead reckoning is not needed while GPS is functional.

Another easy-to-measure performance criterion is static position accuracy. This parameter was measured by placing the GPS receivers at a surveyed location and taking data for approximately 24 hours. Although in typical application the receivers are moving most of the time, the static accuracy does give a good idea of the receivers' position accuracy capabilities. The parameters measured and the performance insights gained from these measurements are summarized in Table 3.7.

In summary, the GPS testing performed for this project consisted of storing position and navigation mode data from five different GPS receivers for both static and dynamic tests. The static testing provides information about the static position accuracy as well as the sensitivity of the receiver and antenna if DOP switching is taken into account. The dynamic testing mostly provides information about the receiver/antenna sensitivity and the receiver's ability to recover from temporary obstructions (taking into account DOP switching). The dynamic testing also provides some qualitative information about position accuracy by comparing plots of the data points from the various receivers.

Table 3.7: Summary of parameters measured and performance areas evaluated. (Courtesy of [Byrne, 1993].)

| Parameter measured | Performance evaluated by that parameter |
| :--- | :--- |
| Time-to-first-fix | How quickly a receiver starts navigating. Not explicitly measured, but <br> qualitatively considered. |
| Static position accuracy | Static accuracy and insight into overall accuracy. |
| Static navigation mode- <br> Number of satellites tracked | Taking into account DOP switching, gives insight into receiver/antenna <br> sensitivity. |
| Dynamic position plots | Some accuracy information is obtained by comparing different data plots <br> taken while driving down the same section of road. Most of this analysis is <br> qualitative though because there is no ground-truth data for comparison. |
| Dynamic navigation mode | Taking DOP switching into account gives insight into the sensitivity of the <br> receiver/antenna and the rate with which the receiver recovers from <br> obstructions. |

### 3.3.2.2 Test hardware

The GPS receivers tested use a serial interface for communicating position information. The Magnavox 6400 receiver communicates using RS-422 serial communications, while the other four receivers use the RS-232 communications standard. The RS-422 and RS-232 standards for data transmission are compared in Table 3.8.

For the short distances involved in transmitting GPS data from the receiver to a computer, the type of serial communications is not important. In fact, even though RS-232 communications are inferior in some ways to RS422, RS-232 is easier to work with because it is a more common standard (especially for PC-type computers).

A block diagram of the overall GPS test system is shown in Figure 3.10. Figure 3.10 depicts the system used for dynamic testing where power was supplied from a 12 -Volt battery. For the static testing, AC power was available with an extension cord. Therefore, the computer supply was connected directly to AC, while the +12 Volts for the GPS receivers was generated using an AC-DC power supply for the static test.

The GPS test fixture was set up in a Chevrolet van with an extended rear for additional room. The GPS antennas were mounted on aluminum plates that where attached to the van with magnets. The Rockwell antenna came with a magnetic mount so it was attached directly to the roof. The five antennas were within one meter of each other near the rear of the van and mounted at the same height so that no antenna obstructed the others.


Figure 3.10: Block diagram of the GPS test fixture. (Courtesy of [Byrne, 1993].)
For the dynamic testing, power was supplied from a 60 Amp -Hour lead acid battery. The battery was used to power the AC-DC inverter as well as the five receivers. The van's electrical system was tried at first, but noise caused the computer to lock up occasionally. Using an isolated battery solved this problem. An AC-powered computer monitor was used for the static testing because AC power was available. For the dynamic testing, the low power LCD display was used.

### 3.3.2.3 Data post processing

The GPS data was stored in raw form and post processed to extract position and navigation data. This was done so that the raw data could be analyzed again if there were any questions with the results. Also, storing the data as it came in from the serial ports required less computational effort and reduced the chance of overloading the data acquisition computer. This section describes the software used to post process the data.

Table 3.9 shows the minimum resolution (I..e, the smallest change in measurement the unit can output) of the different GPS receivers. Note, however, that the resolution of all tested receivers is still orders of magnitude smaller than the typical position error of up to 100 meters. Therefore, this parameter will not be an issue in the data analysis.

Table 3.8: Comparison of RS-232 and RS-422 serial communications. (Courtesy of [Byrne, 1993].)

| RS-232 Communications | RS-422 Communications |
| :--- | :--- |
| Single-ended data transmission | Differential data transmissions |
| Relatively slow data rates (usually < 20 kbs ), <br> short distances up to 50 feet, most widely used. | Very high data rates (up to 10 Mbs ), long distances <br> (up to 4000 feet at 100 Kbs ), good noise immunity. |

Once the raw data was converted to files with latitude, longitude, and navigation mode in columnar form, the data was prepared for analysis. Data manipulations included obtaining the position error from a surveyed location, generating histograms of position error and navigation mode, and plotting dynamic position data. The mean and variance of the position errors were also obtained. Degrees of latitude and longitude were converted to meters using the conversion factors listed below.

Latitude Conversion Factor $\quad 11.0988 \times 10^{4} \mathrm{~m} /{ }^{\circ}$ latitude
Longitude Conversion Factor $\quad 9.126 \times 10^{4} \mathrm{~m} /{ }^{\circ}$ longitude

### 3.3.3 Test Results

Sections 3.3.3.1 and 3.3.3.2 discuss the test results for the static and dynamic tests, respectively, and a summary of these results is given in Section 3.3.3.3. The results of the static and dynamic tests provide different information about the overall performance of the GPS receivers. The static test compares the accuracy of the different receivers as they navigate at a surveyed location. The static test also provides some information about the receiver/antenna sensitivity by comparing navigation modes (3D-mode, 2D-mode, or not navigating) of the different receivers over the same time period. Differences in navigation mode may be caused by several factors. One is that the receiver/antenna operating in a plane on ground level may not be able to track a satellite close to the horizon. This reflects receiver/antenna sensitivity. Another reason is that different receivers have different DOP limits that cause them to switch to two dimensional navigation when four satellites are in view but the DOP becomes too high. This merely reflects the designer's preference in setting DOP switching masks that are somewhat arbitrary.

Dynamic testing was used to compare relative receiver/antenna sensitivity and to determine the amount of time during which navigation was not possible because of obstructions. By driving over different types of terrain, ranging from normal city driving to deep canyons, the relative sensitivity of the different receivers was observed. The navigation mode (3D-mode, 2D-mode, or not navigating) was used to compare the relative performance of the receivers. In addition, plots of the data taken give some insight into the accuracy by qualitatively observing the scatter of the data.

Table 3.9: Accuracy of receiver data formats. (Courtesy of [Byrne, 1993].)

| Receiver | Data format resolution <br> (degrees) | Minimum resolution <br> (meters) |
| :--- | ---: | ---: |
| Magellan | $10^{-7}$ | 0.011 |
| Magnavox GPS Engine | $1.7 \times 10^{-6}$ | 0.19 |
| Rockwell NavCore V | $5.73 \times 10^{-10}$ | $6.36 \times 10^{-5}$ |
| Magnavox 6400 | $10^{-8} 5.73 \times 10^{-7}$ | $6.36 \times 10^{-2}$ |
| Trimble Placer | $10^{-5}$ | 1.11 |

### 3.3.3.1 Static test results

Static testing was conducted at a surveyed location at Sandia National Laboratories' Robotic Vehicle Range (RVR). The position of the surveyed location is described in Table 3.10.

Table 3.10: Location of the surveyed point at the Sandia Robotic Vehicle Range. (Courtesy of [Byrne, 1993].)

| Surveyed Latitude | Surveyed Longitude |
| :--- | :--- |
| $350227.71607($ deg min sec) | $1063116.14169($ deg min sec) |
| $35.0410322(\mathrm{deg})$ | $106.5211505(\mathrm{deg})$ |

The data for the results presented here was gathered on October 7 and 8, 1992, from 2:21 p.m. to 2:04 p.m. Although this is the only static data analyzed in this report, a significant amount of additional data was gathered when all of the receivers were not functioning simultaneously. This previously gathered data supported the trends found in the October 7 and 8 test.The plots of the static position error for each receiver are shown in Figure 3.11. A summary of the mean and standard deviation ( $\sigma$ ) of the position error for the different receivers appears in Table 3.11.

Table 3.11: Summary of the static position error mean and variance for different receivers. (Courtesy of [Byrne, 1993].)

| Receiver | Mean position error | Position error standard <br> deviation |  |  |
| :--- | :---: | ---: | ---: | ---: |
|  | (meters) | (feet) | (meters) | (feet) |
| Magellan | 33.48 | 110 | 23.17 | 76 |
| Magnavox GPS Engine | 22.00 | 72 | 16.06 | 53 |
| Rockwell NavCore V | 30.09 | 99 | 20.27 | 67 |
| Magnavox 6400 | 28.01 | 92 | 19.76 | 65 |
| Trimble Placer | 29.97 | 98 | 23.58 | 77 |

It is evident from Table 3.11 that the Magnavox GPS Engine was noticeably more accurate when comparing static position error. The Magellan, Rockwell, Magnavox 6400, and Trimble Placer all exhibit comparable, but larger, average position errors. This trend was also observed when SA was turned off. However, a functioning Rockwell receiver was not available for this test so the data will not be presented. It is interesting to note that the Magnavox 6400 unit compares well with the newer receivers when looking at static accuracy. This is expected: since the receiver only has two channels, it will take longer to reacquire satellites after blockages; one can also expect greater difficulties with dynamic situations. However, in a static test, the weaknesses of a sequencing receiver are less noticeable.


The histogramic error distributions for the data taken during the static test are shown in Figure 3.12. One can see from Fig. 3.12 that the Magnavox GPS Engine has the most data points within 20 meters of the surveyed position. This corresponds with the smallest mean position error exhibited by the Magnavox receiver. The error distributions for the other four receivers are fairly similar. The Magnavox 6400 unit has slightly more data points in the 10 to 20 meter error bin, but otherwise there are no unique features. The Magnavox GPS Engine is the only receiver of the five tested that had a noticeably superior static position error distribution. Navigation mode data for the different receivers is summarized in Figure 3.13 for the static test.


Figure 3.12: Histogramic error distributions for the data taken during the static test, for all five tested GPS receivers. (Adapted from [Byrne, 1993].)

In order to analyze the data in Figure 3.13, one needs to take into account the DOP criterion for the different receivers. As mentioned previously, some receivers switch from 3D-mode navigation to 2D-mode navigation if four satellites are visible but the DOP is above a predetermined threshold. The DOP switching criterion for the different receivers are outlined in Table 3.12. As seen in Table 3.12, the different receivers use different DOP criteria. However, by taking advantage of Equations (3.1) and (3.2), the different DOP criteria can be compared.


Figure 3.13: Navigation mode data for the static test. (Adapted from [Byrne, 1993].)
Table 3.12 relates all of the different DOP criteria to the PDOP. Based on the information in Table 3.12, several comments can be made about the relative stringency of the various DOP criterions. First, the Magnavox GPS Engine VDOP criterion is much less stringent than the Magellan VDOP criterion (these two can be compared directly). The Magellan unit also incorporates hysteresis, which makes the criterion even more stringent. Comparing the Rockwell to the Trimble Placer, the Rockwell criterion is much less stringent. A TDOP of 10.2 would be required to make the two criteria equivalent. The Rockwell and Magnavox GPS Engine have the least stringent DOP requirements.

Taking into account the DOP criterions of the different receivers, the significant amount of twodimensional navigation exhibited by the Magellan receiver might be attributed to a more stringent DOP criterion. However, this did not improve the horizontal (latitude-longitude) position error. The Magnavox GPS Engine still exhibited the most accurate static position performance. The same can

Table 3.12: Summary of DOP - navigation mode switching criteria. (Courtesy of [Byrne, 1993].)

| Receiver | 2-D/3-D DOP criterion | PDOP equivalent |
| :--- | :--- | :--- |
| Magellan | If 4 satellites visible and VDOP $>7$, will <br> switch to 2-D navigation. <br> Enters 3-D navigation when VDOP $<5$. | $\mathrm{PDOP} \geq\left(\mathrm{HDOP}^{2}+7^{2}\right)^{1 / 2}$ |
| Magnavox GPS <br> Engine | If 4 satellites visible and VDOP $>10$, <br> switches to 2-D navigation. <br> If HDOP $>10$, suspends 2-D navigation | $\mathrm{PDOP} \leq\left(\mathrm{HDOP}^{2}+5^{2}\right)^{1 / 2}$ <br> $\mathrm{PDOP} \geq\left(\mathrm{HDOP}^{2}+10^{2}\right)^{1 / 2}$ |
| Rockwell NavCore V | If 4 satellites visible and GDOP $>13$, <br> switches to 2-D navigation. | $\mathrm{PDOP} \geq\left(13^{2}-\mathrm{TDOP}^{2}\right)^{1 / 2}$ |
| Magnavox 6400 | Data Not Available in MX 5400 manual <br> provided | $\mathrm{PDOP} \geq 8$ |
| Trimble Placer | If 4 satellites visible and PDOP $>8$, switches to 2-D <br> navigation. If PDOP $>12$, receiver stops navigating. |  |

be said for the Trimble Placer unit. Although is has a stricter DOP requirement than the Magnavox Engine, its position location accuracy was not superior. The static navigation mode results don't conclusively show that any receiver has superior sensitivity. However, the static position error results do show that the Magnavox GPS Engine is clearly more accurate than the other receivers tested. The superior accuracy of the Magnavox receiver in the static tests might be attributed to more filtering in the receiver. It should also be noted that the Magnavox 6400 unit was the only receiver that did not navigate for some time period during the static test.

### 3.3.3.2 Dynamic test results

The dynamic test data was obtained by driving the instrumented van over different types of terrain. The various routes were chosen so that the GPS receivers would be subjected to a wide variety of obstructions. These include buildings, underpasses, signs, and foliage for the city driving. Rock cliffs and foliage were typical for the mountain and canyon driving. Large trucks, underpasses, highway signs, buildings, foliage, as well as small canyons were found on the interstate and rural highway driving routes.

The results of the dynamic testing are presented in Figures 3.14 through 3.18. The dynamic test results as well as a discussion of the results appear on the following pages.

Several noticeable differences exist between Figure 3.13 (static navigation mode) and Figure 3.14. The Magnavox 6400 unit is not navigating a significant portion of the time. This is because sequencing receivers do not perform as well in dynamic environments with periodic obstructions. The Magellan GPS receiver also navigated in 2D-mode a larger percentage of the time compared with the other receivers. The Rockwell unit was able to navigate in 3D-mode the largest percentage of the time. Although this is also a result of the Rockwell DOP setting discussed in the previous section, it does seem to indicate that the Rockwell receiver might have slightly better sensitivity (Rockwell claims this is one of the receiver's selling points). The Magnavox GPS Engine also did not navigate a small percentage of the time. This can be attributed to the small period of time when the receiver was obstructed and the other receivers (which also were obstructed) might not have been outputting data (caused by asynchronous sampling).

The Mountain Driving Test actually yielded less obstructions than the City Driving Test. This might be a result of better satellite geometries during the test period. However, the Magnavox 6400 unit once again did not navigate for a significant portion of the time. The Magellan receiver navigated in 2D-mode a significant portion of the time, but this can be attributed to some degree to the stricter DOP limits. The performance of the Rockwell NavCore V, Trimble Placer, and Magnavox GPS Engine are comparable.


Figure 3.14: Summary of City Driving Results. (Adapted from [Byrne, 1993]).


Figure 3.15: Summary of mountain driving results. (Adapted from [Byrne, 1993]).


Figure 3.16: Summary of Canyon Driving Results. (Adapted from [Byrne, 1993]).


Figure 3.17: Summary of Interstate Highway Results. (Adapted from [Byrne, 1993]).


Figure 3.18. Summary of Rural Highway Results. (Adapted from [Byrne, 1993]).

The Canyon Driving Test exposed the GPS receivers to the most obstructions. The steep canyon walls and abundant foliage stopped the current receiver from navigating over 30 percent of the time. The Magnavox GPS Engine and Rockwell receiver were also not navigating a small percentage of the time. This particular test clearly shows the superiority of the newer receivers over the older sequencing receiver. Because the newer receivers are able to track extra satellites and recover more quickly from obstructions, they are better suited for operation in dynamic environments with periodic obstructions. The Trimble Placer and Rockwell receiver performed the best in this particular test, followed closely by the Magnavox GPS Engine.

During the Interstate Highway Driving tests, the Magnavox 6400 unit did not navigate over 20 percent of the time. This is consistent with the sometimes poor performance exhibited by the current navigation system. The other newer receivers did quite well, with the Trimble Placer, Magnavox GPS Engine, and Rockwell NavCore V exhibiting similar performance. Once again, the

Magellan unit navigated in 2D-mode a significant portion of the time. This can probably be attributed to the stricter DOP limits.

During the Rural Highway Driving test the Magnavox 6400 unit once again did not navigate a significant portion of the time. All of the newer receivers had similar performance results. The Magellan receiver navigated in 2D-mode considerably less in this test compared to the other dynamic tests.

### 3.3.3.3 Summary of test results

Both static and dynamic tests were used to compare the performance of the five different GPS receivers. The static test results showed that the Magnavox GPS Engine was the most accurate (for static situations). The other four receivers were slightly less accurate and exhibited similar static position error performance. The static navigation mode results did not differentiate the sensitivity of the various receivers significantly. The Magellan unit navigated in 2D-mode much more frequently than the other receivers, but some of this can be attributed to stricter DOP limits. However, the stricter DOP limits of the Magellan receiver and Trimble Placer did not yield better static position accuracies. All four of the newer GPS receivers obtained a first fix under one minute, which verifies the time to first-fix specifications stated by the manufacturers.

The dynamic tests were used to differentiate receiver sensitivity and the ability to recover quickly from periodic obstructions. As expected, the Magnavox 6400 unit did not perform very well in the dynamic testing. The Magnavox 6400 was unable to navigate for some period of each dynamic test. This was most noticeable in the Canyon route, where the receiver did not navigate over 30 percent of the time. The newer receivers performed much better in the dynamic testing, navigating almost all of the time. The Magnavox GPS Engine, Rockwell NavCore V, and Trimble Placer exhibited comparable receiver/antenna sensitivity during the dynamic testing based on the navigation mode data. The Magellan unit navigated in 2D-mode significantly more than the other receivers in the dynamic tests. Most of this can probably be attributed to a more stringent DOP requirement. It should also be noted that the Magellan receiver was the only receiver to navigate in 2D-mode or 3Dmode 100 percent of the time in all of the dynamic tests.

Overall, the four newer receivers performed significantly better than the Magnavox 6400 unit in the dynamic tests. In the static test, all of the receivers performed satisfactorily, but the Magnavox GPS Engine exhibited the most accurate position estimation. Recommendations on choosing a GPS receiver are outlined in the next section.

### 3.3.4 Recommendations

In order to discuss some of the integration issues involved with GPS receivers, a list of the problems encountered with the receivers tested is outlined in Section 3.3.4.1. The problems encountered with the Magnavox 6400 unit (there were several) are not listed because the Magnavox 6400 unit is not comparable to the newer receivers in performance.

Based on the problems experienced testing the GPS receivers as well as the requirements of the current application, a list of critical issues is outlined in Section 3.3.4.2.

One critical integration issue not mentioned in Section 3.3.4.2 is price. Almost any level of performance can be purchased, but at a significantly increased cost. This issue will be addressed further in the next section. Overall, the Magellan OEM Module, the Magnavox GPS Engine, Rockwell NavCore V, and Trimble Placer are good receivers. The Magnavox GPS Engine exhibited superior static position accuracy. During dynamic testing, all of the receivers were able to navigate
a large percentage of the time, even in hilly wooded terrain. Based on the experimental results, other integration issues such as price, software flexibility, technical support, size, power, and differential capability are probably the most important factors to consider when choosing a GPS receiver.

### 3.3.4.1 Summary of problems encountered with the tested GPS receivers

## Magellan OEM Module

- No problems, unit functioned correctly out of the box. However, the current drain on the battery for the battery backed RAM seemed high. A 1-AmpHour 3.6-Volt Lithium battery only lasted a few months.
- The binary position packet was used because of the increased position resolution. Sometimes the receiver outputs a garbage binary packet (about I percent of the time).


## Magnavox GPS Engine

- The first unit received was a pre-production unit. It had a difficult time tracking satellites. On one occasion it took over 24 hours to obtain a first fix. This receiver was returned to Magnavox. Magnavox claimed that upgrading the software fixed the problem. However, the EEPROM failed when trying to load the oscillator parameters. A new production board was shipped and it functioned flawlessly out of the box.
- The RF connector for the Magnavox GPS Engine was also difficult to obtain. The suppliers recommended in the back of the GPS Engine Integration Guide have large minimum orders. A sample connector was finally requested. It never arrived and a second sample had to be requested.


## Rockwell NavCore V

- The first Rockwell receiver functioned for a while, and then began outputting garbage at 600 baud ( 9600 baud is the only selectable baud rate). Rockwell claims that a Gallium Arsenide IC that counts down a clock signal was failing because of contamination from the plastic package of the IC (suppliers fault). This Rockwell unit was returned for repair under warranty.
- The second Rockwell unit tested output data but did not navigate. Power was applied to the unit with reverse polarity (Sandia's fault) and an internal rectifier bridge allowed the unit to function, but not properly. Applying power in the correct manner (positive on the outside contact) fixed the problem.


## Trimble Placer

- No problems, unit functioned correctly out of the box.


### 3.3.4.2 Summary of critical integration issues

Flexible software interface Having the flexibility to control the data output by the receiver is important. This includes serial data format (TTL, RS-232, RS-422). baud rates, and packet data rates. It is desirable to have the receiver output position data at fixed data rate, that is user selectable. It is also desirable to be able to request other data packets when needed. All of the receivers with the exception of the Rockwell unit were fairly flexible. The Rockwell unit on the other hand outputs position data at a fixed $1-\mathrm{Hz}$ rate and fixed baud rate of 9600 baud.

The format of the data packets is also important. ASCII formats are easier to work with because the raw data can be stored and then analyzed visually. The Rockwell unit uses an IEEE floating point
format. Although Binary data formats and the Rockwell format might be more efficient, it is much easier to troubleshoot a problem when the data docs not have to be post processed just to take a quick look.

Differential capability The capability to receive differential corrections is important if increased accuracy is desired. Although a near-term fielded system might not use differential corrections, the availability of subscriber networks that broadcast differential corrections in the future will probably make this a likely upgrade.

Time to first fix A fast time-to-first-fix is important. However, all newer receivers usually advertise a first fix in under one minute when the receiver knows its approximate position. The difference between a 30 -second first fix and a one-minute first fix is probably not that important. This parameter also affects how quickly the receiver can reacquire satellites after blockages.

Memory back up Different manufacturers use different approaches for providing power to back up the static memory (which stores the last location, almanac, ephemeris, and receiver parameters) when the receiver is powered down. These include an internal lithium battery, an external voltage supplied by the integrator, and a large capacitor. The large capacitor has the advantage of never needing replacement. This approach is taken on the Rockwell NavCore V. However, the capacitor charge can only last for several weeks. An internal lithium battery can last for several years, but will eventually need replacement. An external voltage supplied by the integrator can come from a number of sources, but must be taken into account when doing the system design.

Size, Power, and packaging Low power consumption and small size are advantageous for vehicular applications. Some manufacturers also offer the antenna and receiver integrated into a single package. This has some advantages, but limits antenna choices.

Active/passive antenna Active antennas with built-in amplifiers allow longer cable runs to the receiver. Passive antennas require no power but can not be used with longer cabling because of losses.

Cable length and number of connectors The losses in the cabling and connectors must be taken into account when designing the cabling and choosing the appropriate antenna.

Receiver/antenna sensitivity Increased receiver/antenna sensitivity will reduce the affects of foliage and other obstructions. The sensitivity is affected by the receiver, the cabling, as well as the antenna used.

Position accuracy Both static and dynamic position accuracy are important. However, the effects of SA reduce the accuracy of all receivers significantly. Differential accuracy will become an important parameter in the future.

Technical Support Good technical support, including quick turn around times for repairs, is very important. Quick turn around for failed units can also be accomplished by keeping spares in stock.

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## Chapter 4

## Sensors for Map-Based Positioning

Most sensors used for the purpose of map building involve some kind of distance measurement. There are three basically different approaches to measuring range:

- Sensors based on measuring the time of flight (TOF) of a pulse of emitted energy traveling to a reflecting object, then echoing back to a receiver.
- The phase-shift measurement (or phase-detection) ranging technique involves continuous wave transmission as opposed to the short pulsed outputs used in TOF systems.
- Sensors based on frequency-modulated (FM) radar. This technique is somewhat related to the (amplitude-modulated) phase-shift measurement technique.


### 4.1 Time-of-Flight Range Sensors

Many of today's range sensors use the time-of-flight (TOF) method. The measured pulses typically come from an ultrasonic, RF, or optical energy source. Therefore, the relevant parameters involved in range calculation are the speed of sound in air (roughly $0.3 \mathrm{~m} / \mathrm{ms}-1 \mathrm{ft} / \mathrm{ms}$ ), and the speed of light ( $0.3 \mathrm{~m} / \mathrm{ns}-1 \mathrm{ft} / \mathrm{ns}$ ). Using elementary physics, distance is determined by multiplying the velocity of the energy wave by the time required to travel the round-trip distance:
$d=v t$
where
$d$ = round-trip distance
$v=$ speed of propagation
$t$ = elapsed time.
The measured time is representative of traveling twice the separation distance (i.e., out and back) and must therefore be reduced by half to result in actual range to the target.

The advantages of TOF systems arise from the direct nature of their straight-line active sensing. The returned signal follows essentially the same path back to a receiver located coaxially with or in close proximity to the transmitter. In fact, it is possible in some cases for the transmitting and receiving transducers to be the same device. The absolute range to an observed point is directly available as output with no complicated analysis required, and the technique is not based on any assumptions concerning the planar properties or orientation of the target surface. The missing parts problem seen in triangulation does not arise because minimal or no offset distance between transducers is needed. Furthermore, TOF sensors maintain range accuracy in a linear fashion as long as reliable echo detection is sustained, while triangulation schemes suffer diminishing accuracy as distance to the target increases.

Potential error sources for TOF systems include the following:

- Variations in the speed of propagation, particularly in the case of acoustical systems.
- Uncertainties in determining the exact time of arrival of the reflected pulse.
- Inaccuracies in the timing circuitry used to measure the round-trip time of flight.
- Interaction of the incident wave with the target surface.

Each of these areas will be briefly addressed below, and discussed later in more detail.
a. Propagation Speed For mobile robotics applications, changes in the propagation speed of electromagnetic energy are for the most part inconsequential and can basically be ignored, with the exception of satellite-based position-location systems as presented in Chapter 3. This is not the case, however, for acoustically based systems, where the speed of sound is markedly influenced by temperature changes, and to a lesser extent by humidity. (The speed of sound is actually proportional to the square root of temperature in degrees Rankine.) An ambient temperature shift of just $30^{\circ} \mathrm{F}$ can cause a 0.3 meter ( 1 ft ) error at a measured distance of 10 meters ( 35 ft ) [Everett, 1985].
b. Detection Uncertainties So-called time-walk errors are caused by the wide dynamic range in returned signal strength due to varying reflectivities of target surfaces. These differences in returned signal intensity influence the rise time of the detected pulse, and in the case of fixedthreshold detection will cause the more reflective targets to appear closer. For this reason, constant fraction timing discriminators are typically employed to establish the detector threshold at some specified fraction of the peak value of the received pulse [Vuylsteke et al., 1990].
c. Timing Considerations Due to the relatively slow speed of sound in air, compared to light, acoustically based systems face milder timing demands than their light-based counterparts and as a result are less expensive. Conversely, the propagation speed of electromagnetic energy can place severe requirements on associated control and measurement circuitry in optical or RF implementations. As a result, TOF sensors based on the speed of light require sub-nanosecond timing circuitry to measure distances with a resolution of about a foot [Koenigsburg, 1982]. More specifically, a desired resolution of 1 millimeter requires a timing accuracy of 3 picoseconds ( $3 \times 10^{-12}$ s) [Vuylsteke et al., 1990]. This capability is somewhat expensive to realize and may not be cost effective for certain applications, particularly at close range where high accuracies are required.
d. Surface Interaction When light, sound, or radio waves strike an object, any detected echo represents only a small portion of the original signal. The remaining energy reflects in scattered directions and can be absorbed by or pass through the target, depending on surface characteristics and the angle of incidence of the beam. Instances where no return signal is received at all can occur because of specular reflection at the object's surface, especially in the ultrasonic region of the energy spectrum. If the transmission source approach angle meets or exceeds a certain critical value, the reflected energy will be deflected outside of the sensing envelope of the receiver. In cluttered environments soundwaves can reflect from (multiple) objects and can then be received by other sensors. This phenomenon is known as crosstalk (see Figure 4.1). To compensate, repeated measurements are often averaged to bring the signal-to-noise ratio within acceptable levels, but at the expense of additional time required to determine a single range value. Borenstein and Koren [1995] proposed a method that allows individual sensors to detect and reject crosstalk.

Using this method much faster firing rates - under 100 ms for a complete scan with 12 sonars - are feasible.

### 4.1.1 Ultrasonic TOF Systems

Ultrasonic TOF ranging is today the most common technique employed on indoor mobile robotics systems, primarily due to the ready availability of low-cost systems and their ease of interface. Over the past decade, much research has been conducted investigating applicability in such areas as world modeling and collision avoidance, position estimation, and motion detection. Several researchers have more recently begun to assess the effectiveness of ultrasonic sensors in


Figure 4.1: Crosstalk is a phenomenon in which one sonar picks up the echo from another. One can distinguish between a. direct crosstalk and b. indirect crosstalk. exterior settings [Pletta et al., 1992; Langer and Thorpe, 1992; Pin and Watanabe, 1993; Hammond, 1994]. In the automotive industry, BMW now incorporates four piezoceramic transducers (sealed in a membrane for environmental protection) on both front and rear bumpers in its Park Distance Control system [Siuru, 1994]. A detailed discussion of ultrasonic sensors and their characteristics with regard to indoor mobile robot applications is given in [Jörg, 1994].

Two of the most popular commercially available ultrasonic ranging systems will be reviewed in the following sections.

### 4.1.1.1 Massa Products Ultrasonic Ranging Module Subsystems

Massa Products Corporation, Hingham, MA, offers a full line of ultrasonic ranging subsystems with maximum detection ranges from 0.6 to 9.1 meters ( 2 to 30 ft ) [MASSA]. The E-201B series sonar operates in the bistatic mode with separate transmit and receive transducers, either side by side for echo ranging or as an opposed pair for unambiguous distance measurement between two uniquely defined points. This latter configuration is sometimes used in ultrasonic position location systems and provides twice the effective operating range with respect to that advertised for conventional echo ranging. The $E-220 B$ series (see Figure 4.2 ) is designed for monostatic (single transducer) operation but is otherwise functionally identical to the $E-201 B$. Either version can be externally triggered on command, or internally triggered by a free-running oscillator at a repetition rate determined by an external resistor (see Figure 4.3).

Selected specifications for the four operating frequencies available in the E-220B series are listed in Table 4.1 below. A removable focusing horn is provided for the $26-\mathrm{and} 40-\mathrm{kHz}$ models that decreases the effective beamwidth (when installed) from 35 to 15 degrees. The horn must be in place to achieve the maximum listed range.


Figure 4.2: The single-transducer Massa E-220B-series ultrasonic ranging module can be internally or externally triggered, and offers both analog and digital outputs. (Courtesy of Massa Products Corp.)


Digital


Figure 4.3: Timing diagram for the E-220B series ranging module showing analog and digital output signals in relationship to the trigger input. (Courtesy of Massa Products Corp.)

Table 4.1: Specifications for the monostatic E-220B Ultrasonic Ranging Module Subsystems. The E-201 series is a bistatic configuration with very similar specifications. (Courtesy of Massa Products Corp.)

| Parameter | $\mathrm{E}-220 \mathrm{~B} / 215$ | $\mathrm{E}-220 \mathrm{~B} / 150$ | $\mathrm{E}-220 \mathrm{~B} / 40$ | $\mathrm{E}-220 \mathrm{~B} / 26$ Units |
| :--- | ---: | ---: | ---: | ---: |
| Range | $10-61$ | $20-152$ | $61-610$ | $61-914 \mathrm{~cm}$ |
|  | $4-24$ | $8-60$ | $24-240$ | $24-360 \mathrm{in}$ |
| Beamwidth | 10 | 10 | $35(15)$ | $35(15) \circ$ |
| Frequency | 215 | 150 | 40 | 26 kHz |
| Max rep rate | 150 | 100 | 25 | 20 Hz |
| Resolution | 0.076 | 0.03 | 0.1 | 0.76 |
|  | $8-15$ | 0.04 | 0.3 | 1 cm |
| Power | $4-8$ | $4-15$ | $8-15$ | 0.4 in |
| Weight |  | $4-8$ | $4-8$ | $8-15 \mathrm{VDC}$ |
|  |  |  | $4-8 \mathrm{oz}$ |  |

### 4.1.1.2 Polaroid Ultrasonic Ranging Modules

The Polaroid ranging module is an active TOF device developed for automatic camera focusing, which determines the range to target by measuring elapsed time between the transmission of an ultrasonic waveform and the detected echo [Biber et al., 1987, POLAROID]. This system is the most widely found in mobile robotics literature [Koenigsburg, 1982; Moravec and Elfes, 1985; Everett, 1985; Kim, 1986; Moravec, 1988; Elfes, 1989; Arkin, 1989; Borenstein and Koren, 1990; 1991a; 1991b; 1995; Borenstein et al., 1995], and is representa-


Figure 4.4: The Polaroid OEM kit included the transducer and a small electronics interface board. tive of the general characteristics of such ranging devices. The most basic configuration consists of two fundamental components: 1) the ultrasonic transducer, and 2) the ranging module electronics. Polaroid offers OEM kits with two transducers and two ranging module circuit boards for less than $\$ 100$ (see Figure 4.4).

A choice of transducer types is now available. In the original instrument-grade electrostatic version, a very thin metal diaphragm mounted on a machined backplate formed a capacitive transducer as illustrated in Figure 4.5 [POLAROID, 1991]. The system operates in the monostatic transceiver mode so that only a single transducer is necessary to acquire range data. A smaller diameter electrostatic transducer (7000-series) has also been made available, developed for the Polaroid Spectra camera [POLAROID, 1987]. A more rugged piezoelectric (9000-series) environmental transducer for applications in severe environmental conditions including vibration is able to meet or exceed the SAE J1455 January 1988 specification for heavyduty trucks. Table 4.2 lists the technical specifications for the different Polaroid transducers.

The original Polaroid ranging module functioned by transmitting a chirp of four discrete fre-


Figure 4.5: The Polaroid instrument grade electrostatic transducer consists of a gold-plated plastic foil stretched across a machined backplate. (Reproduced with permission from Polaroid [1991].)
quencies at about of 50 kHz . The $S N 28827$ module was later developed with reduced parts count, lower power consumption, and simplified computer interface requirements. This second-generation board transmits only a single frequency at 49.1 kHz . A third-generation board ( 6500 series) introduced in 1990 provided yet a further reduction in interface circuitry, with the ability to detect and report multiple echoes [Polaroid, 1990]. An Ultrasonic Ranging Developer's Kit based on the Intel 80C196 microprocessor is now available for use with the 6500 series ranging module that allows software control of transmit frequency, pulse width, blanking time, amplifier gain, and maximum range [Polaroid, 1993].

The range of the Polaroid system runs from about 41 centimeters to 10.5 meters ( 1.33 ft to 35 ft ). However, using custom circuitry suggested in [POLAROID, 1991] the minimum range can be reduced reliably to about 20 centimeters ( 8 in ) [Borenstein et al., 1995]. The beam dispersion angle is approximately 30 degrees. A typical operating cycle is as follows.

1. The control circuitry fires the transducer and waits for indication that transmission has begun.
2. The receiver is blanked for a short period of time to prevent false detection due to ringing from residual transmit signals in the transducer.
3. The received signals are amplified with increased gain over time to compensate for the decrease in sound intensity with distance.
4. Returning echoes that exceed a fixed threshold value are recorded and the associated distances calculated from elapsed time.


Figure 4.6 [Polaroid, 1990] illustrates the operation of the sensor in a timing diagram. In the single-echo mode of operation for the 6500-series module, the blank (BLNK) and blank-inhibit (BINH) lines are held low as the initiate (INIT) line goes high to trigger the outgoing pulse train. The internal blanking (BLANKING) signal automatically goes high for 2.38 milliseconds to prevent transducer ringing from being misinterpreted as a returned echo. Once a valid return is received, the echo (ECHO) output will latch high until reset by a high-to-low transition on INIT.

For multiple-echo processing, the blanking (BLNK) input must be toggled high for at least 0.44 milliseconds after detection of the first return signal to reset the echo output for the next return.


Figure 4.6: Timing diagram for the 6500-Series Sonar Ranging Module executing a multiple-echo-mode cycle with blanking input. (Courtesy of Polaroid Corp.)

### 4.1.2 Laser-Based TOF Systems

Laser-based TOF ranging systems, also known as laser radar or lidar, first appeared in work performed at the Jet Propulsion Laboratory, Pasadena, CA, in the 1970s [Lewis and Johnson, 1977]. Laser energy is emitted in a rapid sequence of short bursts aimed directly at the object being ranged. The time required for a given pulse to reflect off the object and return is measured and used to calculate distance to the target based on the speed of light. Accuracies for early sensors of this type could approach a few centimeters over the range of 1 to 5 meters ( 3.3 to 16.4 ft ) [NASA, 1977; Depkovich and Wolfe, 1984].

### 4.1.2.1 Schwartz Electro-Optics Laser Rangefinders

Schwartz Electro-Optics, Inc. (SEO), Orlando, FL, produces a number of laser TOF rangefinding systems employing an innovative time-to-amplitude-conversion scheme to overcome the subnanosecond timing requirements necessitated by the speed of light. As the laser fires, a precision capacitor begins discharging from a known set point at a constant rate. An analog-to-digital conversion is performed on the sampled capacitor voltage at the precise instant a return signal is detected, whereupon the resulting digital representation is converted to range using a look-up table.

## SEO LRF-200 OEM Laser Rangefinders

The LRF-200 OEM Laser Rangefinder shown in Figure 4.7 features compact size, high-speed processing, and the ability to acquire range information from most surfaces (i.e., minimum 10percent Lambertian reflectivity) out to a maximum of 100 meters ( 328 ft ). The basic system uses a pulsed InGaAs laser diode in conjunction with an avalanche photodiode detector, and is available with both analog and digital (RS-232) outputs. Table 4.3 lists general specifications for the sensor's performance [SEO, 1995a].


Figure 4.7: The LRF-200 OEM Laser Rangefinder. (Courtesy of Schwartz Electro-Optics, Inc.)

Another adaptation of the LRF-200 involved the addition of a mechanical single-DOF beam scanning capability. Originally developed for use in submunition sensor research, the Scanning Laser Rangefinder is currently installed on board a remotely piloted vehicle. For this application, the sensor is positioned so the forward motion of the RPV is perpendicular to the vertical scan plane, since three-dimensional target profiles are required [SEO, 1991b]. In a second application, the Scanning Laser Rangefinder was used by the Field Robotics Center at Carnegie Mellon University as a terrain mapping sensor on their unmanned autonomous vehicles.

Table 4.3: Selected specifications for the LRF 200 OEM Laser Rangefinder. (Courtesy of Schwartz Electro-Optics, Inc.)

| Electro-Optics, Inc.) | Value |  |
| :--- | ---: | :--- |
| Parameter | Units |  |
| Range (non-cooperative | 1 to 100 | m |
| target) | $3.3-328$ | ft |
| Accuracy | $\pm 30$ | cm |
|  | $\pm 12$ | in |
| Range jitter | $\pm 12$ | cm |
|  | $\pm 4.7$ | in |
| Wavelength | 902 | nm |
| Diameter | 89 | mm |
|  | 3.5 | in |
|  | 178 | mm |
| Length | 7 | in |
|  | 1 | kg |
| Weight | 2.2 | lb |
|  | 8 to 24 | VDC |
| Power | 5 | W |

Table 4.4: Selected specifications for the SEO
Scanning Laser Rangefinder. (Courtesy of Schwartz
Electro-Optics, Inc.)

| Parameter | Value $\quad$ Units |
| :--- | ---: |
| Range | $1-100 \mathrm{~m}$ |
|  | $3.3-330 \mathrm{ft}$ |
| Accuracy | $\pm 30 \mathrm{~cm}$ |
|  | $\pm 12 \mathrm{in}$ |
| Scan angle | $\pm 30$ |
| Scan rate | $24.5-30.3 \mathrm{kHz}$ |
| Samples per scan | 175 |
| Wavelength | 920 nm |
| Diameter | 127 mm |
|  | 5 in |
| Length | 444 mm |
|  | 17.5 in |
| Weight | 5.4 kg |
|  | 11.8 lb |
| Power | $8-25 \mathrm{VDC}$ |

## SEO Scanning Helicopter Interference Envelope Laser Detector (SHIELD)

This system was developed for the U.S. Army [SEO, 1995b] as an onboard pilot alert to the presence of surrounding obstructions in a 60 -meter radius hemispherical envelope below the helicopter. A high-pulse-repetition-rate GaAs eye-safe diode emitter shares a common aperture with a sensitive avalanche photodiode detector. The transmit and return beams are reflected from a motor-driven prism rotating at 18 rps (see Figure 4.9). Range measurements are correlated with the azimuth angle using an optical encoder. Detected obstacles are displayed on a 5.5 -inch color monitor. Table 4.5 lists the key specifications of the SHIELD.

Table 4.5: Selected specifications for the Scanning Helicopter Interference Envelope Laser Detector (SHIELD). (Courtesy of Schwartz Electro-Optics, Inc.)

| Parameter | Value |
| :--- | ---: |
| Maximum range | Units |
| (hemispherical envelope) | $>600 \mathrm{~m}$ |
| Accuracy | $<30 \mathrm{~cm}$ |
|  | 1 ft |
| Wavelength | 905 nm |
| Scan angle | $360 \circ$ |
| Scan rate | 18 Hz |
| Length | 300 mm |
|  | 11.75 in |
| Weight | 15 lb |
| Power | 18 VDC |
|  | $<5 \mathrm{~A}$ |

## SEO TreeSense



Figure 4.8: The Scanning Helicopter Interference Envelope Laser Detector (SHIELD). (Courtesy of Schwartz Electro-Optics, Inc.)

The TreeSense system was developed by SEO for automating the selective application of pesticides to orange trees, where the goal was to enable individual spray nozzles only when a tree was detected within their associated field of coverage. The sensing subsystem (see Figure 4.9) consists of a horizontally oriented unit mounted on the back of an agricultural vehicle, suitably equipped with a rotating mirror arrangement that scans the beam in a vertical plane orthogonal to the direction of travel. The scan rate is controllable up to 40 rps ( 35 rps typical). The ranging subsystem is gated on and off twice during each revolution to illuminate two 90 -degree fan-shaped sectors to a maximum range of 7.6 meters ( 25 ft ) either side of the vehicle as shown in Figure 4.10. The existing hardware is theoretically capable of ranging to 9 meters ( 30 ft ) using a PIN photodiode and can be extended further through an upgrade option that incorporates an avalanche photodiode detector.

The TreeSense system is hard-wired to a valve manifold to enable/disable a vertical array of nozzles for the spraying of insecticides, but analog as well as digital (RS-232) output can easily be made available for other applications. The system is housed in a rugged aluminum enclosure with a total weight of only 2.2 kilograms ( 5 lb ). Power requirements are 12 W at 12 VDC . Further details on the system are contained in Table 4.6.


Figure 4.9: The SEO TreeSense. (Courtesy of Schwartz Electro-Optics, Inc.)


Figure 4.10: Scanning pattern of the SEO TreeSense system. (Courtesy of Schwartz Electro-Optics, Inc.)

## SEO AutoSense

The AutoSense I system was developed by SEO under a Department of Transportation Small Business Innovative Research (SBIR) effort as a replacement for buried inductive loops for traffic signal control. (Inductive loops don't always sense motorcyclists and some of the smaller cars with fiberglass or plastic body panels, and replacement or maintenance can be expensive as well as disruptive to traffic flow.) The system is configured to look down at about a 30-degree angle on moving vehicles in a traffic lane as illustrated in Figure 4.12.

AutoSense I uses a PIN photo-diode detector and a pulsed ( 8 ns ) InGaAs near-infrared laser-diode source with peak power of 50 W . The laser output is directed by a beam splitter into a pair of cylindrical lenses to generate two fan-shaped beams 10 degrees apart in elevation for improved target detection. (The original prototype projected only a single spot of light, but ran into problems due to target absorption and specular reflection.) As an added benefit, the use of two separate beams makes it possible to calculate the speed of moving vehicles to an accuracy of $1.6 \mathrm{~km} / \mathrm{h}(1 \mathrm{mph})$. In addition, a two-dimensional image (i.e., length and


Figure 4.11: Color-coded range image created by the SEO TreeSense system. (Courtesy of Schwartz Electro-Optics, Inc.)

Table 4.6: Selected specifications for the TreeSense system. (Courtesy of Schwartz ElectroOptics, Inc.)

| Parameter | Value |
| :--- | ---: |
| Maximum range | 9 mits |
|  | 30 ft |
| Accuracy | $1 \%$ |
| (in \% of measured range) |  |
| Wavelength | 902 nm |
| Pulse repetition frequency | 15 KHz |
| Scan rate | 29.3 rps |
| Length | 229 mm |
|  | 9 in |
| Width | 229 mm |
|  | 9 in |
| Height | 115 mm |
|  | 4.5 in |
| Weight | 5 lbs |
| Power | 12 V |
|  | 12 W |



Figure 4.12: Two fan-shaped beams look down on moving vehicles for improved target detection. (Courtesy of Schwartz Electro-Optics, Inc.)
width) is formed of each vehicle as it passes through the sensor's field of view, opening the door for numerous vehicle classification applications under the Intelligent Vehicle Highway Systems concept.

AutoSense II is an improved second-generation unit (see Figure 4.13) that uses an avalanche photodiode detector instead of the PIN photodiode for greater sensitivity, and a multi-faceted rotating mirror with alternating pitches on adjacent facets to create the two beams. Each beam is scanned across the traffic lane 720 times per second, with 15 range measurements made per scan. This azimuthal scanning action generates a precise three-dimensional profile to better facilitate vehicle classification in automated toll booth applications. An abbreviated system block diagram is depicted in Figure 4.14.


Figure 4.13: The AutoSense I/ is SEO's active-infrared overhead vehicle imaging sensor. (Courtesy of Schwartz Electro-Optics, Inc.)


Figure 4.14: Simplified block diagram of the AutoSense // time-of-flight 3-D ranging system. (Courtesy of Schwartz Electro-Optics, Inc.)

Intensity information from the reflected signal is used to correct the "time-walk" error in threshold detection resulting from varying target reflectivities, for an improved range accuracy of $7.6 \mathrm{~cm}(3 \mathrm{in})$ over a 1.5 to 15 m ( 5 to 50 ft ) field of regard. The scan resolution is 1 degree, and vehicle velocity can be calculated with an accuracy of $3.2 \mathrm{~km} / \mathrm{h}(2 \mathrm{mph})$ at speeds up to $96 \mathrm{~km} / \mathrm{h}$ ( 60 mph ). A typical scan image created with the Autosense II is shown in Figure 4.15.

A third-generation AutoSense III is now under development for an application in Canada that requires 3 -dimensional vehicle profile generation at speeds up to $160 \mathrm{~km} / \mathrm{h}(100 \mathrm{mph})$. Selected specifications


Figure 4.15: Output sample from a scan with the AutoSense II.
a. Actual vehicle with trailer (photographed with a conventional camera).
b. Color-coded range information.
c. Intensity image.
(Courtesy of Schwartz Electro-Optics, Inc.)
for the AutoSense II package are provided in Table 4.7.

Table 4.7: Selected specifications for the AutoSense II ranging system. (Courtesy of Schwartz Electro-Optics, Inc.)

| Parameter | Value $\quad$ Units |  |
| :--- | ---: | :--- |
| Range | $0.61-1.50 \mathrm{~m}$ |  |
|  | $2-50 \mathrm{ft}$ |  |
| Accuracy | 7.5 cm |  |
|  | 3 in |  |
| Wavelength | 904 nm |  |
| Pulse repetition rate | 86.4 kHz |  |
| Scan rate | $720 \mathrm{scans} / \mathrm{s} / \mathrm{scanline}$ |  |
| Range readings per scan | 30 |  |
| Weight | 11.4 kg |  |
|  | 25 lb |  |
| Power | 115 | VAC |
|  | 75 W |  |

### 4.1.2.2 RIEGL Laser Measurement Systems

RIEGL Laser Measurement Systems, Horn, Austria, offers a number of commercial products (i.e., laser binoculars, surveying systems, "speed guns," level sensors, profile measurement systems, and tracking laser scanners) employing short-pulse TOF laser ranging. Typical applications include lidar altimeters, vehicle speed measurement for law enforcement, collision avoidance for cranes and vehicles, and level sensing in silos. All RIEGL products are distributed in the United States by RIEGEL USA, Orlando, FL.

## LD90-3 Laser Rangefinder

The RIEGL LD90-3 series laser rangefinder (see Figure 4.16) employs a near-infrared laser diode source and a photodiode detector to perform TOF ranging out to 500 meters ( $1,640 \mathrm{ft}$ ) with diffuse surfaces, and to over 1,000 meters ( $3,281 \mathrm{ft}$ ) in the case of co-operative targets. Round-trip propagation time is precisely measured by a quartz-stabilized clock and converted to measured distance by an internal microprocessor using one of two available algorithms. The clutter suppression algorithm incorporates a combination of range measurement averaging and noise rejection techniques to filter out backscatter from airborne particles, and is therefore useful when operating under conditions of poor visibility [Riegl, 1994]. The standard measurement algorithm, on the other hand, provides rapid range measurements without regard for noise suppression, and can subsequently deliver a higher update rate under more favorable environmental conditions. Worst-case range measurement accuracy is $\pm 5$ centimeters ( $\pm 2$ in), with typical values of around $\pm 2$ centimeters ( $\pm 0.8$ in). See Table 4.8 for a complete listing of the LD90-3's features.

The pulsed near-infrared laser is Class-1 eye safe under all operating conditions. A nominal beam divergence of 0.1 degrees ( 2 mrad ) for the LD90-3100 unit (see Tab. 4.9 below) produces a 20 centimeter ( 8 in ) footprint of illumination at 100 meters ( 328 ft ) [Riegl, 1994]. The complete system is housed in a small light-weight metal enclosure weighing only 1.5 kilograms ( 3.3 lb ), and draws 10 W at 11 to 18 VDC . The standard output format is serial RS-232 at programmable data


Figure 4.16: The RIEGL LD90-3 series laser rangefinder. (Courtesy of Riegl USA.)
rates up to 19.2 kilobits per second, but RS-422 as well as analog options ( 0 to 10 VDC and 4 to 20 mA current-loop) are available upon request.

Table 4.8: Selected specifications for the RIEGL LD90-3 series laser rangefinder. (Courtesy of RIEGL Laser Measurement Systems.)

| Parameter |  | LD90-3100 | LD90-3300 Units |
| :--- | :--- | ---: | ---: |
| Maximum range | (diffuse) | 150 | 400 m |
|  |  | 492 | $1,312 \mathrm{ft}$ |
|  | (cooperative) | $>1000$ | $>1000 \mathrm{~m}$ |
|  |  | $>3,280$ | $>3,280 \mathrm{ft}$ |
| Minimum range |  | 1 | $3-5 \mathrm{~m}$ |
| Accuracy | (distance) | 2 | 5 cm |
|  | (velocity) | $3 / 4$ | 2 in |
|  | 0.3 | $0.5 \mathrm{~m} / \mathrm{s}$ |  |
| Beam divergence | 2 | 2.8 mrad |  |
| Output | (digital) | RS-232, -422 | RS-232, -422 |
|  | $0-10$ | $0-10 \mathrm{VDC}$ |  |
| Power | (analog) | $11-18$ | $11-18 \mathrm{VDC}$ |
|  |  | 10 | 10 W |
| Size |  | $22 \times 13 \times 7.6$ | $22 \times 13 \times 7.6 \mathrm{~cm}$ |
|  |  | $8.7 \times 5.1 \times 3$ | $8.7 \times 5.1 \times 3 \mathrm{in}$ |
| Weight | 3.3 | 3.3 lb |  |

## Scanning Laser Rangefinders

The LRS90-3 Laser Radar Scanner is an adaptation of the basic LD90-3 electronics, fiber-optically coupled to a remote scanner unit as shown in Figure 4.17. The scanner package contains no internal electronics and is thus very robust under demanding operating conditions typical of industrial or robotics scenarios. The motorized scanning head pans the beam back and forth in the horizontal plane at a $10-\mathrm{Hz}$ rate, resulting in 20 data-gathering sweeps per second. Beam divergence is 0.3 degrees ( 5 mrad ) with the option of expanding in the vertical direction if desired up to 2 degrees.


Figure 4.17: The LRS90-3 Laser Radar Scanner consists of an electronics unit (not shown) connected via a duplex fiber-optic cable to the remote scanner unit depicted above. (Courtesy of RIEGL USA.)

The LSS390 Laser Scanning System is very similar to the LRS90-3, but scans a more narrow field of view ( $10^{\circ}$ ) with a faster update rate $(2000 \mathrm{~Hz}$ ) and a more tightly focused beam. Range accuracy is 10 centimeters ( 4 in ) typically and 20 centimeters ( 8 in ) worst case. The LSS390 unit is available with an RS-422 digital output ( 19.2 kbs standard, 150 kbs optional) or a 20 bit parallel TTL interface.

Table 4.9: Typical specifications for the LRS90-3 Laser Radar Scanner and the LSS390 Laser
Scanner System. (Courtesy of RIEGL USA.)

| Parameter |  | LRS90-3 | LSS390 Units |
| :---: | :---: | :---: | :---: |
| Maximum range |  | 80 | 60 m |
|  |  | 262 | 197 ft |
| Minimum range |  | 2 | 1 m |
|  |  | 6.5 | 3.25 ft |
| Accuracy |  | 3 | 10 cm |
|  |  | 1.2 | 4 ft |
| Beam divergence |  | 5 | 3.5 mrad |
| Sample rate |  | 1000 | 2000 Hz |
| Scan range |  | 18 | 10 。 |
| Scan rate |  | 10 | 10 scans/s |
| Output | (digital) | RS-232, -422 | parallel, RS-422 |
| Power |  | 11-15 | 9-16 VDC |
|  |  | 880 | mA |
| Size | (electronics) | $22 \times 13 \times 7.6$ | $22 \times 13 \times 7.6 \mathrm{~cm}$ |
|  |  | $8.7 \times 5.1 \times 3$ | $8.7 \times 5.1 \times 3$ in |
|  | (scanner) | $18 \times 10 \times 10$ | $18 \times 10 \times 10 \mathrm{~cm}$ |
|  |  | $7 \times 4 \times 4$ | $7 \times 4 \times 4$ in |
| Weight | (electronics) | 7.25 | 2.86 lb |
|  | (scanner) | 3.52 | 2 lb |

### 4.1.2.3 RVSI Long Optical Ranging and Detection System

Robotic Vision Systems, Inc., Haupaugue, NY, has conceptually designed a laser-based TOF ranging system capable of acquiring three-dimensional image data for an entire scene without scanning. The Long Optical Ranging and Detection System (LORDS) is a patented concept incorporating an optical encoding technique with ordinary vidicon or solid state camera(s), resulting in precise distance measurement to multiple targets in a scene illuminated by a single laser pulse. The design configuration is relatively simple and comparable in size and weight to traditional TOF and phaseshift measurement laser rangefinders (Figure 4.18).

Major components will include a single laser-energy source; one or more imaging cameras, each with an electronically implemented shuttering mechanism; and the associated control and processing electronics. In a typical configuration, the laser will emit a $25-\mathrm{mJ}$ (millijoule) pulse lasting 1 nanosecond, for an effective transmission of 25 mW . The anticipated operational wavelength will lie between 532 and 830 nanometers, due to the ready availability within this range of the required laser source and imaging arrays.

The cameras will be two-dimensional CCD arrays spaced closely together with parallel optical axes resulting in nearly identical, multiple views of the illuminated surface. Lenses for these cameras will be of the standard photographic varieties between 12 and 135 millimeters. The shuttering


Figure 4.18: Simplified block diagram of a three-camera configuration of the LORDS 3-D laser TOF rangefinding system. (Courtesy of Robotics Vision Systems, Inc.)
function will be performed by microchannel plate image intensifiers (MCPs) 18 or 25 millimeters in size, which will be gated in a binary encoding sequence, effectively turning the CCDs on and off during the detection phase. Control of the system will be handled by a single-board processor based on the Motorola MC-68040.

LORDS obtains three-dimensional image information in real time by employing a novel time-offlight technique requiring only a single laser pulse to collect all the information for an entire scene. The emitted pulse journeys a finite distance over time; hence, light traveling for 2 milliseconds will illuminate a scene further away than light traveling only 1 millisecond.

The entire sensing range is divided into discrete distance increments, each representing a distinct range plane. This is accomplished by simultaneously gating the MCPs of the observation cameras according to their own unique on-off encoding pattern over the duration of the detection phase. This binary gating alternately blocks and passes any returning reflection of the laser emission off objects within the field-of-view. When the gating cycles of each camera are lined up and compared, there exists a uniquely coded correspondence which can be used to calculate the range to any pixel in the scene.


Figure 4.19: Range ambiguity is reduced by increasing the number of binary range gates. (Courtesy of Robotic Vision Systems, Inc.)

For instance, in a system configured with only one camera, the gating MCP would be cycled on for half the detection duration, then off the remainder of the time. Figure 4.19 shows any object detected by this camera must be positioned within the first half of the sensor's overall range (half the distance the laser light could travel in the allotted detection time). However, significant distance ambiguity exists because the exact time of detection of the reflected energy could have occurred anywhere within this relatively long interval.

This ambiguity can be reduced by a factor of two through the use of a second camera with its associated gating cycled at twice the rate of the first. This scheme would create two complete on-off sequences, one taking place while the first camera is on and the other while the first camera is off. Simple binary logic can be used to combine the camera outputs and further resolve the range. If the first camera did not detect an object but the second did, then by examining the instance when the first camera is off and the second is on, the range to the object can be associated with a relatively specific time frame. Incorporating a third camera at again twice the gating frequency (i.e., two cycles for every one of camera two, and four cycles for every one of camera one) provides even more resolution. As Figure 4.20 shows, for each additional CCD array incorporated into the system, the number of distance divisions is effectively doubled.


Figure 4.20: Binary coded images from range gates 1-3 are combined to generate the composite range map on the far right. (Courtesy of Robotics Vision Systems, Inc.)

Alternatively, the same encoding effect can be achieved using a single camera when little or no relative motion exists between the sensor and the target area. In this scenario, the laser is pulsed multiple times, and the gating frequency for the single camera is sequentially changed at each new transmission. This creates the same detection intervals as before, but with an increase in the time required for data acquisition.

LORDS is designed to operate over distances between one meter and several kilometers. An important characteristic is the projected ability to range over selective segments of an observed scene to improve resolution in that the depth of field over which a given number of range increments is spread can be variable. The entire range of interest is initially observed, resulting in the maximum distance between increments (coarse resolution). An object detected at this stage is thus localized to a specific, abbreviated region of the total distance.

The sensor is then electronically reconfigured to cycle only over this region, which significantly shortens the distance between increments, thereby increasing resolution. A known delay is introduced between transmission and the time when the detection/gating process is initiated. The laser light thus travels to the region of interest without concern for objects positioned in the foreground.

### 4.2 Phase-Shift Measurement

The phase-shift measurement (or phase-detection) ranging technique involves continuous wave transmission as opposed to the short pulsed outputs used in TOF systems. A beam of amplitudemodulated laser, RF, or acoustical energy is directed towards the target. A small portion of this wave (potentially up to six orders of magnitude less in amplitude) is reflected by the object's surface back to the detector along a direct path [Chen et al., 1993]. The returned energy is compared to a simultaneously generated reference that has been split off from the original signal, and the relative phase shift between the two is measured as illustrated in Figure 4.21 to ascertain the round-trip distance the wave has traveled. For high-frequency RF- or laser-based systems, detection is usually preceded by heterodyning the reference and received signals with an intermediate frequency (while preserving the relative phase shift) to allow the phase detector to operate at a more convenient lower frequency [Vuylsteke, 1990].


Figure 4.21: Relationship between outgoing and reflected waveforms, where x is the distance corresponding to the differential phase. (Adapted from [Woodbury et al., 1993].)

The relative phase shift expressed as a function of distance to the reflecting target surface is [Woodbury et al., 1993]:
$\phi=\frac{4 \pi d}{\lambda}$
where
$\phi=$ phase shift
$d=$ distance to target
$\lambda=$ modulation wavelength.

The desired distance to target $d$ as a function of the measured phase shift $\phi$ is therefore given by

$$
\begin{equation*}
d=\frac{\phi \lambda}{4 \pi}=\frac{\phi c}{4 \pi f} \tag{4.2}
\end{equation*}
$$

where
$f=$ modulation frequency.
For square-wave modulation at the relatively low frequencies typical of ultrasonic systems (20 to 200 kHz ), the phase difference between incoming and outgoing waveforms can be measured with the simple linear circuit shown in Figure 4.22 [Figueroa and Barbieri, 1991]. The output of the exclusive-or gate goes high whenever its inputs are at opposite logic levels, generating a voltage across capacitor C that is proportional to the phase shift. For example, when the two signals are in phase (i.e., $\phi=0$ ), the gate output stays low and $V$ is zero; maximum output voltage occurs when $\phi$ reaches 180 degrees. While easy to implement, this simplistic approach is limited to low frequencies, and may require frequent calibration to compensate for drifts and offsets due to component aging or changes in ambient conditions [Figueroa and Lamancusa, 1992].

At higher frequencies, the phase shift between outgoing and reflected sine waves can be measured by multiplying the two signals together in an electronic mixer, then averaging the product over many modulation cycles [Woodbury et al., 1993]. This integration process can be relatively time consuming, making it difficult to achieve extremely rapid update rates. The result can be expressed mathematically as follows [Woodbury et al., 1993]:

$$
\begin{equation*}
\lim _{T-\infty} \frac{1}{T} \int_{0}^{T} \sin \left(\frac{2 \pi c}{\lambda} t+\frac{4 \pi d}{\lambda}\right) \sin \left(\frac{2 \pi c}{\lambda}\right) d t \tag{4.3}
\end{equation*}
$$

which reduces to
$A \cos \frac{4 \pi d}{\lambda}$
where
$t=$ time
$T=$ averaging interval
$A=$ amplitude factor from gain of integrating amplifier.

From the earlier expression for $\phi$, it can be seen that the quantity actually measured is in fact the cosine of the phase shift and not the phase shift itself [Woodbury et al., 1993]. This situation introduces a so-called ambiguity interval for scenarios where the round-trip distance exceeds the modulation wavelength (i.e., the phase measurement becomes ambiguous once $\phi$
exceeds $360^{\circ}$ ). Conrad and Sampson [1990] define this ambiguity interval as the maximum range that allows the phase difference to go through one complete cycle of 360 degrees:

$$
\begin{equation*}
R_{a}=\frac{c}{2 f} \tag{4.5}
\end{equation*}
$$

where
$R_{a}=$ ambiguity range interval
$f=$ modulation frequency
$c=$ speed of light.
Referring again to Figure 4.21, it can be seen that the total round-trip distance $2 d$ is equal to some integer number of wavelengths $n \lambda$ plus the fractional wavelength distance $x$ associated with the phase shift. Since the cosine relationship is not single valued for all of $\phi$, there will be more than one distance $d$ corresponding to any given phase shift measurement [Woodbury et al., 1993]:

$$
\begin{equation*}
\cos \phi=\cos \left(\frac{4 \pi d}{\lambda}\right)=\cos \left(\frac{2 \pi(x+n \lambda)}{\lambda}\right) \tag{4.6}
\end{equation*}
$$

where:
$d=(x+n \lambda) / 2=$ true distance to target.
$x=$ distance corresponding to differential phase $\phi$.
$n=$ number of complete modulation cycles.
The potential for erroneous information as a result of this ambiguity interval reduces the appeal of phase-detection schemes. Some applications simply avoid such problems by arranging the optical path so that the maximum possible range is within the ambiguity interval. Alternatively, successive measurements of the same target using two different modulation frequencies can be performed, resulting in two equations with two unknowns, allowing both $x$ and $n$ to be uniquely determined. Kerr [1988] describes such an implementation using modulation frequencies of 6 and 32 MHz .

Advantages of continuous-wave systems over pulsed time-of-flight methods include the ability to measure the direction and velocity of a moving target in addition to its range. In 1842, an Austrian by the name of Johann Doppler published a paper describing what has since become known as the Doppler effect. This well-known mathematical relationship states that the frequency of an energy wave reflected from an object in motion is a function of the relative velocity between the object and the observer. This subject was discussed in detail in Chapter 1.

As with TOF rangefinders, the paths of the source and the reflected beam are coaxial for phase-shift-measurement systems. This characteristic ensures objects cannot cast shadows when illuminated by the energy source, preventing the missing parts problem. Even greater measurement accuracy and overall range can be achieved when cooperative targets are attached to the objects of interest to increase the power density of the return signal.

Laser-based continuous-wave (CW) ranging originated out of work performed at the Stanford Research Institute in the 1970s [Nitzan et al., 1977]. Range accuracies approach those of pulsed laser TOF methods. Only a slight advantage is gained over pulsed TOF rangefinding, however, since the time-measurement problem is replaced by the need for fairly sophisticated phase-measurement electronics [Depkovich and Wolfe, 1984]. Because of the limited information obtainable from a single range point, laser-based systems are often scanned in one or more directions by either electromechanical or acousto-optical mechanisms.

### 4.2.1 Odetics Scanning Laser Imaging System

Odetics, Inc., Anaheim, CA, developed an adaptive and versatile scanning laser rangefinder in the early 1980s for use on ODEX 1, a six-legged walking robot [Binger and Harris, 1987; Byrd and DeVries, 1990]. The system determines distance by phase-shift measurement, constructing threedimensional range pictures by panning and tilting the sensor across the field of view. The phase-shift measurement technique was selected over acoustic-ranging, stereo vision and structured light alternatives because of the inherent accuracy and fast update rate.

The imaging system is broken down into the two major subelements depicted in Figure 4.23: the scan unit and the electronics unit. The scan unit houses the laser source, the photodetector, and the scanning mechanism. The laser source is a GaAlAs laser diode emitting at a wavelength of 820 nanometers; the power output is adjustable under software control between 1 to 50 mW . Detection of the returned energy is achieved through use of an avalanche photodiode whose output is routed to the phase-measuring electronics.


Figure 4.23: Block diagram of the Odetics scanning laser rangefinder. (Courtesy of Odetics, Inc.)

The scanning hardware consists of a rotating polygonal mirror which pans the laser beam across the scene, and a planar mirror whose back-and-forth nodding motion tilts the beam for a realizable field of view of 60 degrees in azimuth and 60 degrees in elevation. The scanning sequence follows a raster-scan pattern and can illuminate and detect an array of $128 \times 128$ pixels at a frame rate of 1.2 Hz [Boltinghouse et al., 1990].

The second subelement, the electronics unit, contains the range calculating and video processor as well as a programmable frame buffer interface. The range and video processor is responsible for controlling the laser transmission, activation of the scanning mechanism, detection of the returning
energy, and determination of range values. Distance is calculated through a proprietary phasedetection scheme, reported to be fast, fully digital, and self-calibrating with a high signal-to-noise ratio. The minimum observable range is 0.46 meters ( 1.5 ft ), while the maximum range without ambiguity due to phase shifts greater than 360 degrees is 9.3 meters ( 30 ft ).

For each pixel, the processor outputs a range value and a video reflectance value. The video data are equivalent to that obtained from a standard black-and-white television camera, except that interference due to ambient light and shadowing effects are eliminated. The reflectance value is compared to a prespecified threshold to eliminate pixels with insufficient return intensity to be properly processed, thereby eliminating potentially invalid range data; range values are set to maximum for all such pixels [Boltinghouse and Larsen, 1989]. A $3 \times 3$ neighborhood median filter is used to further filter out noise from data qualification, specular reflection, and impulse response [Larson and Boltinghouse, 1988].

The output format is a 16-bit data word consisting of the range value in either 8 or 9 bits, and the video information in either 8 or 7 bits, respectively. The resulting range resolution for the system is 3.66 centimeters ( 1.44 in ) for the 8 -bit format, and 1.83 centimeters ( 0.72 in ) with 9 bits. A buffer interface provides interim storage of the data and can execute single-word or whole-block direct-memory-access transfers to external host controllers under program control. Information can also be routed directly to a host without being held in the buffer. Currently, the interface is designed to support VAX, VME-Bus, Multibus, and IBM-PC/AT equipment. The scan and electronics unit together weigh 31 lb and require 2 A at 28 VDC .

### 4.2.2 ESP Optical Ranging System

A low-cost near-infrared rangefinder (see Fig. 4.24, Fig. 4.25, and Tab. 4.10) was developed in 1989 by ESP Technologies, Inc., Lawrenceville, NJ [ESP], for use in autonomous robot cart navigation in factories and similar environments. An eyesafe $2 \mathrm{~mW}, 820$-nanometer LED source is 100 percent modulated at 5 MHz and used to form a collimated 2.5 centimeters ( 1 in ) diameter transmit beam that is unconditionally eye-safe. Reflected radiation is focused by a 10 -centimeter ( 4 in) diameter coaxial Fresnel lens onto the photodetector; the measured phase shift is proportional to the roundtrip distance to the illuminated object. The Optical Ranging System (ORS-1) provides three outputs: range and angle of the target, and an automatic gain control (AGC) signal [Miller and Wagner, 1987]. Range resolution at 6.1 meters ( 20 ft ) is approximately 6 centimeters ( 2.5 in ), while angular resolution is about 2.5 centimeters ( 1 in ) at a range of 1.5 meters ( 5 ft ).

The ORS-1 AGC output signal is inversely proportional to the received signal strength and provides information about a target's near-infrared reflectivity, warning against insufficient or excessive signal return [ESP, 1992]. Usable range results are produced only when the corresponding gain signal is within a predetermined operating range. A rotating mirror mounted at 45 degrees to the optical axis provides 360 -degree polar-coordinate

Table 4.10: Selected specifications for the LEDbased near-infrared Optical Ranging System.
(Courtesy of ESP Technologies, Inc.)

| Parameter | ValueUnits <br> Accuracy <br> AGC output$<6 \mathrm{in}$ |
| :--- | ---: |
| Output power | $1-5 \mathrm{~V}$ |
| Beam width | 2 mW |
|  | 2.5 cm |
| Dimensions | 1 in |
|  | $15 \times 15 \times 30 \mathrm{~cm}$ |
| Weight | $6 \times 6 \times 12 \mathrm{in}$ |
| Power | 12 lb |
|  | 2 ADC |



Figure 4.24: Schematic drawing of the ORS-1 ranging system. (Courtesy of ESP Technologies, Inc.)
coverage. It is driven at 1 to 2 rps by a motor fitted with an integral incremental encoder and an optical indexing sensor that signals the completion of each revolution. The system is capable of simultaneous operation as a wideband optical communication receiver [Miller and Wagner, 1987].


Figure 4.25: The ORS-1 ranging system. (Courtesy of ESP Technologies, Inc.)

### 4.2.3 Acuity Research AccuRange 3000

Acuity Research, Inc., [ACUITY], Menlo Park, CA, has recently introduced an interesting product capable of acquiring unambiguous range data from 0 to 20 meters ( 0 to 66 ft ) using a proprietary technique similar to conventional phase-shift measurement (see Tab. 4.11). The AccuRange 3000 (see Figure 4.26) projects a collimated beam of near-infrared or visible laser light, amplitude modulated with a non-sinusoidal waveform at a 50 -percent duty cycle. A $63.6-$ millimeter ( 2.5 in ) collection aperture surrounding the laser diode emitter on the front face of the cylindrical housing gathers any reflected energy returning from the target, and


Figure 4.26: The AccuRange 3000 distance measuring sensor provides a square-wave output that varies inversely in frequency as a function of range. (Courtesy of Acuity Research, Inc.)
compares it to the outgoing reference signal to produce a square-wave output with a period of oscillation proportional to the measured range. The processing electronics reportedly are substantially different, however, from heterodyne phase-detection systems [Clark, 1994].

The frequency of the output signal varies from approximately 50 MHz at zero range to 4 MHz at 20 meters ( 66 ft ). The distance to
target can be determined through use of a frequency-tovoltage converter, or by measuring the period with a hardware or software timer [Clark, 1994]. Separate 0 to 10 V analog outputs are provided for returned signal amplitude, ambient light, and temperature to facilitate dynamic calibration for optimal accuracy in demanding applications. The range output changes within 250 nanoseconds to reflect any change in target distance, and all outputs are updated within a worst-case time frame of only $3 \mu \mathrm{~s}$. This rapid response rate (up to 312.5 kHz for all outputs with the optional SCSI interface) allows the beam to be manipulated at a 1,000 to $2,000 \mathrm{~Hz}$ rate with the mechanical-scanner option shown in Figure 4.27. A 45 -degree balanced-mirror arrangement is rotated under servo-control to deflect the coaxial outgoing and incoming beams for full 360 -degree planar coverage.

It is worthwhile noting that the AccuRange 3000 appears to be quite popular with commercial and academic lidar developers. For example, TRC (see Sec. 4.2.5 and 6.3.5) is using this sensor in their Lidar and Beacon Navigation products, and the University of Kaiserslautern, Germany, (see Sec. 8.2.3) has used the AccuRange 3000 in their in-house-made lidars.


Figure 4.27: A $360^{\circ}$ beam-deflection capability is provided by an optional single axis rotating scanner. (Courtesy of Acuity Research, Inc.)

### 4.2.4 TRC Light Direction and Ranging System

Transitions Research Corporation (TRC), Danbury, CT, offers a low-cost lidar system (see Figure 4.23) for detecting obstacles in the vicinity of a robot and/or estimating position from local landmarks, based on the previously discussed Acuity Research AccuRange 3000 unit. TRC adds a 2-DOF scanning mechanism employing a gold front-surfaced mirror specially mounted on a vertical pan axis that rotates between 200 and 900 rpm . The tilt axis of the scanner is mechanically synchronized to nod one complete cycle (down $45^{\circ}$ and back to horizontal) per 10 horizontal scans, effectively creating a protective spiral of detection coverage around the robot [TRC, 1994] (see Fig. 4.29). The tilt axis can be mechanically disabled if so desired for 360 -degree azimuthal scanning at a fixed elevation angle.

A $68 \mathrm{HCl1}$ microprocessor automatically compensates for variations in ambient lighting and sensor temperature, and reports range, bearing, and elevation data via an Ethernet or RS-232 interface. Power requirements are 500 mA at 12 VDC and 100 mA at 5 VDC . Typical operating parameters are listed in Table 4.12.

Table 4.12: Selected specifications for the TRC Light Direction and Ranging System. (Courtesy of
Transitions Research Corp.)

| Parameter | Value Units |
| :---: | :---: |
| Maximum range | $\begin{aligned} & 12 \mathrm{~m} \\ & 39 \mathrm{ft} \end{aligned}$ |
| Minimum range | 0 m |
| Laser output | 6 mW |
| Wavelength | 780 nm |
| Beam divergence | 0.5 mrad |
| Modulation frequency | 2 MHz |
| Accuracy (range) | $\begin{gathered} 25 \mathrm{~mm} \\ 1 \mathrm{in} \end{gathered}$ |
| Resolution (range) | $\begin{array}{r} 5 \mathrm{~mm} \\ 0.2 \text { in } \end{array}$ |
| (azimuth) | $0.18{ }^{\circ}$ |
| Sample rate | 25 kHz |
| Scan rate | 200-900 rpm |
| Size (scanner) | $\begin{aligned} & 13 \times 13 \times 35 \mathrm{~cm} \\ & 5 \times 5 \times 13.7 \mathrm{in} \end{aligned}$ |
| (electronics) | $\begin{aligned} & 30 \times 26 \times 5 \mathrm{~cm} \\ & 12 \times 10 \times 2 \mathrm{in} \end{aligned}$ |
| Weight | 4.4 lb |
| Power | 12 and 5 VDC |
|  | $\begin{gathered} 500 \text { and } \mathrm{mA} \\ 100 \end{gathered}$ |



Figure 4.28: The TRC Light Direction and Ranging System incorporates a two-axis scanner to provide full-volume coverage sweeping $360^{\circ}$ in azimuth and $45^{\circ}$ in elevation. (Courtesy of Transitions Research Corp.)


Figure 4.29: LightRanger data plotted from scans of a room. An open door at the upper left and a wall in the corridor detected through the open doorway are seen in the image to the left. On the right a trail has been left by a person walking through the room. (Courtesy of Transitions Research Corp.)

### 4.2.5 Swiss Federal Institute of Technology's "3-D Imaging Scanner"

Researchers at the Swiss Federal Institute of Technology, Zürich, Switzerland, have developed an optical rangefinder designed to overcome many of the problems associated with commercially available optical rangefinders [Adams, 1995]. The design concepts of the 3-D Imaging Scanner have been derived from Adam's earlier research work at Oxford University, U.K. [Adams, 1992]. Figure 4.30 shows the working prototype of the sensor. The transmitter consists of an eye-safe high-powered ( 250 mW ) Light Emitting Diode (LED) that provides a range resolution of $4.17 \mathrm{~cm} /{ }^{\circ}$ of phase shift between

Table 4.13: Preliminary specifications for the 3-D Imaging Scanner. (Courtesy of [Adams, 1995].)

| Parameter | Value Units |
| :---: | :---: |
| Maximum range | $\begin{aligned} & 15 \mathrm{~m} \\ & 50 \mathrm{ft} \end{aligned}$ |
| Minimum range | 0 m |
| LED power (eye-safe) | 1 mW |
| Sweep $\begin{array}{r}\text { (horizontal) } \\ \text { (vertical - "nod") }\end{array}$ | $\begin{aligned} & 360^{\circ} \\ & 130^{\circ} \end{aligned}$ |
| Resolution $\begin{array}{r}\text { (range) } \\ \text { (azimuth) }\end{array}$ | $\begin{gathered} \sim 20 \mathrm{~mm} \\ 0.8 \mathrm{in} \\ 0.072 \text { 。 } \end{gathered}$ |
| Sample rate | 8 kHz |
| Size (diameter $\times$ height) | $\begin{aligned} & 14 \times 27 \mathrm{~cm} \\ & 5.5 \times 10 \mathrm{in} \\ & \text { Not yet determined } \end{aligned}$ |
| Weight | Not yet determined |
| Power | $\begin{array}{r} \text { +12 V @ } 400 \mathrm{~mA} \\ \text {-12 V @ } 20 \mathrm{~mA} \end{array}$ |



Figure 4.30: The 3-D Imaging Scanner consists of a transmitter which illuminates a target and a receiver to detect the returned light. A range estimate from the sensor to the target is then produced. The mechanism shown sweeps the light beam horizontally and vertically. (Courtesy of [Adams, 1995].)
transmitted and received beams. More detailed specifications are listed in Table 4.13.
The 3-D Imaging Scanner is now in an advanced prototype stage and the developer plans to market it in the near future [Adams, 1995].

These are some special design features employed in the 3-D Imaging Scanner:

- Each range estimate is accompanied by a range variance estimate, calibrated from the received light intensity. This quantifies the system's confidence in each range data point.
- Direct "crosstalk" has been removed between transmitter and receiver by employing circuit neutralization and correct grounding techniques.
- A software-based discontinuity detector finds spurious points between edges. Such spurious points are caused by the finite optical beamwidth, produced by the sensor's transmitter.
- The newly developed sensor has a tuned load, low-noise, FET input, bipolar amplifier to remove amplitude and ambient light effects.
- Design emphasis on high-frequency issues helps improve the linearity of the amplitude-modulated continuous-wave (phase measuring) sensor.

Figure 4.31 shows a typical scan result from the 3-D Imaging Scanner. The scan is a pixel plot, where the horizontal axis corresponds to the number of samples recorded in a complete 360 -degree rotation of the sensor head, and the vertical axis corresponds to the number of 2-dimensional scans recorded. In Figure 4.31330 readings were recorded per revolution of the sensor mirror in each horizontal plane, and there were 70 complete revolutions of the mirror. The geometry viewed is "wrap-around geometry," meaning that the vertical pixel set at horizontal coordinate zero is the same as that at horizontal coordinate 330 .

### 4.2.6 Improving Lidar Performance

Unpublished results from [Adams, 1995] show that it is possible to further improve the already good performance of lidar systems. For example, in some commercially available sensors the measured phase shift is not only a function of the sensor-to-target range, but also of the received signal amplitude and ambient light conditions [Vestli et al., 1993]. Adams demonstrates this effect in the sample scan shown in Figure 4.32a. This scan was obtained with the ESP ORS-1 sensor (see Sec. 4.2.3). The solid lines in Figure 4.32 represent the actual environment and each " $\times$ " shows a single range data point. The triangle marks the sensor's position in each case. Note the non-linear behavior of the sensor between points A and B.

Figure 4.32b shows the results from the same ESP sensor, but with the receiver unit redesigned and rebuilt by Adams. Specifically, Adams removed the automatic gain controlled circuit, which is largely responsible for the amplitude-induced range error, and replaced it with four soft limiting amplifiers.

This design approximates the behavior of a logarithmic amplifier. As a result, the weak signals are amplified strongly, while stronger signals remain virtually unamplified. The resulting near-linear signal allows for more accurate phase measurements and hence range determination.


Figure 4.31: Range and intensity scans obtained with Adams' 3-D Imaging Scanner.
a. In the range scan the brightness of each pixel is proportional to the range of the signal received (darker pixels are closer).
b. In the intensity scan the brightness of each pixel is proportional to the amplitude of the signal received.
(Courtesy of [Adams, 1995].)


Figure 4.32: Scanning results obtained from the ESP ORS-1 lidar. The triangles represent the sensor's position; the lines represent a simple plan view of the environment and each small cross represents a single range data point.
a. Some non-linearity can be observed for scans of straight surfaces (e.g., between points $A$ and $B$ ),
b. Scanning result after applying the signal compression circuit from in [Adams and Probert, 1995].
(Reproduced with permission from [Adams and Probert, 1995].)

Note also the spurious data points between edges (e.g., between C and D ). These may be attributed to two potential causes:

- The "ghost-in-the-machine problem," in which crosstalk directly between the transmitter and receiver occurs even when no light is returned. Adams' solution involves circuit neutralization and proper grounding procedures.
- The "beamwidth problem," which is caused by the finite transmitted width of the light beam. This problem shows itself in form of range points lying between the edges of two objects located at different distances from the lidar. To overcome this problem Adams designed a software filter capable of finding and rejecting erroneous range readings. Figure 4.33 shows the lidar map after applying the software filter.


Figure 4.33: Resulting lidar map after applying a software filter.
a. "Good" data that successfully passed the software filter; R and S are "bad" points that "slipped through."
b. Rejected erroneous data points. Point $M$ (and all other square data points) was rejected because the amplitude of the received signal was too low to pass the filter threshold.
(Reproduced with permission from [Adams and Probert, 1995].)

### 4.3 Frequency Modulation

A closely related alternative to the amplitude-modulated phase-shift-measurement ranging scheme is frequency-modulated (FM) radar. This technique involves transmission of a continuous electromagnetic wave modulated by a periodic triangular signal that adjusts the carrier frequency above and below the mean frequency $f_{o}$ as shown in Figure 4.34. The transmitter emits a signal that varies in frequency as a linear function of time:
$f(t)=f_{0}+a t$
where
$a=$ constant
$t$ = elapsed time.
This signal is reflected from a target and arrives at the receiver at time $t+T$.
$T=\frac{2 d}{c}$
where
$T=$ round-trip propagation time
$d=$ distance to target
$c=$ speed of light.


Figure 4.34: The received frequency curve is shifted along the time axis relative to the reference frequency [Everett, 1995].

The received signal is compared with a reference signal taken directly from the transmitter. The received frequency curve will be displaced along the time axis relative to the reference frequency curve by an amount equal to the time required for wave propagation to the target and back. (There might also be a vertical displacement of the received waveform along the frequency axis, due to the Doppler effect.) These two frequencies when combined in the mixer produce a beat frequency $F_{b}$ :
$F_{\mathrm{b}}=f(t)-f(T+t)=a T$
where
$a=$ constant.
This beat frequency is measured and used to calculate the distance to the object:
$d=\frac{F_{b} c}{4 F_{r} F_{d}}$
where
$d=$ range to target
$c=$ speed of light
$F_{b}=$ beat frequency
$F_{r}=$ repetition (modulation) frequency
$F_{d}=$ total FM frequency deviation.
Distance measurement is therefore directly proportional to the difference or beat frequency, and as accurate as the linearity of the frequency variation over the counting interval.

Advances in wavelength control of laser diodes now permit this radar ranging technique to be used with lasers. The frequency or wavelength of a laser diode can be shifted by varying its temperature. Consider an example where the wavelength of an 850 -nanometer laser diode is shifted by 0.05 nanometers in four seconds: the corresponding frequency shift is 5.17 MHz per nanosecond. This laser beam, when reflected from a surface 1 meter away, would produce a beat frequency of 34.5 MHz . The linearity of the frequency shift controls the accuracy of the system; a frequency linearity of one part in 1000 yards yields an accuracy of 1 millimeter.

The frequency-modulation approach has an advantage over the phase-shift-measurement technique in that a single distance measurement is not ambiguous. (Recall phase-shift systems must perform two or more measurements at different modulation frequencies to be unambiguous.) However, frequency modulation has several disadvantages associated with the required linearity and repeatability of the frequency ramp, as well as the coherence of the laser beam in optical systems. As a consequence, most commercially available FMCW ranging systems are radar-based, while laser devices tend to favor TOF and phase-detection methods.

### 4.3.1 Eaton VORAD Vehicle Detection and Driver Alert System

VORAD Technologies [VORAD-1], in joint venture with [VORAD-2], has developed a commercial millimeter-wave FMCW Doppler radar system designed for use on board a motor vehicle [VORAD1]. The Vehicle Collision Warning System employs a $12.7 \times 12.7$-centimeter ( $5 \times 5 \mathrm{in}$ ) antenna/transmitter-receiver package mounted on the front grill of a vehicle to monitor speed of and distance to other traffic or obstacles on the road (see Figure4.35). The flat etched-array antenna radiates approximately 0.5 mW of power at 24.725 GHz directly down the roadway in a narrow directional beam. A GUNN diode is used for the transmitter, while the receiver employs a balancedmixer detector [Woll, 1993].


Figure 4.35: The forward-looking antenna/transmitter/ receiver module is mounted on the front of the vehicle at a height between 50 and 125 cm , while an optional side antenna can be installed as shown for blind-spot protection. (Courtesy of VORAD-2).

The Electronics Control Assembly (see Figure 4.36) located in the passenger compartment or cab can individually distinguish up to 20 moving or stationary objects [Siuru, 1994] out to a maximum range of 106 meters ( 350 ft ); the closest three targets within a prespecified warning distance are tracked at a 30 Hz rate. A Motorola DSP 56001 and an Intel 87 C196 microprocessor calculate range and range-rate information from the RF data and analyze the results in conjunction with vehicle velocity, braking, and steering-angle information. If necessary, the Control Display Unit alerts the operator if warranted of potentially hazardous driving situations with a series of caution lights and audible beeps.
As an optional feature, the Vehicle Collision Warning System offers blind-spot detection along the right-hand side of the vehicle out to 4.5 meters ( 15 ft ). The Side Sensor transmitter employs a dielectric resonant oscillator operating in pulsed-Doppler mode at 10.525 GHz , using a flat etchedarray antenna with a beamwidth of about 70 degrees [Woll, 1993]. The system microprocessor in the Electronics Control Assembly analyzes the signal strength and frequency components from the Side Sensor subsystem in conjunction with vehicle speed and steering inputs, and activates audible and visual LED alerts if a dangerous condition is thought to exist. (Selected specifications are listed in Tab. 4.14.)

Among other features of interest is a recording feature, which stores 20 minutes of the most recent historical data on a removable EEPROM memory card for post-accident reconstruction. This data includes steering, braking, and idle time. Greyhound Bus Lines recently completed installation of the VORAD radar on all of its 2,400 buses [Bulkeley, 1993], and subsequently reported a 25 -year low accident record [Greyhound, 1994]. The entire system weighs just 3 kilograms ( 6.75 lb ), and operates from 12 or 24 VDC with a nominal power consumption of 20 W . An RS-232 digital output is available.

| Parameter | Value Units |
| :--- | ---: |
| Effective range | $0.3-107 \mathrm{~m}$ |
|  | $1-350 \mathrm{ft}$ |
| Accuracy | $3 \%$ |
| Update rate | 30 Hz |
| Host platform speed | $0.5-120 \mathrm{mph}$ |
| Closing rate | $0.25-100 \mathrm{mph}$ |
| Operating frequency | 24.725 GHz |
| RF power | 0.5 mW |
| Beamwidth (horizontal) | $4{ }^{\circ}$ |
| (vertical) | $5{ }^{\circ}$ |
| Size (antenna) | $15 \times 20 \times 3 . \mathrm{cm}$ |
|  | 8 in |
| (electronics unit) | $6 \times 8 \times 1.5$ |
|  | $20 \times 15 \times 12 \mathrm{~cm}$ |
|  | .7 in |
|  | $8 \times 6 \times 5$ |
| Weight (total) | 6.75 lb |
| Power | $12-24 \mathrm{VDC}$ |
|  | 20 W |
| MTBF | $17,000 \mathrm{hr}$ |



Figure 4.36: The electronics control assembly of the Vorad EVT-200 Collision Warning System. (Courtesy of VORAD-2.)

### 4.3.2 Safety First Systems Vehicular Obstacle Detection and Warning System

Safety First Systems, Ltd., Plainview, NY, and General Microwave, Amityville, NY, have teamed to develop and market a 10.525 GHz microwave unit (see Figure 4.37) for use as an automotive blind-spot alert for drivers when backing up or changing lanes [Siuru, 1994]. The narrowband (100kHz ) modified-FMCW technique uses patent-pending phase discrimination augmentation for a $20-$ fold increase in achievable resolution. For example, a conventional FMCW system operating at 10.525 GHz with a 50 MHz bandwidth is limited to a best-case range resolution of approximately 3 meters ( 10 ft ), while the improved approach can resolve distance to within 18 centimeters ( 0.6 ft ) out to 12 meters ( 40 ft ) [SFS]. Even greater accuracy and maximum ranges (i.e., $48 \mathrm{~m}-160 \mathrm{ft}$ ) are possible with additional signal processing.


Figure 4.37: Safety First/General Microwave Corporation's Collision Avoidance Radar, Model 1707A with two antennas. (Courtesy of Safety First/General Microwave Corp.)

A prototype of the system delivered to Chrysler Corporation uses conformal bistatic microstrip antennae mounted on the rear side panels and rear bumper of a minivan, and can detect both stationary and moving objects within the coverage patterns shown in Figure 4.38. Coarse range information about reflecting targets is represented in four discrete range bins with individual TTL output lines: 0 to 1.83 meters ( 0 to 6 ft ), 1.83 to 3.35 meters ( 6 to 11 ft ), 3.35 to 6.1 meters ( 11 to $20 \mathrm{ft})$, and $>6.1 \mathrm{~m}(20 \mathrm{ft})$. Average radiated power is about $50 \mu \mathrm{~W}$ with a three-percent duty cycle, effectively eliminating adjacent-system interference. The system requires 1.5 A from a single 9 to 18 VDC supply.


Figure 4.38: The Vehicular Obstacle Detection and Warning System employs a modified FMCW ranging technique for blind-spot detection when backing up or changing lanes. (Courtesy of Safety First Systems, Ltd.)

## Part II <br> Systems and Methods for Mobile Robot Positioning



Tech-Team leaders Chuck Cohen, Frank Koss, Mark Huber, and David Kortenkamp (left to right) fine-tune CARMEL in preparation of the 1992 Mobile Robot Competition in San Jose, CA. The efforts paid off: despite its age, CARMEL proved to be the most agile among the contestants, winning first place honors for the University of Michigan.

## Chapter 5 Odometry and Other Dead-Reckoning Methods

Odometry is the most widely used navigation method for mobile robot positioning. It is well known that odometry provides good short-term accuracy, is inexpensive, and allows very high sampling rates. However, the fundamental idea of odometry is the integration of incremental motion information over time, which leads inevitably to the accumulation of errors. Particularly, the accumulation of orientation errors will cause large position errors which increase proportionally with the distance traveled by the robot. Despite these limitations, most researchers agree that odometry is an important part of a robot navigation system and that navigation tasks will be simplified if odometric accuracy can be improved. Odometry is used in almost all mobile robots, for various reasons:

- Odometry data can be fused with absolute position measurements to provide better and more reliable position estimation [Cox, 1991; Hollingum, 1991; Byrne et al., 1992; Chenavier and Crowley, 1992; Evans, 1994].
- Odometry can be used in between absolute position updates with landmarks. Given a required positioning accuracy, increased accuracy in odometry allows for less frequent absolute position updates. As a result, fewer landmarks are needed for a given travel distance.
- Many mapping and landmark matching algorithms (for example: [Gonzalez et al., 1992; Chenavier and Crowley, 1992]) assume that the robot can maintain its position well enough to allow the robot to look for landmarks in a limited area and to match features in that limited area to achieve short processing time and to improve matching correctness [Cox, 1991].
- In some cases, odometry is the only navigation information available; for example: when no external reference is available, when circumstances preclude the placing or selection of landmarks in the environment, or when another sensor subsystem fails to provide usable data.


### 5.1 Systematic and Non-Systematic Odometry Errors

Odometry is based on simple equations (see Chapt. 1) that are easily implemented and that utilize data from inexpensive incremental wheel encoders. However, odometry is also based on the assumption that wheel revolutions can be translated into linear displacement relative to the floor. This assumption is only of limited validity. One extreme example is wheel slippage: if one wheel was to slip on, say, an oil spill, then the associated encoder would register wheel revolutions even though these revolutions would not correspond to a linear displacement of the wheel.

Along with the extreme case of total slippage, there are several other more subtle reasons for inaccuracies in the translation of wheel encoder readings into linear motion. All of these error sources fit into one of two categories: systematic errors and non-systematic errors.

## Systematic Errors

- Unequal wheel diameters.
- Average of actual wheel diameters differs from nominal wheel diameter.
- Actual wheelbase differs from nominal wheelbase.
- Misalignment of wheels.
- Finite encoder resolution.
- Finite encoder sampling rate.


## Non-Systematic Errors

- Travel over uneven floors.
- Travel over unexpected objects on the floor.
- Wheel-slippage due to:
- slippery floors.
- overacceleration.
- fast turning (skidding).
- external forces (interaction with external bodies).
- internal forces (castor wheels).
- non-point wheel contact with the floor.

The clear distinction between systematic and non-systematic errors is of great importance for the effective reduction of odometry errors. For example, systematic errors are particularly grave because they accumulate constantly. On most smooth indoor surfaces systematic errors contribute much more to odometry errors than non-systematic errors. However, on rough surfaces with significant irregularities, non-systematic errors are dominant. The problem with non-systematic errors is that they may appear unexpectedly (for example, when the robot traverses an unexpected object on the ground), and they can cause large position errors. Typically, when a mobile robot system is installed with a hybrid odometry/landmark navigation system, the frequency of the landmarks is determined empirically and is based on the worst-case systematic errors. Such systems are likely to fail when one or more large non-systematic errors occur.

It is noteworthy that many researchers develop algorithms that estimate the position uncertainty of a dead-reckoning robot (e.g., [Tonouchi et al., 1994; Komoriya and Oyama, 1994].) With this approach each computed robot position is surrounded by a characteristic "error ellipse," which indicates a region of uncertainty for the robot's actual position (see Figure 5.1) [Tonouchi et al., 1994; Adams et al., 1994]. Typically, these ellipses grow with travel distance, until an absolute position measurement reduces the growing uncertainty and thereby "resets" the size of the error ellipse. These error estimation techniques must rely on error estimation parameters derived from observations of the vehicle's dead-reckoning performance. Clearly, these parameters can take into account only systematic errors, because the magnitude of non-systematic errors is unpredictable.


Figure 5.1: Growing "error ellipses" indicate the growing position uncertainty with odometry. (Adapted from [Tonouchi et al., 1994].)

### 5.2 Measurement of Odometry Errors

One important but rarely addressed difficulty in mobile robotics is the quantitative measurement of odometry errors. Lack of well-defined measuring procedures for the quantification of odometry errors results in the poor calibration of mobile platforms and incomparable reports on odometric accuracy in scientific communications. To overcome this problem Borenstein and Feng [1995a; 1995c] developed methods for quantitatively measuring systematic odometry errors and, to a limited degree, non-systematic odometry errors. These methods rely on a simplified error model, in which two of the systematic errors are considered to be dominant, namely:

- the error due to unequal wheel diameters, defined as

$$
\begin{equation*}
E_{\mathrm{d}}=D_{\mathrm{R}} / D_{\mathrm{L}} \tag{5.1}
\end{equation*}
$$

where $D_{\mathrm{R}}$ and $D_{\mathrm{L}}$ are the actual wheel diameters of the right and left wheel, respectively.

- The error due to uncertainty about the effective wheelbase, defined as

$$
\begin{equation*}
E_{\mathrm{b}}=b_{\text {actual }} / b_{\text {nominal }} \tag{5.2}
\end{equation*}
$$

where $b$ is the wheelbase of the vehicle.

### 5.2.1 Measurement of Systematic Odometry Errors

To better understand the motivation for Borenstein and Feng's method (discussed in Sec. 5.2.1.2), it will be helpful to investigate a related method first. This related method, described in Section 5.2.1.1, is intuitive and widely used (e.g., [Borenstein and Koren, 1987; Cybermotion, 1988; Komoriya and Oyama, 1994; Russell, 1995], but it is a fundamentally unsuitable benchmark test for differential-drive mobile robots.

### 5.2.1.1 The Unidirectional Square-Path Test - A Bad Measure for Odometric Accuracy

Figure 5.2 a shows a $4 \times 4$ meter unidirectional square path. The robot starts out at a position $x_{0}$, $y_{0}, \theta_{0}$, which is labeled START. The starting area should be located near the corner of two perpendicular walls. The walls serve as a fixed reference before and after the run: measuring the distance between three specific points on the robot and the walls allows accurate determination of the robot's absolute position and orientation.

To conduct the test, the robot must be programmed to traverse the four legs of the square path. The path will return the vehicle to the starting area but, because of odometry and controller errors, not precisely to the starting position. Since this test aims at determining odometry errors and not controller errors, the vehicle does not need to be programmed to return to its starting position precisely - returning approximately to the starting area is sufficient. Upon completion of the square path, the experimenter again measures the absolute position of the vehicle, using the fixed walls as a reference. These absolute measurements are then compared to the position and orientation of the vehicle as computed from odometry data. The result is a set of return position errors caused by odometry and denoted $\epsilon x, \epsilon y$, and $\epsilon \theta$.

$$
\begin{align*}
& \epsilon x=x_{a b s}-x_{c a l c} \\
& \epsilon y=y_{a b s}-y_{\text {calc }}  \tag{5.3}\\
& \epsilon \theta=\theta_{a b s}-\theta_{\text {calc }}
\end{align*}
$$

where

$$
\begin{aligned}
\epsilon x, \epsilon y, \epsilon \theta= & \text { position and orientation er- } \\
& \text { rors due to odometry } \\
x_{a b s}, y_{a b s}, \theta_{a b s}= & \text { absolute position and orienta- } \\
& \text { tion of the robot } \\
x_{\text {calc }}, y_{\text {calc }}, \theta_{\text {calc }}= & \text { position and orientation of } \\
& \text { the robot as computed from } \\
& \text { odo- } \\
& \text { metry. }
\end{aligned}
$$

The path shown in Figure 5.2a comprises of four straight-line segments and four pure rotations about the robot's centerpoint, at the corners of the square. The robot's end position shown in Figure 5.2a visualizes the odometry error.

While analyzing the results of this experiment, the experimenter may draw two different conclusions: The odometry error is the result of unequal wheel diameters, $E_{d}$, as shown by the slightly curved trajectory in Figure 5.2b (dotted line). Or, the odometry error is the result of uncertainty about the wheelbase, $E_{b}$. In the example of Figure $5.2 \mathrm{~b}, E_{b}$ caused the robot to turn 87 degrees instead of the desired 90 degrees (dashed trajectory in Figure 5.2b).

As one can see in Figure 5.2b, either one of these two cases could yield approximately the same position error. The fact that two different error mechanisms might result in the same overall error may lead an experimenter toward a serious mistake: correcting only one of the two error sources in software. This mistake is so serious because it will yield apparently "excellent" results, as shown in the example in Figure 5.3. In this example, the experimenter began "improving" performance by adjusting the wheelbase $b$ in the control software. According to the dead-reckoning equations for differential-drive vehicles (see Eq. (1.5) in Sec. 1.3.1), the experimenter needs only to increase the value of $b$ to make the robot turn more in each nominal 90 -degree turn. In doing so, the experimenter will soon have adjusted $b$ to the seemingly "ideal" value that will cause the robot to turn 93 degrees, thereby effectively compensating for the 3 -degree orientation error introduced by each slightly curved (but nominally straight) leg of the square path.

One should note that another popular test path, the "figure-8" path [Tsumura et al., 1981; Borenstein and Koren, 1985; Cox, 1991] can be shown to have the same shortcomings as the uni-directional square path.

### 5.2.1.2 The Bidirectional Square-Path Experiment

The detailed example of the preceding section illustrates that the unidirectional square path experiment is unsuitable for testing odometry performance in differential-drive platforms, because it can easily conceal two mutually compensating odometry errors. To overcome this problem, Borenstein and Feng [1995a; 1995c] introduced the bidirectional square-path experiment, called University of Michigan Benchmark (UMBmark). UMBmark requires that the square path experiment be performed in both clockwise and counterclockwise direction. Figure 5.4 shows that the concealed dual error from the example in Figure 5.3 becomes clearly visible when the square path is performed in the opposite direction. This is so because the two dominant systematic errors, which may compensate for each other when run in only one direction, add up to each other and increase the overall error when run in the opposite direction.

The result of the bidirectional squarepath experiment might look similar to the one shown in Figure 5.5, which presents actual experimental results with an off-theshelf TRC LabMate robot [TRC] carrying an evenly distributed load. In this experi ment the robot was programmed to follow a $4 \times 4$ meter square path, starting at $(0,0)$. The stopping positions for five runs each in clockwise (cw) and counterclockwise (ccw) directions are shown in Figure 5.5. Note that Figure 5.5 is an enlarged view of the target area. The results of Figure 5.5 can be interpreted as follows:


Figure 5.3: The effect of the two dominant systematic dead-reckoning errors $E_{b}$ and $E_{d}$. Note how both errors may cancel each other out when the test is performed in only one direction.


Figure 5.4: The effect of the two dominant systematic odometry errors $E_{b}$ and $E_{d}$ : when the square path is performed in the opposite direction one may find that the errors add up.

- The stopping positions after cw and ccw runs are clustered in two distinct areas.
- The distribution within the cw and ccw clusters are the result of non-systematic errors, such as those mentioned in Section 5.1. However, Figure 5.5 shows that in an uncalibrated vehicle, traveling over a reasonably smooth concrete floor, the contribution of systematic errors to the total odometry error can be notably larger than the contribution of non-systematic errors.

After conducting the UMBmark experiment, one may wish to derive a single numeric value that expresses the odometric accuracy (with respect to systematic errors) of the tested vehicle. In order to minimize the effect of non-systematic errors, it has been suggested [Komoriya and Oyama, 1994; Borenstein and Feng, 1995c] to consider the center of gravity of each cluster as representative for the systematic odometry errors in the cw and ccw directions.

The coordinates of the two centers of gravity are computed from the results of Equation (5.3) as

$$
\begin{aligned}
& x_{c . g ., c w / c c w}=\frac{1}{n} \sum_{i=1}^{n} \epsilon x_{i, c w / c c w} \\
& y_{c . g ., c w / c c w}=\frac{1}{n} \sum_{i=1}^{n} \epsilon y_{i, c w / c c w}
\end{aligned}
$$

where $n=5$ is the number of runs in each direction.

The absolute offsets of the two centers of gravity from the origin are denoted $r_{\text {c.g., cw }}$ and $r_{\text {c.g., ccw }}$ (see Fig. 5.5) and are given by

$$
\begin{equation*}
r_{c . g, c w}=\sqrt{\left(x_{c . g, c w}\right)^{2}+\left(y_{c . g, c w}\right)^{2}} \tag{5.5a}
\end{equation*}
$$

and

$$
\begin{equation*}
r_{c . g ., c c w}=\sqrt{\left(x_{c . g ., c c w}\right)^{2}+\left(y_{c . g, c c w}\right)^{2}} . \tag{5.5b}
\end{equation*}
$$



Figure 5.5: Typical results from running UMBmark (a square path run in both cw and ccw directions) with an uncalibrated vehicle.

Finally, the larger value among $r_{\mathrm{c} . \mathrm{g}, \mathrm{cw}}$ and $r_{\mathrm{c} . \mathrm{g}, \text {, cow }}$ is defined as the "measure of odometric accuracy for systematic errors":
$E_{\mathrm{max}, \mathrm{syst}}=\max \left(r_{\mathrm{c} . \mathrm{g}, \mathrm{cw}} ; r_{\mathrm{c} . \mathrm{g}, \mathrm{ccw}}\right)$.
The reason for not using the average of the two centers of gravity $r_{\mathrm{c} . \mathrm{g}, \mathrm{cw}}$ and $r_{\mathrm{c}, \mathrm{g}, \mathrm{ccw}}$ is that for practical applications one needs to worry about the largest possible odometry error. One should also note that the final orientation error $\epsilon \theta$ is not considered explicitly in the expression for $E_{\text {max,syst }}$. This
is because all systematic orientation errors are implied by the final position errors. In other words, since the square path has fixed-length sides, systematic orientation errors translate directly into position errors.

### 5.2.2 Measurement of Non-Systematic Errors

Some limited information about a vehicle's susceptibility to non-systematic errors can be derived from the spread of the return position errors that was shown in Figure 5.5. When running the UMBmark procedure on smooth floors (e.g., a concrete floor without noticeable bumps or cracks), an indication of the magnitude of the non-systematic errors can be obtained from computing the estimated standard deviation $\sigma$. However, Borenstein and Feng [1994] caution that there is only limited value to knowing $\sigma$, since $\sigma$ reflects only on the interaction between the vehicle and a certain floor. Furthermore, it can be shown that from comparing $\sigma$ from two different robots (even if they traveled on the same floor), one cannot necessarily conclude that the robots with the larger $\sigma$ showed higher susceptibility to non-systematic errors.

In real applications it is imperative that the largest possible disturbance be determined and used in testing. For example, the estimated standard deviation of the test in Figure 5.5 gives no indication at all as to what error one should expect if one wheel of the robot inadvertently traversed a large bump or crack in the floor. For the above reasons it is difficult (perhaps impossible) to design a generally applicable quantitative test procedure for non-systematic errors. However, Borenstein [1994] proposed an easily reproducible test that would allow comparing the susceptibility to nonsystematic errors of different vehicles. This test, called the extended UMBmark, uses the same bidirectional square path as UMBmark but, in addition, introduces artificial bumps. Artificial bumps are introduced by means of a common, round, electrical household-type cable (such as the ones used with 15 A six-outlet power strips). Such a cable has a diameter of about 9 to 10 millimeters. Its rounded shape and plastic coating allow even smaller robots to traverse it without too much physical impact. In the proposed extended UMBmark test the cable is placed 10 times under one of the robot's wheels, during motion. In order to provide better repeatability for this test and to avoid mutually compensating errors, Borenstein and Feng [1994] suggest that these 10 bumps be introduced as evenly as possible. The bumps should also be introduced during the first straight segment of the square path, and always under the wheel that faces the inside of the square. It can be shown [Borenstein, 1994b] that the most noticeable effect of each bump is a fixed orientation error in the direction of the wheel that encountered the bump. In the TRC LabMate, for example, the orientation error resulting from a bump of height $h=10 \mathrm{~mm}$ is roughly $\Delta \theta=0.44^{\circ}$ [Borenstein, 1994b].

Borenstein and Feng [1994] proceed to discuss which measurable parameter would be the most useful for expressing the vehicle's susceptibility to non-systematic errors. Consider, for example, Path A and Path B in Figure 5.6. If the 10 bumps required by the extended UMBmark test were concentrated at the beginning of the first straight leg (as shown in exaggeration in Path A), then the return position error would be very small. Conversely, if the 10 bumps were concentrated toward the end of the first straight leg (Path B in Figure 5.6), then the return position error would be larger. Because of this sensitivity of the return position errors to the exact location of the bumps it is not a good idea to use the return position error as an indicator for a robot's susceptibility to nonsystematic errors. Instead, the return orientation error $\epsilon \theta$ should be used. Although it is more difficult to measure small angles, measurement of $\epsilon \theta$ is a more consistent quantitative indicator for
comparing the performance of different robots. Thus, one can measure and express the susceptibility of a vehicle to non-systematic errors in terms of its average absolute orientation error defined as
$\epsilon \theta_{\text {avrg }}^{\text {nonsys }}=\frac{1}{n} \sum_{i=1}^{n}\left|\epsilon \theta_{i, c w}^{\text {nonsys }}-\epsilon \theta_{\text {avrg,cw }}^{\text {sys }}\right|+\frac{1}{n} \sum_{i=1}^{n}\left|\epsilon \theta_{i, c c w}^{\text {nonss }}-\epsilon \theta_{\text {avrg,cww }}^{\text {sys }}\right|$
where $n=5$ is the number of experiments in cw or ccw direction, superscripts "sys" and "nonsys" indicate a result obtained from either the regular UMBmark test (for systematic errors) or from the extended UMBmark test (for non-systematic errors). Note that Equation (5.7) improves on the accuracy in identifying non-systematic errors by removing the systematic bias of the vehicle, given by

$$
\epsilon \theta_{\text {avrg,cw }}^{s y s}=\frac{1}{n} \sum_{i=1}^{n} \epsilon \theta_{i, c w}^{s y s}
$$

and

$$
\epsilon \theta_{\text {avrg,ccw }}^{s y s}=\frac{1}{n_{i=1}^{n}} \sum_{i, c c w}^{s y s}
$$

Also note that the arguments inside the Sigmas in Equation (5.7) are absolute values of the bias-free return orientation errors. This is because one would want to avoid the case in which two return orientation errors of opposite sign cancel each other out. For example, if in one run $\epsilon \theta=1^{\circ}$ and in the next run $\epsilon \theta=-1^{\circ}$, then one should not conclude that $\epsilon \theta_{\text {avrg }}^{\text {nonsys }}=0$. Using the average absolute return error as computed in Equation (5.7) would correctly compute $\epsilon \theta_{\text {avrg }}^{\text {nonss }}=.1$ By contrast, in Equation (5.8) the actual arithmetic average is computed to identify a fixed bias.


Figure 5.6: The return position of the extended UMBmark test is sensitive to the exact location where the 10 bumps were placed. The return orientation is not.

### 5.3 Reduction of Odometry Errors

The accuracy of odometry in commercial mobile platforms depends to some degree on their kinematic design and on certain critical dimensions. Here are some of the design-specific considerations that affect dead-reckoning accuracy:

Vehicles with a small wheelbase are more prone to orientation errors than vehicles with a larger wheelbase. For example, the differential drive LabMate robot from TRC has a relatively small wheelbase of 340 millimeters ( 13.4 in ). As a result, Gourley and Trivedi [1994], suggest that
odometry with the LabMate be limited to about 10 meters ( 33 ft ), before a new "reset" becomes necessary.

- Vehicles with castor wheels that bear a significant portion of the overall weight are likely to induce slippage when reversing direction (the "shopping cart effect"). Conversely, if the castor wheels bear only a small portion of the overall weight, then slippage will not occur when reversing direction [Borenstein and Koren, 1985].
- It is widely known that, ideally, wheels used for odometry should be "knife-edge" thin and not compressible. The ideal wheel would be made of aluminum with a thin layer of rubber for better traction. In practice, this design is not feasible for all but the most lightweight vehicles, because the odometry wheels are usually also load-bearing drive wheels, which require a somewhat larger ground contact surface.
- Typically the synchro-drive design (see Sec. 1.3.4) provides better odometric accuracy than differential-drive vehicles. This is especially true when traveling over floor irregularities: arbitrary irregularities will affect only one wheel at a time. Thus, since the two other drive wheels stay in contact with the ground, they provide more traction and force the affected wheel to slip. Therefore, overall distance traveled will be reflected properly by the amount of travel indicated by odometry.

Other attempts at improving odometric accuracy are based on more detailed modeling. For example, Larsson et al. [1994] used circular segments to replace the linear segments in each sampling period. The benefits of this approach are relatively small. Boyden and Velinsky [1994] compared (in simulations) conventional odometric techniques, based on kinematics only, to solutions based on the dynamics of the vehicle. They presented simulation results to show that for both differentially and conventionally steered wheeled mobile robots, the kinematic model was accurate only at slower speeds up to $0.3 \mathrm{~m} / \mathrm{s}$ when performing a tight turn. This result agrees with experimental observations, which suggest that errors due to wheel slippage can be reduced to some degree by limiting the vehicle's speed during turning, and by limiting accelerations.

### 5.3.1 Reduction of Systematic Odometry Errors

In this section we present specific methods for reducing systematic odometry errors. When applied individually or in combination, these measures can improve odometric accuracy by orders of magnitude.

### 5.3.1.1 Auxiliary Wheels and Basic Encoder Trailer

It is generally possible to improve odometric accuracy by adding a pair of "knife-edge," non-loadbearing encoder wheels, as shown conceptually in Figure 5.7. Since these wheels are not used for transmitting power, they can be made to be very thin and with only a thin layer of rubber as a tire. Such a design is feasible for differential-drive, tricycle-drive, and Ackerman vehicles.

Hongo et al. [1987] had built such a set of encoder wheels, to improve the accuracy of a large differential-drive mobile robot weighing 350 kilograms ( 770 lb ). Hongo et al. report that, after careful calibration, their vehicle had a position error of less than 200 millimeters ( 8 in ) for a travel distance of 50 meters ( 164 ft ). The ground surface on which this experiment was carried out was a "well-paved" road.

### 5.3.1.2 The Basic Encoder Trailer

An alternative approach is the use of a trailer with two encoder wheels [Fan et al., 1994; 1995]. Such an encoder trailer was recently built and tested at the University of Michigan (see Figure 5.8). This encoder trailer was designed to be attached to a Remotec Andros $V$ tracked vehicle [REMOTEC]. As was explained in Section 1.3, it is virtually impossible to use odometry with tracked vehicles, because of the large amount of slippage between the tracks and the floor during turning. The idea of the encoder trailer is


Figure 5.7: Conceptual drawing of a set of encoder wheels for a differential drive vehicle. to perform odometry whenever the ground characteristics allow one to do so. Then, when the Andros has to move over small obstacles, stairs, or otherwise uneven ground, the encoder trailer would be raised. The argument for this part-time deployment of the encoder trailer is that in many applications the robot may travel mostly on reasonably smooth concrete floors and that it would thus benefit most of the time from the encoder trailer's odometry.

### 5.3.1.3 Systematic Calibration

Another approach to improving odometric accuracy without any additional devices or sensors is based on the careful calibration of a mobile robot. As was explained in Section 5.1, systematic errors are inherent properties of each individual robot. They change very slowly as the result of wear or of different load distributions. Thus, these errors remain almost constant over extended periods of time [Tsumura et al., 1981]. One way to reduce such errors is vehiclespecific calibration. However, calibration is difficult because even minute deviations in the geometry of the vehicle or its parts (e.g., a change in wheel diameter due to a different load distribution) may cause substantial odometry errors.

Borenstein and Feng [1995a; 1995b] have developed a systematic procedure for the measurement and correction of odometry errors. This method requires that the UMBmark procedure, described in Section 5.2.1, be run with at least five runs each in cw and ccw direction. Borenstein and Feng define two new error characteristics that are meaningful only in the context of the UMBmark test. These characteristics, called Type A and Type B, represent odometry errors in orientation. A Type A is defined as an orientation error that reduces (or increases) the total amount of rotation of the robot during the square-path experiment in both $\boldsymbol{c w}$ and ccw direction. By contrast, Type B is defined as an orientation error that reduces (or increases) the total amount of rotation of the robot during the square-path experiment in one direction, but
increases (or reduces) the amount of rotation when going in the other direction. Examples for Type A and Type B errors are shown in Figure 5.9.


Figure 5.9: Type $A$ and Type $B$ errors in the $c c w$ and $c w$ directions. a. Type $A$ errors are caused only by the wheelbase error $E_{b}$. b. Type B errors are caused only by unequal wheel diameters $\left(E_{d}\right)$.

Figure 5.9a shows a case where the robot turned four times for a nominal amount of 90 degrees per turn. However, because the actual wheelbase of the vehicle was larger than the nominal value, the vehicle actually turned only 85 degrees in each corner of the square path. In the example of Figure 5.9 the robot actually turned only $\theta_{\text {total }}=4 \times 85^{\circ}=340^{\circ}$, instead of the desired $\theta_{\text {nominal }}=360^{\circ}$. One can thus observe that in both the cw and the ccw experiment the robot ends up turning less than the desired amount, i.e.,

$$
\left|\theta_{\text {total, cw }}\right|<\mid \theta_{\text {nominal }} \text { and }\left|\theta_{\text {total, ccw }}\right|<\left|\theta_{\text {nominal }}\right| \text {. }
$$

Hence, the orientation error is of Type A.
In Figure 5.9b the trajectory of a robot with unequal wheel diameters is shown. This error expresses itself in a curved path that adds to the overall orientation at the end of the run in ccw direction, but it reduces the overall rotation in the ccw direction, i.e.,

$$
\left|\theta_{\text {total, ccw }}\right|>\left|\theta_{\text {nominal }} \boldsymbol{b u t}\right| \theta_{\text {total, cw }}|<| \theta_{\text {nominal }} .
$$

Thus, the orientation error in Figure 5.9 b is of Type B.
In an actual run Type A and Type B errors will of course occur together. The problem is therefore how to distinguish between Type A and Type B errors and how to compute correction factors for these errors from the measured final position errors of the robot in the UMBmark test. This question will be addressed next.

Figure 5.9a shows the contribution of Type A errors. We recall that Type A errors are caused mostly by $\mathrm{E}_{\mathrm{b}}$. We also recall that Type A errors cause too much or too little turning at the corners of the square path. The (unknown) amount of erroneous rotation in each nominal 90-degree turn is denoted as $\alpha$ and measured in [rad].

Figure 5.9 b shows the contribution of Type B errors. We recall that Type B errors are caused mostly by the ratio between wheel diameters $\mathrm{E}_{\mathrm{d}}$. We also recall that Type B errors cause a slightly curved path instead of a straight one during the four straight legs of the square path. Because of the curved motion, the robot will have gained an incremental orientation error, denoted $\beta$, at the end of each straight leg.

We omit here the derivation of expressions for $\alpha$ and $\beta$, which can be found from simple geometric relations in Figure 5.9 (see [Borenstein and Feng, 1995a] for a detailed derivation). Here we just present the results:

$$
\begin{equation*}
\alpha=\frac{\mathrm{X}_{\mathrm{c} . \mathrm{g}, \mathrm{cw}}+\mathrm{X}_{\mathrm{c} . \mathrm{g}, \mathrm{ccw}}}{-4 \mathrm{~L}} \frac{180^{\circ}}{\pi} \tag{5.9}
\end{equation*}
$$

solves for $\alpha$ in $\left[{ }^{\circ}\right]$ and

$$
\begin{equation*}
\beta=\frac{\mathrm{x}_{\mathrm{c} . \mathrm{g}, \mathrm{cw}}-\mathrm{x}_{\mathrm{c} . \mathrm{g}, \mathrm{ccw}}}{-4 \mathrm{~L}} \frac{180^{\circ}}{\pi} \tag{5.10}
\end{equation*}
$$

solves for $\beta$ in $\left[{ }^{\circ}\right]$.
Using simple geometric relations, the radius of curvature $R$ of the curved path of Figure 5.9b can be found as

$$
\begin{equation*}
\mathrm{R}=\frac{\mathrm{L} / 2}{\sin \beta / 2} \tag{5.11}
\end{equation*}
$$

Once the radius R is computed, it is easy to determine the ratio between the two wheel diameters that caused the robot to travel on a curved, instead of a straight path

$$
\begin{equation*}
\mathrm{E}_{\mathrm{d}}=\frac{\mathrm{D}_{\mathrm{R}}}{\mathrm{D}_{\mathrm{L}}}=\frac{\mathrm{R}+\mathrm{b} / 2}{\mathrm{R}-\mathrm{b} / 2} . \tag{5.12}
\end{equation*}
$$

Similarly one can compute the wheelbase error $\mathrm{E}_{\mathrm{b}}$. Since the wheelbase b is directly proportional to the actual amount of rotation, one can use the proportion:
$\frac{b_{\text {actual }}}{90^{\circ}}=\frac{b_{\text {nominal }}}{90^{\circ}-c}$
so that

$$
\begin{equation*}
b_{\text {actual }}=\frac{90^{\circ}}{90^{\circ}-\alpha} b_{\text {nominal }} \tag{5.14}
\end{equation*}
$$

where, per definition of Equation (5.2)

$$
\begin{equation*}
E_{b}=\frac{90^{\circ}}{90^{\circ}-c} . \tag{5.15}
\end{equation*}
$$

Once $E_{\mathrm{b}}$ and $E_{\mathrm{d}}$ are computed, it is straightforward to use their values as compensation factors in the controller software [see Borenstein and Feng, 1995a; 1995b]. The result is a 10- to 20-fold reduction in systematic errors.

Figure 5.10 shows the result of a typical calibration session. $D_{\mathrm{R}}$ and $D_{\mathrm{L}}$ are the effective wheel diameters, and $b$ is the effective wheelbase.


Figure 5.10: Position rrors after completion of the bidirectional square-path experiment (4 x 4 m ).
Before calibration: $\mathrm{b}=340.00 \mathrm{~mm}, D_{\mathrm{R}} / D_{\mathrm{L}}=1.00000$.
After calibration: $\mathrm{b}=336.17, D_{\mathrm{R}} / D_{\mathrm{L}}=1.00084$.

This calibration procedure can be performed with nothing more than an ordinary tape measure. It takes about two hours to run the complete calibration procedure and measure the individual return errors with a tape measure.

### 5.3.2 Reducing Non-Systematic Odometry Errors

This section introduces methods for the reduction of non-systematic odometry errors. The methods discussed in Section 5.3.2.2 may at first confuse the reader because they were implemented on the somewhat complex experimental platform described in Section 1.3.7. However, the methods of Section 5.3.2.2 can be applied to many other kinematic configurations, and efforts in that direction are subject of currently ongoing research at the University of Michigan.

### 5.3.2.1 Mutual Referencing

Sugiyama [1993] proposed to use two robots that could measure their positions mutually. When one of the robots moves to another place, the other remains still, observes the motion, and determines the first robot's new position. In other words, at any time one robot localizes itself with reference to a fixed object: the standing robot. However, this stop and go approach limits the efficiency of the robots.

### 5.3.2.2 Internal Position Error Correction

A unique way for reducing odometry errors even further is Internal Position Error Correction (IPEC). With this approach two mobile robots mutually correct their odometry errors. However, unlike the approach described in Section 5.3.2.1, the IPEC method works while both robots are in continuous, fast motion [Borenstein, 1994a]. To implement this method, it is required that both robots can measure their relative distance and bearing continuously and accurately. Coincidentally, the MDOF vehicle with compliant linkage (described in Sec. 1.3.7) offers exactly these features, and the IPEC method was therefore implemented and demonstrated on that MDOF vehicle. This implementation is named Compliant Linkage Autonomous Platform with Position Error Recovery (CLAPPER).

The CLAPPER's compliant linkage instrumentation was illustrated in Chapter 1, Figure 1.15. This setup provides real-time feedback on the relative position and orientation of the two trucks. An absolute encoder at each end measures the rotation of each truck (with respect to the linkage) with a resolution of 0.3 degrees, while a linear encoder is used to measure the separation distance to within 5 millimeters ( 0.2 in ). Each truck computes its own dead-reckoned position and heading in conventional fashion, based on displacement and velocity information derived from its left and right drive-wheel encoders. By examining the perceived odometry solutions of the two robot platforms in conjunction with their known relative orientations, the CLAPPER system can detect and significantly reduce heading errors for both trucks (see video clip in [Borenstein, 1995V].)

The principle of operation is based on the concept of error growth rate presented by Borenstein [1994a, 1995a], who makes a distinction between "fast-growing" and "slow-growing" odometry errors. For example, when a differentially steered robot traverses a floor irregularity it will immediately experience an appreciable orientation error (i.e., a fast-growing error). The associated lateral displacement error, however, is initially very small (i.e., a slow-growing error), but grows in an unbounded fashion as a consequence of the orientation error. The internal error correction algorithm performs relative position measurements with a sufficiently fast update rate ( 20 ms ) to
allow each truck to detect fast-growing errors in orientation, while relying on the fact that the lateral position errors accrued by both platforms during the sampling interval were small.

Figure 5.11 explains how this method works. After traversing a bump Truck A's orientation will change (a fact unknown to Truck A's odometry computation). Truck A is therefore expecting to "see" Truck B along the extension of line $L_{e}$. However, because of the physically incurred rotation of Truck A, the absolute encoder on truck A will report that truck B is now actually seen along line $L_{\mathrm{m}}$. The angular difference between $L_{e}$ and $L_{\mathrm{m}}$ is the thus measured odometry orientation error of Truck A, which can be corrected immediately. One should note that even if Truck B encountered a bump at the same time, the resulting rotation of Truck B would not affect the orientation error measurement.

The compliant linkage in essence forms a pseudo-stable heading reference in world coordinates, its own orientation being dictated solely by the relative translations of its end points, which in turn are affected only by the lateral displacements of the two trucks. Since the lateral displacements are slow growing, the linkage rotates only a very small amount between encoder samples. The fast-growing azimuthal disturbances of the trucks, on the other hand, are not coupled through the rotational joints to the linkage, thus allowing the rotary encoders to detect and quantify the instantaneous orientation errors of the trucks, even when both are in motion. Borenstein [1994a; 1995a] provides a more complete description of this innovative concept and reports experimental results indicating improved odometry performance of up to two orders of magnitude over conventional mobile robots.

It should be noted that the rather complex kinematic design of the MDOF vehicle is not necessary to implement the IPEC error correction method. Rather, the MDOF vehicle happened to be available at the time and allowed the University of Michigan researchers to implement and verify the validity of the IPEC approach. Currently, efforts are under way to implement the IPEC method on a tractor-trailer assembly, called "Smart Encoder Trailer" (SET), which is shown in Figure 5.12. The principle of operation is


Figure 5.11: After traversing a bump, the resulting change of orientation of Truck A can be measured relative to Truck B.


Figure 5.12: The University of Michigan's "Smart Encoder Trailer" (SET) is currently being instrumented to allow the implementation of the IPEC error correction method explained in Section 5.3.2.2. (Courtesy of The University of Michigan.)
illustrated in Figure 5.13. Simulation results, indicating the feasibility of implementing the IPEC method on a tractor-trailer assembly, were presented in [Borenstein, 1994b].

### 5.4 Inertial Navigation

An alternative method for enhancing dead reckoning is inertial navigation, initially developed for deployment on aircraft. The technology was quickly adapted for use on missiles and in outer space, and found its way to maritime usage when the nuclear submarines Nautilus and Skate were suitably equipped in support of their transpolar voyages in 1958 [Dunlap and Shufeldt, 1972]. The


Figure 5.13: Proposed implementation of the IPEC method on a tractor-trailer assembly. principle of operation involves continuous sensing of minute accelerations in each of the three directional axes and integrating over time to derive velocity and position. A gyroscopically stabilized sensor platform is used to maintain consistent orientation of the three accelerometers throughout this process.

Although fairly simple in concept, the specifics of implementation are rather demanding. This is mainly caused by error sources that adversely affect the stability of the gyros used to ensure correct attitude. The resulting high manufacturing and maintenance costs have effectively precluded any practical application of this technology in the automated guided vehicle industry [Turpin, 1986]. For example, a high-quality inertial navigation system (INS) such as would be found in a commercial airliner will have a typical drift of about 1850 meters ( 1 nautical mile) per hour of operation, and cost between $\$ 50 \mathrm{~K}$ and $\$ 70 \mathrm{~K}$ [Byrne et al., 1992]. High-end INS packages used in ground applications have shown performance of better than 0.1 percent of distance traveled, but cost in the neighborhood of $\$ 100 \mathrm{~K}$ to $\$ 200 \mathrm{~K}$, while lower performance versions (i.e., one percent of distance traveled) run between $\$ 20 \mathrm{~K}$ to $\$ 50 \mathrm{~K}$ [Dahlin and Krantz, 1988].

Experimental results from the Université Montpellier in France [Vaganay et al., 1993a; 1993b], from the University of Oxford in the U.K. [Barshan and Durrant-Whyte, 1993; 1995], and from the University of Michigan indicate that a purely inertial navigation approach is not realistically advantageous (i.e., too expensive) for mobile robot applications. As a consequence, the use of INS hardware in robotics applications to date has been generally limited to scenarios that aren't readily addressable by more practical alternatives. An example of such a situation is presented by Sammarco [1990; 1994], who reports preliminary results in the case of an INS used to control an autonomous vehicle in a mining application.

Inertial navigation is attractive mainly because it is self-contained and no external motion information is needed for positioning. One important advantage of inertial navigation is its ability to provide fast, low-latency dynamic measurements. Furthermore, inertial navigation sensors typically have noise and error sources that are independent from the external sensors [Parish and Grabbe, 1993]. For example, the noise and error from an inertial navigation system should be quite different from that of, say, a landmark-based system. Inertial navigation sensors are self-contained, nonradiating, and non-jammable. Fundamentally, gyros provide angular rate and accelerometers provide velocity rate information. Dynamic information is provided through direct measurements. However, the main disadvantage is that the angular rate data and the linear velocity rate data must be integrated once and twice (respectively), to provide orientation and linear position, respectively. Thus, even very small errors in the rate information can cause an unbounded growth in the error of integrated measurements. As we remarked in Section 2.2, the price of very accurate laser gyros and optical fiber gyros have come down significantly. With price tags of $\$ 1,000$ to $\$ 5,000$, these devices have now become more suitable for many mobile robot applications.

### 5.4.1 Accelerometers

The suitability of accelerometers for mobile robot positioning was evaluated at the University of Michigan. In this informal study it was found that there is a very poor signal-to-noise ratio at lower accelerations (i.e., during low-speed turns). Accelerometers also suffer from extensive drift, and they are sensitive to uneven grounds, because any disturbance from a perfectly horizontal position will cause the sensor to detect the gravitational acceleration $g$. One low-cost inertial navigation system aimed at overcoming the latter problem included a tilt sensor [Barshan and Durrant-Whyte, 1993; 1995]. The tilt information provided by the tilt sensor was supplied to the accelerometer to cancel the gravity component projecting on each axis of the accelerometer. Nonetheless, the results obtained from the tilt-compensated system indicate a position drift rate of 1 to $8 \mathrm{~cm} / \mathrm{s}$ ( 0.4 to 3.1 $\mathrm{in} / \mathrm{s}$ ), depending on the frequency of acceleration changes. This is an unacceptable error rate for most mobile robot applications.

### 5.4.2 Gyros

Gyros have long been used in robots to augment the sometimes erroneous dead-reckoning information of mobile robots. As we explained in Chapter 2, mechanical gyros are either inhibitively expensive for mobile robot applications, or they have too much drift. Recent work by Barshan and Durrant-Whyte [1993; 1994; 1995] aimed at developing an INS based on solid-state gyros, and a fiber-optic gyro was tested by Komoriya and Oyama [1994].
5.4.2.1 Barshan and Durrant-Whyte [1993; 1994; 1995]

Barshan and Durrant-Whyte developed a sophisticated INS using two solid-state gyros, a solid-state triaxial accelerometer, and a two-axis tilt sensor. The cost of the complete system was $£ 5,000$ (roughly $\$ 8,000$ ). Two different gyros were evaluated in this work. One was the ENV-O5S Gyrostar from [MURATA], and the other was the Solid State Angular Rate Transducer (START) gyroscope manufactured by [GEC]. Barshan and Durrant-Whyte evaluated the performance of these two gyros and found that they suffered relatively large drift, on the order of 5 to $15 \% / \mathrm{min}$. The Oxford researchers then developed a sophisticated error model for the gyros, which was subsequently used in an Extended Kalman Filter (EKF - see Appendix A). Figure 5.14 shows the results of the experiment for the START gyro (left-hand side) and the Gyrostar (right-hand side). The thin plotted lines represent the raw output from the gyros, while the thick plotted lines show the output after conditioning the raw data in the EKF.

The two upper plots in Figure 5.14 show the measurement noise of the two gyros while they were stationary (i.e., the rotational rate input was zero, and the gyros should ideally show $\dot{\phi}=0 \% \mathrm{~s}$ ). Barshan and Durrant-Whyte determined that the standard deviation, here used as a measure for the


Figure 5.14: Angular rate (top) and orientation (bottom) for zero-input case (i.e., gyro remains stationary) of the START gyro (left) and the Gyrostar (right) when the bias error is negative. The erroneous observations (due mostly to drift) are shown as the thin line, while the EKF output, which compensates for the error, is shown as the heavy line. (Adapted from [Barshan and Durrant-Whyte, 1995] © IEEE 1995.)
amount of noise, was $0.16^{\circ}$ s for the START gyro and $0.24^{\circ}$ s for the Gyrostar. The drift in the rate output, 10 minutes after switching on, is rated at $1.35 \%$ s for the Gyrostar (drift-rate data for the START was not given).

The more interesting result from the experiment in Figure 5.14 is the drift in the angular output, shown in the lower two plots. We recall that in most mobile robot applications one is interested in the heading of the robot, not the rate of change in the heading. The measured rate $\dot{\phi}$ must thus be integrated to obtain $\phi$. After integration, any small constant bias in the rate measurement turns into a constant-slope, unbounded error, as shown clearly in the lower two plots of Figure 5.14. At the end of the five-minute experiment, the START had accumulated a heading error of -70.8 degrees while that of the Gyrostar was -59 degrees (see thin lines in Figure 5.14). However, with the EKF, the accumulated errors were much smaller: 12 degrees was the maximum heading error for the START gyro, while that of the Gyrostar was -3.8 degrees.

Overall, the results from applying the EKF show a five- to six-fold reduction in the angular measurement after a five-minute test period. However, even with the EKF, a drift rate of 1 to $3 \% \mathrm{~min}$ can still be expected.

### 5.4.2.2 Komoriya and Oyama [1994]

Komoriya and Oyama [1994] conducted a study of a system that uses an optical fiber gyroscope, in conjunction with odometry information, to improve the overall accuracy of position estimation. This fusion of information from two different sensor systems is realized through a Kalman filter (see Appendix A).

Figure 5.15 shows a computer simulation of a path-following study without (Figure 5.15a) and with (Figure 5.15b) the fusion of gyro information. The ellipses show the reliability of position estimates (the probability that the robot stays within the ellipses at each estimated position is 90 percent in this simulation).


Figure 5.15: Computer simulation of a mobile robot run.. (Adapted from [Komoriya and Oyama, 1994].)
a. Only odometry, without gyro information.
b. Odometry and gyro information fused.

In order to test the effectiveness of their method, Komoriya and Oyama also conducted actual experiments with Melboy, the mobile robot shown in Figure 5.16. In one set of experiments Melboy was instructed to follow the path shown in Figure 5.17a. Melboy's maximum speed was $0.14 \mathrm{~m} / \mathrm{s}(0.5 \mathrm{ft} / \mathrm{s})$ and that speed was further reduced at the corners of the path in Figure 5.17a. The final position errors without and with gyro information are compared and shown in Figure 5.17 b for 20 runs. Figure 5.17 b shows that the deviation of the position estimation errors from the mean value is smaller in the case where the gyro data was used (note that a large average deviation from the mean value indicates larger non-systematic errors, as explained in Sec. 5.1). Komoriya and Oyama explain that the noticeable deviation of the mean values from the origin in both cases could be reduced by careful calibration of the systematic errors (see Sec. 5.3) of the mobile robot.

We should note that from the description of this experiment in [Komoriya and Oyama, 1994] it is not immediately evident how the "position estimation error" (i.e., the circles) in Figure 5.17b was found. In our opinion, these points should have been measured by marking the return position of the robot on the floor (or by any equivalent


Figure 5.16: Melboy, the mobile robot used by Komoriya and Oyama for fusing odometry and gyro data. (Courtesy of [Komoriya and Oyama, 1994].) method that records the absolute position of the robot and compares it with the internally computed position estimation). The results of the plot in Figure 5.17b, however, appear to be too accurate for the absolute position error of the robot. In our experience an error on the order of several centimeters, not millimeters, should be expected after completing the path of Figure 5.17a (see, for example, [Borenstein and Koren, 1987; Borenstein and Feng, 1995a; Russel, 1995].) Therefore, we interpret the data in Figure 5.17b as showing a position error that was computed by the onboard computer, but not measured absolutely.

### 5.5 Summary

- Odometry is a central part of almost all mobile robot navigation systems.
- Improvements in odometry techniques will not change their incremental nature, i.e., even for improved odometry, periodic absolute position updates are necessary.


Figure 5.17: Experimental results from Melboy using odometry with and without a fiber-optic gyro.
a. Actual trajectory of the robot for a triangular path.
b. Position estimation errors of the robot after completing the path of a. Black circles show the errors without gyro; white circles show the errors with the gyro.
(Adapted from [Komoriya and Oyama, 1994].)

- More accurate odometry will reduce the requirements on absolute position updates and will facilitate the solution of landmark and map-based positioning.
- Inertial navigation systems alone are generally inadequate for periods of time that exceed a few minutes. However, inertial navigation can provide accurate short-term information, for example orientation changes during a robot maneuver. Software compensation, usually by means of a Kalman filter, can significantly improve heading measurement accuracy.


## Chapter 6 Active Beacon Navigation Systems

Active beacon navigation systems are the most common navigation aids on ships and airplanes. Active beacons can be detected reliably and provide very accurate positioning information with minimal processing. As a result, this approach allows high sampling rates and yields high reliability, but it does also incur high cost in installation and maintenance. Accurate mounting of beacons is required for accurate positioning. For example, land surveyors' instruments are frequently used to install beacons in a high-accuracy application [Maddox, 1994]. Kleeman [1992] notes that:
> "Although special beacons are at odds with notions of complete robot autonomy in an unstructured environment, they offer advantages of accuracy, simplicity, and speed - factors of interest in industrial and office applications, where the environment can be partially structured."

One can distinguish between two different types of active beacon systems: trilateration and triangulation.

## Trilateration

Trilateration is the determination of a vehicle's position based on distance measurements to known beacon sources. In trilateration navigation systems there are usually three or more transmitters mounted at known locations in the environment and one receiver on board the robot. Conversely, there may be one transmitter on board and the receivers are mounted on the walls. Using time-offlight information, the system computes the distance between the stationary transmitters and the onboard receiver. Global Positioning Systems (GPS), discussed in Section 3.1, are an example of trilateration. Beacon systems based on ultrasonic sensors (see Sec. 6.2, below) are another example.


Figure 6.1: The basic triangulation problem: a rotating sensor head measures the three angles $\lambda_{1}, \lambda_{2}$, and $\lambda_{3}$ between the vehicle's longitudinal axes and the three sources $\mathrm{S}_{1}, \mathrm{~S}_{2}$, and $\mathrm{S}_{3}$.

## Triangulation

In this configuration there are three or more active transmitters (usually infrared) mounted at known locations in the environment, as shown in Figure 6.1. A rotating sensor on board the robot registers the angles $\lambda_{1}, \lambda_{2}$, and $\lambda_{3}$ at which it "sees" the transmitter beacons relative to the vehicle's longitudinal axis. From these three measurements the unknown $x$ - and $y$-coordinates and the unknown vehicle orientation $\theta$ can be computed. Simple navigation systems of this kind can be built very inexpensively [Borenstein and Koren, 1986]. One problem with this configuration is that the active beacons need to be extremely powerful to insure omnidirectional transmission over large distances. Since such powerful beacons are not very practical it is necessary to focus the beacon within a cone-shaped propagation pattern. As a result, beacons are not visible in many areas, a problem that is particularly grave because at least three beacons must be visible for triangulation. A commercially available sensor system based on this configuration (manufactured and marketed by Denning) was tested at the University of Michigan in 1990. The system provided an accuracy of approximately $\pm 5$ centimeters ( $\pm 2$ in), but the aforementioned limits on the area of application made the system unsuitable for precise navigation in large open areas.

Triangulation methods can further be distinguished by the specifics of their implementation:
a. Rotating Transmitter-Receiver, Stationary Reflectors In this implementation there is one rotating laser beam on board the vehicle and three or more stationary retroreflectors are mounted at known locations in the environment.
b. Rotating Transmitter, Stationary Receivers Here the transmitter, usually a rotating laser beam, is used on board the vehicle. Three or more stationary receivers are mounted on the walls. The receivers register the incident beam, which may also carry the encoded azimuth of the transmitter.

For either one of the above methods, we will refer to the stationary devices as "beacons," even though they may physically be receivers, retroreflectors, or transponders.

### 6.1 Discussion on Triangulation Methods

Most of the active beacon positioning systems discussed in Section 6.3 below include computers capable of computing the vehicle's position. One typical algorithm used for this computation is described in [Shoval et al., 1995], but most such algorithms are proprietary because the solutions are non-trivial. In this section we discuss some aspects of triangulation algorithms.

In general, it can be shown that triangulation is sensitive to small angular errors when either the observed angles are small, or when the observation point is on or near a circle which contains the three beacons. Assuming reasonable angular measurement tolerances, it was found that accurate navigation is possible throughout a large area, although error sensitivity is a function of the point of observation and the beacon arrangements [McGillem and Rappaport, 1988].

### 6.1.1 Three-Point Triangulation

Cohen and Koss [1992] performed a detailed analysis on three-point triangulation algorithms and ran computer simulations to verify the performance of different algorithms. The results are summarized as follows:

- The geometric triangulation method works consistently only when the robot is within the triangle formed by the three beacons. There are areas outside the beacon triangle where the geometric approach works, but these areas are difficult to determine and are highly dependent on how the angles are defined.
- The Geometric Circle Intersection method has large errors when the three beacons and the robot all lie on, or close to, the same circle.
- The Newton-Raphson method fails when the initial guess of the robot' position and orientation is beyond a certain bound.
- The heading of at least two of the beacons was required to be greater than 90 degrees. The angular separation between any pair of beacons was required to be greater than 45 degrees.

In summary, it appears that none of the above methods alone is always suitable, but an intelligent combination of two or more methods helps overcome the individual weaknesses.

Yet another variation of the triangulation method is the so-called running fix, proposed by Case [1986]. The underlying principle of the running fix is that an angle or range obtained from a beacon at time $t-1$ can be utilized at time $t$, as long as the cumulative movement vector recorded since the reading was obtained is added to the position vector of the beacon, thus creating a virtual beacon.

### 6.1.2 Triangulation with More Than Three Landmarks

Betke and Gurvits [1994] developed an algorithm, called the Position Estimator, that solves the general triangulation problem. This problem is defined as follows: given the global position of $n$ landmarks and corresponding angle measurements, estimate the position of the robot in the global coordinate system. Betke and Gurvits represent the $n$ landmarks as complex numbers and formulate the problem as a set of linear equations. By contrast, the traditional law-of-cosines approach yields a set of non-linear equations. Betke and Gurvits also prove mathematically that their algorithm only fails when all landmarks are on a circle or a straight line. The algorithm estimates the robot's position in $\mathrm{O}(n)$ operations where $n$ is the number of landmarks on a two-dimensional map.

Compared to other triangulation methods, the Position Estimator algorithm has the following advantages: (1) the problem of determining the robot position in a noisy environment is linearized, (2) the algorithm runs in an amount of time that is a linear function of the number of landmarks, (3) the algorithm provides a position estimate that is close to the actual robot position, and (4) large errors ("outliers") can be found and corrected.

Betke and Gurvits present results of a simulation for the following scenario: the robot is at the origin of the map, and the landmarks are randomly distributed in a $10 \times 10$ meter $(32 \times 32 \mathrm{ft})$ area (see Fig. 6.2). The robot is at the corner of this area. The distance between a landmark and the robot is at most 14.1 meters


Figure 6.2: Simulation results using the algorithm Position Estimator on an input of noisy angle measurements. The squared error in the position estimate $p$ (in meters) is shown as a function of measurement errors (in percent of the actual angle). (Reproduced and adapted with permission from [Betke and Gurvits, 1994].)
$(46 \mathrm{ft})$ and the angles are at most 45 degrees. The simulation results show that large errors due to misidentified landmarks and erroneous angle measurements can be found and discarded. Subsequently, the algorithm can be repeated without the outliers, yielding improved results. One example is shown in Figure 6.3, which depicts simulation results using the algorithm Position Estimator. The algorithm works on an input of 20 landmarks (not shown in Figure 6.3) that were randomly placed in a $10 \times 10$ meters ( $32 \times 32 \mathrm{ft}$ ) workspace. The simulated robot is located at $(0,0)$. Eighteen of the landmarks were simulated to have a one-percent error in the angle measurement and two of the landmarks were simulated to have a large 10 -percent angle measurement


Figure 6.3: Simulation results showing the effect of outliers and the result of removing the outliers. (Reproduced and adapted with permission from [Betke and Gurvits, 1994].) error. With the angle measurements from 20 landmarks the Position Estimator produces 19 position estimates $p_{1}-p_{19}$ (shown as small blobs in Figure 6.3). Averaging these 19 estimates yields the computed robot position. Because of the two landmarks with large angle measurement errors two position estimates are bad: $p_{5}$ at $(79 \mathrm{~cm}, 72 \mathrm{~cm})$ and $p_{18}$ at $(12.5 \mathrm{~cm}, 18.3 \mathrm{~cm})$. Because of these poor position estimates, the resulting centroid (average) is at $\mathrm{P}^{\mathrm{a}}=(17 \mathrm{~cm}, 24 \mathrm{~cm})$. However, the Position Estimator can identify and exclude the two outliers. The centroid calculated without the outliers $p_{5}$ and $p_{18}$ is at $\mathrm{P}^{\mathrm{b}}=(12.5 \mathrm{~cm}, 18.3 \mathrm{~cm})$. The final position estimate after the Position Estimator is applied again on the 18 "good" landmarks (i.e., without the two outliers) is at $\mathrm{P}^{\mathrm{c}}=(6.5 \mathrm{~cm}, 6.5 \mathrm{~cm})$.

### 6.2 Ultrasonic Transponder Trilateration

Ultrasonic trilateration schemes offer a medium- to high-accuracy, low-cost solution to the position location problem for mobile robots. Because of the relatively short range of ultrasound, these systems are suitable for operation in relatively small work areas and only if no significant obstructions are present to interfere with wave propagation. The advantages of a system of this type fall off rapidly, however, in large multi-room facilities due to the significant complexity associated with installing multiple networked beacons throughout the operating area.

Two general implementations exist: 1) a single transducer transmitting from the robot, with multiple fixed-location receivers, and 2) a single receiver listening on the robot, with multiple fixed transmitters serving as beacons. The first of these categories is probably better suited to applications involving only one or at most a very small number of robots, whereas the latter case is basically unaffected by the number of passive receiver platforms involved (i.e., somewhat analogous to the Navstar GPS concept).

### 6.2.1 IS Robotics 2-D Location System

IS Robotics, Inc. [ISR], Somerville, MA, a spin-off company from MIT's renowned Mobile Robotics Lab, has introduced a beacon system based on an inexpensive ultrasonic trilateration system. This system allows their Genghis series robots to localize position to within 12.7 millimeters ( 0.5 in ) over a $9.1 \times 9.1$ meter ( $30 \times 30 \mathrm{ft}$ ) operating area [ISR, 1994]. The ISR system consists of a base station master hard-wired to two slave ultrasonic "pingers" positioned a known distance apart (typically 2.28 $\mathrm{m}-90 \mathrm{in}$ ) along the edge of the operating area as shown in Figure 6.4. Each robot is equipped with a receiving ultrasonic transducer situated beneath a cone-shaped reflector for omnidirectional coverage. Communication between the base station and individual robots is accomplished using a Proxim spread-spectrum ( 902 to 928 MHz ) RF link.

The base station alternately fires the two $40-\mathrm{kHz}$ ultrasonic pingers every half second, each time transmitting a two-byte radio packet in broadcast mode to advise all robots of pulse emission. Elapsed time between radio packet reception and detection of the ultrasonic wave front is used to calculate distance between the robot's current position and the known location of the active beacon. Inter-robot communication is accomplished over the same spread-spectrum channel using a time-division-multiple-access


Figure 6.4: The ISR Genghis series of legged robots localize x-y position with a master/slave trilateration scheme using two 40 kHz ultrasonic "pingers." (Adapted from [ISR, 1994].) scheme controlled by the base station. Principle sources of error include variations in the speed of sound, the finite size of the ultrasonic transducers, non-repetitive propagation delays in the electronics, and ambiguities associated with time-of-arrival detection. The cost for this system is $\$ 10,000$.

### 6.2.2 Tulane University 3-D Location System

Researchers at Tulane University in New Orleans, LA, have come up with some interesting methods for significantly improving the time-of-arrival measurement accuracy for ultrasonic transmitterreceiver configurations, as well as compensating for the varying effects of temperature and humidity. In the hybrid scheme illustrated in Figure 6.5, envelope peak detection is employed to establish the approximate time of signal arrival, and to consequently eliminate ambiguity interval problems for a more precise phase-measurement technique that provides final resolution [Figueroa and Lamancusa, 1992]. The desired 0.025 millimeters ( 0.001 in ) range accuracy required a time unit discrimination of 75 nanoseconds at the receiver, which can easily be achieved using fairly simplistic phase measurement circuitry, but only within the interval of a single wavelength. The actual distance from transmitter to receiver is the summation of some integer number of wavelengths (determined by the
coarse time-of-arrival measurement) plus that fractional portion of a wavelength represented by the phase measurement results.

Details of this time-of-arrival detection scheme and associated error sources are presented by Figueroa and Lamancusa [1992]. Range measurement accuracy of the prototype system was experimentally determined to be 0.15 millimeters ( 0.006 in ) using both threshold adjustments (based on peak detection) and phase correction, as compared to 0.53 millimeters ( 0.021 in ) for threshold adjustment alone. These high-accuracy requirements were necessary for an application that involved tracking the end-effector of a 6-DOF industrial robot [Figueroa et al, 1992]. The system incorporates seven 90-degree Massa piezoelectric transducers operating at 40 kHz , interfaced to a 33 MHz IBMcompatible PC. The general position-location strategy was based on a trilateration method developed by Figueroa and Mohegan [1994].


Figure 6.5: A combination of threshold adjusting and phase detection is employed to provide higher accuracy in time-of-arrival measurements in the Tulane University ultrasonic position-location system [Figueroa and Lamancusa, 1992].

The set of equations describing time-of-flight measurements for an ultrasonic pulse propagating from a mobile transmitter located at point ( $u, v, w$ ) to various receivers fixed in the inertial reference frame can be listed in matrix form as follows [Figueroa and Mohegan, 1994]:

$$
\left\{\begin{array}{c}
\left(\mathrm{t}_{1}-\mathrm{t}_{\mathrm{d}}\right)^{2}  \tag{6.1}\\
\left(\mathrm{t}_{2}-\mathrm{t}_{\mathrm{d}}\right)^{2} \\
* \\
* \\
* \\
\left(\mathrm{t}_{\mathrm{n}}-\mathrm{t}_{\mathrm{d}}\right)^{2}
\end{array}\right\}=\left[\begin{array}{ccccc}
1 & \mathrm{r}_{1}^{2} & 2 \mathrm{x}_{1} & 2 \mathrm{y}_{1} & 2 \mathrm{z}_{1} \\
1 & \mathrm{r}_{2}^{2} & 2 \mathrm{x}_{2} & 2 \mathrm{y}_{2} & 2 \mathrm{z}_{2} \\
* & & & \\
* & & & \\
* & & & & \\
1 & \mathrm{r}_{\mathrm{n}}^{2} & 2 \mathrm{x}_{\mathrm{n}} & 2 \mathrm{y}_{\mathrm{n}} & 2 \mathrm{z}_{\mathrm{n}}
\end{array}\right]\left\{\begin{array}{c}
\frac{\mathrm{p}^{2}}{\mathrm{c}^{2}} \\
\frac{1}{\mathrm{c}^{2}} \\
-\frac{\mathrm{u}}{\mathrm{c}^{2}} \\
-\frac{\mathrm{v}}{\mathrm{c}^{2}} \\
-\frac{\mathrm{w}}{\mathrm{c}^{2}}
\end{array}\right\}
$$

where:
$t_{\mathrm{i}} \quad=$ measured time of flight for transmitted pulse to reach $i^{\text {th }}$ receiver
$t_{\mathrm{d}} \quad=$ system throughput delay constant
$r_{\mathrm{i}}^{2} \quad=$ sum of squares of $i^{\text {th }}$ receiver coordinates
$\left(x_{\mathrm{i}}, y_{\mathrm{i}}, z_{\mathrm{i}}\right)=$ location coordinates of $i^{\text {th }}$ receiver
$(u, v, w)=$ location coordinates of mobile transmitter
$c \quad=$ speed of sound
$p^{2} \quad=$ sum of squares of transmitter coordinates.
The above equation can be solved for the vector on the right to yield an estimated solution for the speed of sound $c$, transmitter coordinates ( $u, v, w$ ), and an independent term $p^{2}$ that can be compared to the sum of the squares of the transmitter coordinates as a checksum indicator [Figueroa and Mahajan, 1994]. An important feature of this representation is the use of an additional receiver (and associated equation) to enable treatment of the speed of sound itself as an unknown, thus ensuring continuous on-the-fly recalibration to account for temperature and humidity effects. (The system throughput delay constant $t_{d}$ can also be determined automatically from a pair of equations for $l / c^{2}$ using two known transmitter positions. This procedure yields two equations with $t_{d}$ and $c$ as unknowns, assuming $c$ remains constant during the procedure.) A minimum of five receivers is required for an unambiguous three-dimensional position solution, but more can be employed to achieve higher accuracy using a least-squares estimation approach. Care must be taken in the placement of receivers to avoid singularities as defined by Mahajan [1992].

Figueroa and Mahajan [1994] report a follow-up version intended for mobile robot positioning that achieves 0.25 millimeters ( 0.01 in ) accuracy with an update rate of 100 Hz . The prototype system tracks a TRC LabMate over a $2.7 \times 3.7$ meter ( $9 \times 12 \mathrm{ft}$ ) operating area with five ceilingmounted receivers and can be extended to larger floor plans with the addition of more receiver sets. An RF link will be used to provide timing information to the receivers and to transmit the subsequent $\mathrm{x}-\mathrm{y}$ position solution back to the robot. Three problem areas are being further investigated to increase the effective coverage and improve resolution:

- Actual transmission range does not match the advertised operating range for the ultrasonic transducers, probably due to a resonant frequency mismatch between the transducers and electronic circuitry.
- The resolution of the clocks ( 6 MHz ) used to measure time of flight is insufficient for automatic compensation for variations in the speed of sound.
- The phase-detection range-measurement correction sometimes fails when there is more than one wavelength of uncertainty. This problem can likely be solved using the frequency division scheme described by Figueroa and Barbieri [1991].


### 6.3 Optical Positioning Systems

Optical positioning systems typically involve some type of scanning mechanism operating in conjunction with fixed-location references strategically placed at predefined locations within the operating environment. A number of variations on this theme are seen in practice [Everett, 1995]:

- Scanning detectors with fixed active beacon emitters.
- Scanning emitter/detectors with passive retroreflective targets.
- Scanning emitter/detectors with active transponder targets.
- Rotating emitters with fixed detector targets.

One of the principal problems associated with optical beacon systems, aside from the obvious requirement to modify the environment, is the need to preserve a clear line of sight between the robot and the beacon. Preserving an unobstructed view is sometimes difficult if not impossible in certain applications such as congested warehouse environments. In the case of passive retroreflective targets, problems can sometimes arise from unwanted returns from other reflective surfaces in the surrounding environment, but a number of techniques exists for minimizing such interference.

### 6.3.1 Cybermotion Docking Beacon

The automated docking system used on the Cybermotion Navmaster robot incorporates the unique combination of a structured-light beacon (to establish bearing) along with a one-way ultrasonic ranging system (to determine standoff distance). The optical portion consists of a pair of nearinfrared transceiver units, one mounted on the front of the robot and the other situated in a known position and orientation within the operating environment. These two optical transceivers are capable of full-duplex data transfer between the robot and the dock at a rate of 9600 bits per second. Separate modulation frequencies of 154 and 205 kHz are employed for the uplink and downlink respectively to eliminate crosstalk. Under normal circumstances, the dock-mounted transceiver waits passively until interrogated by an active transmission from the robot. If the interrogation is specifically addressed to the assigned ID number for that particular dock, the dock control computer activates the beacon transmitter for 20 seconds. (Dock IDs are jumper selectable at time of installation.)

Figure 6.6 shows the fixed-location beacon illuminating a 90-degree field of regard broken up into two uniquely identified zones, designated for purposes of illustration here as the Left Zone and Right Zone. An array of LED emitters in the beacon head is divided by a double-sided mirror arranged along the optical axis and a pair of lenses. Positive zone identification is initiated upon request from the robot in the form of a NAV Interrogation byte transmitted over the optical datalink. LEDs on opposite sides of the mirror respond to this NAV Interrogation with slightly different coded responses. The robot can thus determine its relative location with respect


Figure 6.6: The structured-light near-infrared beacon on the Cybermotion battery recharging station defines an optimal path of approach for the K2A Navmaster robot [Everett, 1995].
to the optical axis of the beacon based on the response bit pattern detected by the onboard receiver circuitry.

Once the beacon starts emitting, the robot turns in the appropriate direction and executes the steepest possible (i.e., without losing sight of the beacon) intercept angle with the beacon optical axis. Crossing the optical axis at point B is flagged by a sudden change in the bit pattern of the NAV Response Byte, whereupon the robot turns inward to face the dock. The beacon optical axis establishes the nominal path of approach and in conjunction with range offset information uniquely defines the robot's absolute location. This situation is somewhat analogous to a TACAN station [Dodington, 1989] but with a single defined radial.

The offset distance from vehicle to dock is determined in rather elegant fashion by a dedicated non-reflective ultrasonic ranging configuration. This high-frequency ( $>200 \mathrm{kHz}$ ) narrow-beam ( $15^{\circ}$ ) sonar system consists of a piezoelectric transmitter mounted on the docking beacon head and a complimentary receiving transducer mounted on the front of the vehicle. A ranging operation is initiated upon receipt of the NAV Interrogation Byte from the robot; the answering NAV Response Byte from the docking beacon signals the simultaneous transmission of an ultrasonic pulse. The difference at the robot end between time of arrival for the NAV Response Byte over the optical link and subsequent ultrasonic pulse detection is used to calculate separation distance. This dualtransducer master/slave technique assures an unambiguous range determination between two well defined points and is unaffected by any projections on or around the docking beacon and/or face of the robot.

During transmission of a NAV Interrogation Byte, the left and right sides of the LED array located on the robot are also driven with uniquely identifiable bit patterns. This feature allows the docking beacon computer to determine the robot's actual heading with respect to the nominal path of approach. Recall the docking beacon's structured bit pattern establishes (in similar fashion) the side of the vehicle centerline on which the docking beacon is located. This heading information is subsequently encoded into the NAV Response Byte and passed to the robot to facilitate course correction. The robot closes on the beacon, halting at the defined stop range (not to exceed 8 ft ) as repeatedly measured by the docking sonar. Special instructions in the path program can then be used to reset vehicle heading and/or position.

### 6.3.2 Hilare

Early work incorporating passive beacon tracking at the Laboratoire d'Automatique et d'Analyse des Systemes, Toulouse, France, involved the development of a navigation subsystem for the mobile robot Hilare [Banzil et al., 1981]. The system consisted of two near-infrared emitter/detectors mounted with a 25 centimeters ( 10 in ) vertical separation on a rotating mast, used in conjunction with passive reflective beacon arrays at known locations in three corners of the room.

Each of these beacon arrays was constructed of retroreflective tape applied to three vertical cylinders, which were then placed in a recognizable configuration as shown in Figure 6.7. One of the arrays was inverted so as to be uniquely distinguishable for purposes of establishing an origin. The cylinders were vertically spaced to intersect the two planes of light generated by the rotating optical axes of the two emitters on the robot's mast. A detected reflection pattern as in Figure 6.8 confirmed beacon acquisition. Angular orientation relative to each of the retroreflective arrays was inferred from the stepper-motor commands that drove the scanning mechanism; lateral position was determined through simple triangulation.


Figure 6.7: Retroreflective beacon array configuration used on the mobile robot Hilare. (Adapted from [Banzil et al, 1981].)


Figure 6.8: A confirmed reflection pattern as depicted above was required to eliminate potential interference from other highly specular surfaces [Banzil et al., 1981].

### 6.3.3 NAMCO LASERNET

The NAMCO LASERNET beacon tracking system (Figure 6.9) employs retroreflective targets distributed throughout the operating area of an automated guided vehicle (AGV) in order to measure range and angular position (Figure 6.10). A servo-controlled rotating mirror pans a near-infrared laser beam through a horizontal arc of 90 degrees at a 20 Hz update rate. When the beam sweeps across a target of known dimensions, a return signal of finite duration is sensed by the detector. Since the targets are all the same size, the signal generated by a close target will be of longer duration than that from a distant one.

Angle measurement is initiated when the scanner begins its sweep from right to left; the laser strikes an internal synchronization photodetector that starts a timing sequence. The beam is then panned across the scene until returned by a retroreflective target in the field of view. The reflected signal is detected by the sensor, terminating the timing sequence (Fig. 6.11). The elapsed time is used to calculate the angular position of the target in the equation [NAMCO, 1989]
$\theta=V t_{\mathrm{b}}-45^{\circ}$
where
$\theta=$ target angle
$V=$ scan velocity $\left(7,200^{\circ} / \mathrm{s}\right)$
$T_{\mathrm{b}}=$ time between scan initiation and target detection.


Figure 6.9: The LASERNET beacon tracking system. (Courtesy of Namco Controls Corp.)

This angle calculation determines either the leading edge of the target, the trailing edge of the target, or the center of the target, depending upon the option selected within the LASERNET software option list. The angular accuracy is $\pm 1$ percent, and the angular resolution is 0.1 degrees for the analog output; accuracy is within $\pm .05$ percent with a resolution of 0.006 degrees when the RS-232 serial port is used. The analog output is a voltage ranging from 0 to 10 V over the range of -45 to +45 degrees, whereas the RS-232 serial port reports a proportional "count value" from 0 to 15360 over this same range. The system costs $\$ 3,400$ in its basic configuration, but it has only a limited range of 15 meters ( 50 ft ).


Figure 6.10: The LASERNET system can be used with projecting wall-mounted targets to guide an AGV at a predetermined offset distance. (Courtesy of NAMCO Controls.)


Figure 6.11: a. The perceived width of a retroreflective target of known size is used to calculate range; $b$. while the elapsed time between sweep initiation and leading edge detection yields target bearing. (Courtesy of NAMCO Controls).

### 6.3.3.1 U.S. Bureau of Mines' application of the LaserNet sensor

One robotics application of the NAMCO LaserNet is a research project conducted by Anderson [1991] at the U.S. Bureau of Mines. In this project the feasibility of automating the motion of a continuous mining $(\mathrm{CM})$ machine. One such CM is the Joy 16CM shown in Fig. 6.12. The challenge with a CM is not speed, but vibration. During operation the cylindrical cutting device in front of the machine (see Fig. 6.13) cuts coal from the surface and a conveyor belt moves the coal backward for further processing. This and related activities generate a considerable amount of vibration. Another challenge in this mining application is the stringent requirement for high accuracy. High accuracy is required since even small position and orientation errors cause non-optimal cutting conditions that result in sub-optimal production yield.

The researchers at the U.S. Bureau of Mines installed two cylindrical retroreflective targets on the tail-end of the CM, while two LaserNet sensors were mounted on tripods at the entryway to the mine (see Fig. 6.13). One of the reported difficulties with this setup was the limited range of the early-model LaserNet sensor used in this experiment: 10.67 meter ( 35 ft ) radially with a $110^{\circ}$ field-of-view. The newer LaserNet LN120 (described in Section 6.3.3, above) has an improved range of 15.24 meter ( 50 ft ). Another problem encountered in this application was the irregularity of the floor. Because of these irregularities the stationary scanners' beams would sometimes sweep beneath or above the retroreflective targets on the CM.


Figure 6.13: Front view of the Joy 16CM continuous mining machine at the U.S. Bureau of Mines' test facility. Cylindrical retroreflective targets are mounted on the tail (Courtesy of Anderson [1991].)

Besides the above mentioned technical difficulties the LaserNet system provided accurate data. In a series of test in which the CM moved on average one meter $(3.3 \mathrm{ft})$ forward while cutting coal at the same time the resulting average error in translation was well below one centimeter. In a series of rotational movements of 7 to $15^{\circ}$ the average measurement error was $0.3^{\circ}$. It should be emphasized that the LaserNet system proved robust in the presence of substantial vibrations.


Figure 6.13: Schematic view of the Joy 16CM with two retroreflective targets and two LaserNav beacons/sensors in the entryway. (Courtesy of Anderson, [1991].)

### 6.3.4 Denning Branch International Robotics LaserNav Position Sensor

Denning Branch International Robotics [DBIR], Pittsburgh, PA, offers a laser-based scanning beacon system that computes vehicle position and heading out to 183 meters ( 600 ft ) using cooperative electronic transponders, called active targets. A range of 30.5 meters ( 100 ft ) is achieved with simple reflectors (passive targets). The LaserNav Intelligent Absolute Positioning Sensor, shown in Figures 6.14 and 6.15, is a non-ranging triangulation system with an absolute bearing accuracy of 0.03 degrees at a scan rate of 600 rpm . The fan-shaped beam is spread 4 degrees vertically to ensure target detection at long range while traversing irregular floor surfaces, with horizontal divergence limited to 0.017 degrees. Each target can be uniquely coded so that the LaserNav can distinguish between up to 32 separate active or passive targets during a single scan. The vehicle's x -y position is calculated every 100 milliseconds. The sensor package weighs 4.4 kilograms ( 10 lb ), measures 38 centimeters ( 15 in ) high and 30 centimeters ( 12 in ) in diameter, and has a power consumption of only 300 mA at 12 V . The eye-safe near-infrared laser generates a 1 mW output at a wavelength of 810 nanometers.


Figure 6.14: Schematics of the Denning Branch International Robotics LaserNav laser-based scanning beacon system. (Courtesy of Denning Branch International Robotics.)


Figure 6.15: Denning Branch International Robotics (DBIR) can see active targets at up to 183 meters ( 600 ft ) away. It can identify up to 32 active or passive targets. (Courtesy of Denning Branch International Robotics.)

One potential source of problems with this device is the relatively small vertical divergence of the beam: $\pm 2$ degrees. Another problem mentioned by the developer [Maddox, 1994] is that "the LaserNav sensor ... is subject to rare spikes of wrong data." This undesirable phenomenon is likely due to reflections off shiny surfaces other than the passive reflectors. This problem affects probably all light-based beacon navigation systems to some degree. Another source of erroneous beacon readings is bright sunlight entering the workspace through wall openings.

### 6.3.5 TRC Beacon Navigation System

Transitions Research Corporation [TRC], Danbury, CT, has incorporated their LED-based LightRanger, discussed in Section 4.2, into a compact, low-cost navigational referencing system for open-area autonomous platform control. The TRC Beacon Navigation System calculates vehicle position and heading at ranges up to 24.4 meters ( 80 ft ) within a quadrilateral area defined by four passive retroreflective beacons [TRC, 1994] (see Figure 6.16). A static 15 -second unobstructed view
of all four beacons is required for initial acquisition and setup, after which only two beacons must remain in view as the robot moves about. At this time there is no provision to periodically acquire new beacons along a continuous route, so operation is currently constrained to a single zone roughly the size of a small building (i.e., $24.4 \times 24.4 \mathrm{~m}$ or $80 \times 80 \mathrm{ft}$ ).

System resolution is 120 millimeters $(43 / 4 \mathrm{in})$ in range and 0.125 degrees in bearing for full 360 -degree coverage in the horizontal plane. The scan unit (less processing electronics) is a cube approximately 100 millimeters (4 in) on a side, with a maximum $1-\mathrm{Hz}$ update rate dictated by the $60-\mathrm{rpm}$ scan speed. A dedicated 68 HC 11 microprocessor continuously outputs navigational parameters ( $\mathrm{x}, \mathrm{y}, \theta$ ) to the vehicle's onboard controller via an RS-232 serial port. Power requirements are 0.5 A at 12 VDC and 0.1 A at 5 VDC . The system costs $\$ 11,000$.

### 6.3.6 Siman Sensors and Intelligent Machines Ltd., ROBOSENSE

The ROBOSENSE is an eye-safe, scanning laser rangefinder developed by Siman Sensors \& Intelligent Machines Ltd., Misgav, Israel (see Figure 6.17). The scanner illuminates retroreflective targets mounted on walls in the environment. It sweeps 360 -degree segments in continuous rotation but supplies navigation data even while observing targets in narrower segments (e.g., $180^{\circ}$ ). The system's output are x - and y-coordinates in a global coordinate system, as well as heading and a confidence level. According to the manufacturer [Siman, 1995], the system is designed to operate under severe or adverse conditions, such as the partial occlusion of the reflectors. A rugged case houses the electro-optical sensor, the navigation computer, the communication module, and the power supply. ROBOSENSE incorporates a unique self-mapping feature that does away with the need for precise measurement of the targets, which is needed with other systems.

The measurement range of the ROBOSENSE system is 0.3 to 30 meters ( 1 to 100 ft ). The position accuracy is 20 millimeters ( $3 / 4 \mathrm{in}$ ) and the accuracy in determining the orientation is better than 0.17 degrees. The system can communicate with an onboard computer via serial link, and it updates the position and heading information at a rate of 10 to 40 Hz . ROBOSENSE navigates through areas that can be much larger than the system's range. This is done by dividing the whole site map into partial frames, and positioning the system within each frame in the global coordinate system. This method, called Rolling Frames, enables ROBOSENSE to cover practically unlimited area.

The power consumption of the ROBOSENSE system is less than 20 W at 24 VDC . The price for a single unit is $\$ 12,800$ and $\$ 7,630$ each for an order of three units.


Figure 6.17: The ROBOSENSE scanning laser rangefinder was developed by Siman Sensors \& Intelligent Machines Ltd., Misgav, Israel. The system determines its own heading and absolute position with an accuracy of $0.17^{\circ}$ and 20 millimeters ( $3 / 4 \mathrm{in}$ ), respectively. (Courtesy of Siman Sensors \& Intelligent Machines.)

### 6.3.7 Imperial College Beacon Navigation System

Premi and Besant [1983] of the Imperial College of Science and Technology, London, England, describe an AGV guidance system that incorporates a vehicle-mounted laser beam rotating in a horizontal plane that intersects three fixed-location reference sensors as shown in Figure 6.18. The photoelectric sensors are arranged in collinear fashion with equal separation and are individually wired to a common FM transmitter via appropriate electronics so that the time of arrival of laser energy is relayed to a companion receiver on board the vehicle. A digitally coded identifier in the data stream identifies the activated sensor that triggered the transmission, thus allowing the onboard computer to measure the separation angles $\alpha_{1}$ and $\alpha_{2}$.

AGV position $\mathrm{P}(x, y)$ is given by the equations [Premi and Besant, 1983]

$$
\begin{align*}
& x=x_{1}+r \cos \theta \\
& y=y_{1}+r \sin \theta \tag{6.3}
\end{align*}
$$

where
$r=\frac{a \sin \left(\alpha_{1}+\beta\right)}{\sin \alpha_{1}}$
$\beta=\arctan \frac{2 \tan \alpha_{1} \tan \alpha_{2}}{\tan \alpha_{2}-\tan \alpha_{1}}-1$
$\theta=\phi-\beta$.


Figure 6.18: Three equidistant collinear photosensors are employed in lieu of retroreflective beacons in the Imperial College laser triangulation system for AGV guidance. (Adapted from [Premi and Besant, 1983].)

An absolute or indexed incremental position encoder that monitors laser scan azimuth is used to establish platform heading.

This technique has some inherent advantages over the use of passive retroreflective targets, in that false acquisition of reflective surfaces is eliminated, and longer ranges are possible since target reflectivity is no longer a factor. More robust performance is achieved through elimination of target dependencies, allowing a more rapid scan rate to facilitate faster positional updates. The one-way nature of the optical signal significantly reduces the size, weight, and cost of the onboard scanner with respect to that required for retroreflective beacon acquisition. Tradeoffs, however, include the increased cost associated with installation of power and communications lines and the need for significantly more expensive beacons. This can be a serious drawback in very-large-area installations, or scenarios where multiple beacons must be incorporated to overcome line-of-sight limitations.

### 6.3.8 MTI Research CONAC ${ }^{\text {TM }}$

A similar type system using a predefined network of fixed-location detectors is currently being built and marketed by MTI Research, Inc., Chelmsford, MA [MTI]. MTI's Computerized Opto-electronic Navigation and Control ${ }^{1}$ (CONAC) is a relatively low-cost, high-performance navigational referencing system employing a vehiclemounted laser unit called STRuctured Optoelectronic $\underline{\text { Acquisition Beacon (STROAB), }}$ as shown in Figure 6.19. The scanning laser beam is spread vertically to eliminate critical alignment, allowing the receivers, called Networked Opto-electronic $\underline{\text { Acquisition }}$ $\underline{\text { Datums ( }}$ NOADs) (see Figure 6.20), to be mounted at arbitrary heights (as illustrated in Figure 6.21). Detection of incident illumination by a NOAD triggers a response over the network to a host PC, which in turn calcu-


Figure 6.19: A single STROAB beams a vertically spread laser signal while rotating at 3,000 rpm. (Courtesy of, MTI Research Inc.) lates the implied angles $\alpha_{1}$ and $\alpha_{2}$. An index sensor built into the STROAB generates a special rotation reference pulse to facilitate heading measurement. Indoor accuracy is on the order of centimeters or millimeters, and better than 0.1 degrees for heading.

The reference NOADs are strategically installed at known locations throughout the area of interest, and daisy chained together with ordinary four-conductor modular telephone cable. Alternatively the NOADS can be radio linked to eliminate cable installation problems, as long as power is independently available to the various NOAD sites. STROAB acquisition range is sufficient to where three NOADS can effectively cover an area of $33,000 \mathrm{~m}^{2}$ (over 8 acres) assuming no

[^1]interfering structures block the view. Additional NOADS are typically employed to increase fault tolerance and minimize ambiguities when two or more robots are operating in close proximity. The optimal set of three NOADS is dynamically selected by the host PC, based on the current location of the robot and any predefined visual barriers. The selected NOADS are individually addressed over the network in accordance with assigned codes (set into DIP switches on the back of each device at time of installation).

An interesting and unconventional aspect of CONAC ${ }^{\text {TM }}$ is that no fall-back dead-reckoning capability is incorporated into the system [MacLeod and Chiarella, 1993]. The $3,000 \mathrm{rpm}$ angular rotation speed of the laser STROAB facilitates rapid position updates at a 25 Hz rate, which MTI claims is sufficient for safe automated transit at highway speeds, provided line-of-sight contact is preserved with at least three fixed NOADS. To mini-


Figure 6.20: Stationary NOADs are located at known positions; at least two NOADs are networked and connected to a PC. (Courtesy of MTI Research, Inc.) mize chances of occlusion, the lightweight (less than $250 \mathrm{~g}-9 \mathrm{oz}$ ) STROAB is generally mounted as high as possible on a supporting mast.

The ability of the $\mathrm{CONAC}^{\mathrm{TM}}$ system was demonstrated in an intriguing experiment with a small, radio-controlled race car called Scooter. During this experiment, the Scooter achieved speeds greater than $6.1 \mathrm{~m} / \mathrm{s}(20 \mathrm{ft} / \mathrm{s})$ as shown by the Scooters mid-air acrobatics in Figure 6.22 . The small vehicle was equipped with a STROAB and programmed to race along the race course shown in Figure 6.23. The small boxes in Figure 6.23 represent the desired path, while the continuous line represents the

 system employs an onboard, rapidly rotating and vertically spread laser beam, which sequentially contacts the networked detectors. (Courtesy of MTI Research, Inc.)
position of the vehicle during a typical run. 2,200 data points were collected along the 200 meter $(650 \mathrm{ft})$ long path. The docking maneuver at the end of the path brought the robot to within 2 centimeters ( 0.8 in ) of the desired position. On the tight turns, the Scooter decelerated to smoothly execute the hairpin turns.


Figure 6.22: MTI's Scooter zips through a race course; tight close-loop control is maintained even in mid-air and at speeds of up to $6.1 \mathrm{~m} / \mathrm{s}(20 \mathrm{ft} / \mathrm{s})$.


Figure 6.23: Preprogrammed race course and recorded telemetry of the Scooter experiment. Total length: $200 \mathrm{~m}(650 \mathrm{ft}) ; 2200$ data points collected. (Courtesy of MTI Research, Inc.)

## CONAC ${ }^{\text {TM }}$ Fixed Beacon System

A stationary active beacon system that tracks an omnidirectional sensor mounted on the robot is currently being sold to allow for tracking multiple units. (The original CONAC ${ }^{\mathrm{TM}}$ system allows only one beacon to be tracked at a given time.) The basic system consists of two synchronized stationary beacons that provide bearings to the mobile sensor to establish its $x-y$ location. A hybrid version of this approach employs two lasers in one of the beacons, as illustrated in Figure 6.24, with the lower laser plane tilted from the vertical to provide coverage along the z -axis for three-dimensional applications. A complete two-dimensional indoor system is shown in Figure 6.25.

Long-range exterior position accu racy is specified as $\pm 1.3$ millimeters ( $\pm 0.5 \mathrm{in}$ ) and the heading accuracy as $\pm 0.05$ degrees. The nominal maximum line-of-sight distance is 250 meters ( 780 ft ), but larger distances can be covered with a more complex system. The system was successfully demonstrated in an outdoor environment when MacLeod engineers outfitted a Dodge caravan with electric actuators for steering, throttle, and brakes, then drove the unmanned vehicle at speeds up to 80 $\mathrm{km} / \mathrm{h}(50 \mathrm{mph})$ [Baker, 1993]. MTI recently demonstrated the same vehicle at $108 \mathrm{~km} / \mathrm{h}(65 \mathrm{mph})$. Absolute position and heading accuracies were sufficient to allow the Caravan to maneuver among parked vehicles and into a parking place using a simple AutoCad representation of the environment. Position computations are updated at a rate of 20 Hz . This system represents the current state-of-the-art in terms of active beacon positioning [Fox, 1993; Baker, 1993; Gunther, 1994]. A basic system with one STROAB and three NOADs costs on the order of $\$ 4,000$.


Figure 6.24: Simplified cross section view of the dual-laser position-location system now under development for tracking multiple mobile sensors in 3-D applications. (Courtesy of MTI Research, Inc.)


Figure 6.25: MTI's basic 2-D indoor package. A mobile position transponder (shown in lower center) detects the passing laser emissions generated by the two spread-out stationary laser beacons. (Courtesy of MTI Research, Inc.)

### 6.3.9 Spatial Positioning Systems, inc.: Odyssey

Spatial Positioning Systems, inc. [SPSi] of Reston, Virginia has developed and markets a highaccuracy 3-D positioning system called Odyssey. The Odyssey system was originally developed for the accurate surveying of construction sites and for retro-active three-dimensional modeling of buildings, etc. However, it appears that the system can be used for mobile robot operations quite easily.

The Odyssey system comprises two or more stationary laser transmitters (shown mounted on tripods, in Fig. 6.26) and a mobile optical receiver, which is shown mounted on top of the red-white receiving pole in the center of Fig. 6.26. The receiver is connected to a portable data logging device with real-time data output via RS-232 serial interface. In its originally intended hand-held mode of operation the surveyor holds the tip of the receiver-wand at a point of interest. The system records instantly the three-dimensional coordinates of that point (see Fig 6.27).

To set up the Odyssey system two or more transmitters must be placed at precisely known locations in the environment. Alternatively the accurate transmitter position can be computed in a reverse calibration procedure in which the receiver-wand is placed at four known positions. and the system Once the transmitters are located at known positions, one or more receivers can produce data points simultaneously, while being applied in the same environment.

The system has an accuracy of $\pm 1 \mathrm{~mm}+100 \mathrm{ppm}$ (note: ppm stands for parts in million) over a range of up to 150 meters ( 500 ft ). Thus, at a location 150 meters away from the transmitters the position accuracy would still be $1 \mathrm{~mm}+100 \mathrm{ppm} \times 150 \mathrm{~m}=16 \mathrm{~mm}$. Additional technical specifications are listed in Table y. For mobile robot applications the Odyssey system may be somewhat pricy at roughly $\$ 90,000$, depending on system configuration.


Figure 6.26: The Odyssey positioning system comprises two laser beam transmitters and a pole- or wand-mounted receiver. (Courtesy of Spatial Positioning Systems, Inc.)

Table 6.1: Technical specifications for the Odyssey positioning system. (Courtesy of Spatial Positioning Systems, inc.)

| Parameter | Value Units |
| :---: | :---: |
| Horizontal accuracy | $\begin{gathered} \pm 1 \mathrm{~mm} \\ 0.04 \mathrm{in} \\ +100 \mathrm{ppm} \end{gathered}$ |
| Vertical accuracy | $\begin{gathered} \pm 1 \mathrm{~mm} \\ 0.04 \text { inches } \\ +100 \mathrm{ppm} \end{gathered}$ |
| Outdoor receiver range | $\begin{aligned} & 150 \mathrm{~m} \\ & 500 \mathrm{ft} \end{aligned}$ |
| Indoor receiver range | $\begin{array}{r} 75 \mathrm{~m} \\ 250 \mathrm{ft} \end{array}$ |
| Measurement rate | 5 Hz |
| Transmitter scan rate | 50 Hz |
| Transmitter field of view | $120 \times 30$ |
| Transmitter power max. steady-state | 12 VDC 4.0 A <br> 1.5 A |
| Receiver power steady-state | 12 VDC 0.8 A 0.3 A |
| Transmitter dimensions | $\begin{gathered} 510 \times 210 \mathrm{~mm} \\ \times 180 \mathrm{in} \\ 20 \times 8 \times 7 \end{gathered}$ |
| Transmitter weight | 11 kg <br> 24 lbs |
| Receiver weight | $\begin{array}{r} \sim 4 \mathrm{~kg} \\ 9 \mathrm{lbs} \\ \hline \end{array}$ |



Figure 6.27: In its originally intended hand-held mode of operation the surveyor places the tip of the wand-receiver at a point of interest to record that point's 3-D coordinates. (Courtesy of Spatial Positioning Systems, Inc.)

### 6.3.9 Lawnmower CALMAN

Larsson et al. [1994] from the University of Lulea, Sweden, have converted a large riding lawnmower to fully autonomous operation. This system, called CALMAN, uses an onboard rotating laser scanner to illuminate strategically placed vertical retroreflector stripes. These reflectors are attached to tree stems or vertical poles in the environment. Larsson et al. report experimental results from running the vehicle in a parking lot. According to these results, the vehicle had a positioning error of less than 2 centimeters ( $3 / 4 \mathrm{in}$ ) at speeds of up to 0.3 milliseconds ( $1 \mathrm{ft} / \mathrm{s}$ ). The motion of the vehicle was stable at speeds of up to $1 \mathrm{~m} / \mathrm{s}(3.3 \mathrm{ft} / \mathrm{s})$ and became unstable at $1.5 \mathrm{~m} / \mathrm{s}(5 \mathrm{ft} / \mathrm{s})$.

### 6.4 Summary

We summarize the general characteristics of active beacon systems as follows:

- The environment needs to be modified, and some systems require electric outlets or battery maintenance for stationary beacons.
- A line of sight between transmitter and detector needs to be maintained, i.e., there must be at least two or three visible landmarks in the environment.
- Triangulation-based methods are subject to the limitations of triangulation as discussed by Cohen and Koss [1992].
- Active beacon systems have been proven in practice, and there are several commercial systems available using laser, infrared, and ultrasonic transducers.
- In practice, active beacon systems are the choice when high accuracy and high reliability are required.


## Chapter 7 <br> Landmark Navigation

Landmarks are distinct features that a robot can recognize from its sensory input. Landmarks can be geometric shapes (e.g., rectangles, lines, circles), and they may include additional information (e.g., in the form of bar-codes). In general, landmarks have a fixed and known position, relative to which a robot can localize itself. Landmarks are carefully chosen to be easy to identify; for example, there must be sufficient contrast to the background. Before a robot can use landmarks for navigation, the characteristics of the landmarks must be known and stored in the robot's memory. The main task in localization is then to recognize the landmarks reliably and to calculate the robot's position.

In order to simplify the problem of landmark acquisition it is often assumed that the current robot position and orientation are known approximately, so that the robot only needs to look for landmarks in a limited area. For this reason good odometry accuracy is a prerequisite for successful landmark detection.

The general procedure for performing landmark-based positioning is shown in Figure 7.1. Some approaches fall between landmark and map-based positioning (see Chap. 8). They use sensors to sense the environment and then extract distinct structures that serve as landmarks for navigation in the future. These approaches will be discussed in the chapter on map-based positioning techniques.


Figure 7.1: General procedure for landmark-based positioning.

Our discussion in this chapter addresses two types of landmarks: "artificial" and "natural." It is important to bear in mind that "natural" landmarks work best in highly structured environments such as corridors, manufacturing floors, or hospitals. Indeed, one may argue that "natural" landmarks work best when they are actually man-made (as is the case in highly structured environments). For this reason, we shall define the terms "natural landmarks" and "artificial landmarks" as follows: natural landmarks are those objects or features that are already in the environment and have a function other than robot navigation; artificial landmarks are specially designed objects or markers that need to be placed in the environment with the sole purpose of enabling robot navigation.

### 7.1 Natural Landmarks

The main problem in natural landmark navigation is to detect and match characteristic features from sensory inputs. The sensor of choice for this task is computer vision. Most computer vision-based natural landmarks are long vertical edges, such as doors and wall junctions, and ceiling lights. However, computer vision is an area that is too large and too diverse for the scope of this book. For this reason we will present below only one example of computer vision-based landmark detection, but without going into great detail.

When range sensors are used for natural landmark navigation, distinct signatures, such as those of a corner or an edge, or of long straight walls, are good feature candidates. The selection of features is important since it will determine the complexity in feature description, detection, and matching. Proper selection of features will also reduce the chances for ambiguity and increase positioning accuracy. A natural landmark positioning system generally has the following basic components:

- A sensor (usually computer vision) for detecting landmarks and contrasting them against their background.
- A method for matching observed features with a map of known landmarks.
- A method of computing location and localization errors from the matches.

One system that uses natural landmarks has recently been developed in Canada. This project aimed at developing a sophisticated robot system called the "Autonomous Robot for a Known Environment" (ARK). The project was carried out jointly by the Atomic Energy of Canada Ltd (AECL) and Ontario Hydro Technologies with support from the University of Toronto and York University [Jenkin et al., 1993]. A Cybermotion K2A+ platform serves as the carrier for a number of sensor subsystems (see Figure 7.2).

Of interest for the discussion here is the ARK navigation module (shown in Figure 7.3). This unit consists of a custom-made pan-and-tilt table, a CCD camera, and an eye-safe IR spot laser rangefinder. Two VME-based cards, a single-board computer, and a microcontroller, provide processing power. The navigation module is used to periodically correct the robot's accumulating odometry errors. The system uses natural


Figure 7.2: The ARK system is based on a modified Cybermotion K2A+. It is one of the few working navigation systems based on natural landmark detection. (Courtesy of Atomic Energy of Canada Ltd.)
landmarks such as alphanumeric signs, semipermanent structures, or doorways. The only criteria used is that the landmark be distinguishable from the background scene by color or contrast.

The ARK navigation module uses an interesting hybrid approach: the system stores (learns) landmarks by generating a three- dimensional "grey-level surface" from a single training image obtained from the CCD camera. A coarse, registered range scan of the same field of view is performed by the laser rangefinder, giving depths for each pixel in the grey-level surface. Both procedures are performed from a known robot position. Later, during operation, when the robot is at an approximately known (from odometry) position within a couple of meters from the training position, the vision system searches for those landmarks that are


Figure 7.3: AECL's natural landmark navigation system uses a CCD camera in combination with a time-of-flight laser rangefinder to identify landmarks and to measure the distance between landmark and robot. (Courtesy of Atomic Energy of Canada Ltd.) expected to be visible from the robot's momentary position. Once a suitable landmark is found, the projected appearance of the landmark is computed. This expected appearance is then used in a coarse-to-fine normalized correlation-based matching algorithm that yields the robot's relative distance and bearing with regard to that landmark. With this procedure the ARK can identify different natural landmarks and measure its position relative to the landmarks.

To update the robot's odometry position the system must find a pair of natural landmarks of known position. Positioning accuracy depends on the geometry of the robot and the landmarks but is typically within a few centimeters. It is possible to pass the robot through standard 90-centimeter ( 35 in ) doorway openings using only the navigation module if corrections are made using the upper corners of the door frame just prior to passage.

### 7.2 Artificial Landmarks

Detection is much easier with artificial landmarks [Atiya and Hager, 1993], which are designed for optimal contrast. In addition, the exact size and shape of artificial landmarks are known in advance. Size and shape can yield a wealth of geometric information when transformed under the perspective projection.

Researchers have used different kinds of patterns or marks, and the geometry of the method and the associated techniques for position estimation vary accordingly [Talluri and Aggarwal, 1993]. Many artificial landmark positioning systems are based on computer vision. We will not discuss these systems in detail, but we will mention some of the typical landmarks used with computer vision.

Fukui [1981] used a diamond-shaped landmark and applied a least-squares method to find line segments in the image plane. Borenstein [1987] used a black rectangle with four white dots in the corners. Kabuka and Arenas [1987] used a half-white and half-black circle with a unique bar-code for each landmark. Magee and Aggarwal [1984] used a sphere with horizontal and vertical calibration circles to achieve three-dimensional localization from a single image. Other systems use reflective material patterns and strobed light to ease the segmentation and parameter extraction [Lapin, 1992; Mesaki and Masuda, 1992]. There are also systems that use active (i.e., LED) patterns to achieve the same effect [Fleury and Baron, 1992].

The accuracy achieved by the above methods depends on the accuracy with which the geometric parameters of the landmark images are extracted from the image plane, which in turn depends on the relative position and angle between the robot and the landmark. In general, the accuracy decreases with the increase in relative distance. Normally there is a range of relative angles in which good accuracy can be achieved, while accuracy drops significantly once the relative angle moves out of the "good" region.

There is also a variety of landmarks used in conjunction with non-vision sensors. Most often used are bar-coded reflectors for laser scanners. For example, currently ongoing work by Everett on the Mobile Detection Assessment and Response System (MDARS) [DeCorte, 1994] uses retro-reflectors, and so does the commercially available system from Caterpillar on their Self-Guided Vehicle [Gould, 1990]. The shape of these landmarks is usually unimportant. By contrast, a unique approach taken by Feng et al. [1992] used a circular landmark and applied an optical Hough transform to extract the parameters of the ellipse on the image plane in real time.

### 7.2.1 Global Vision

Yet another approach is the so-called global vision that refers to the use of cameras placed at fixed locations in a workspace to extend the local sensing available on board each AGV [Kay and Luo, 1993]. Figure 7.4 shows a block diagram of the processing functions for vehicle control using global vision.

In global vision methods, characteristic points forming a pattern on the mobile robot are identified and localized from a single view. A probabilistic method is used to select the most probable matching according to geometric characteristics of those percepts. From this reduced search space a prediction-verification loop is applied to identify and to localize the points of the pattern [Fleury and Baron, 1992]. One advantage of this approach is that it allows the operator to monitor robot operation at the same time.

### 7.3 Artificial Landmark Navigation Systems

Many systems use retroreflective barcodes as artificial landmarks, similar to the ones used in beacon navigation systems. However, in this book we distinguish between retroreflective bar-codes used as artificial landmarks and retroreflective poles used as "beacons." The reason is that if retroreflective markers (with or without bar-code) are attached to the walls of a room and their function is merely to aid in determining the location of the wall, then these markers do not


Figure 7.4: Block diagram of the processing functions for vehicle control using global vision. (Adapted from [Kay and Luo, 1993].)
function as beacons. By contrast, if markers are used on arbitrarily placed poles (even if the location of these poles is carefully surveyed), then they act as beacons. A related distinction is the method used for computing the vehicle's position: if triangulation is used, then the reflectors act as beacons.

### 7.3.1 MDARS Lateral-Post Sensor

Currently ongoing work by Everett on the Mobile Detection Assessment and Response System (MDARS) [Everett et al., 1994; DeCorte, 1994] uses passive reflectors in conjunction with a pair of fixed-orientation sensors on board the robot. This technique, called lateral-post detection, was incorporated on MDARS to significantly reduce costs by exploiting the forward motion of the robot for scanning purposes. Short vertical strips of 2.5 centimeters ( 1 in ) retroreflective tape are placed on various immobile objects (usually structural-support posts) on either side of a virtual path segment. The exact $x-y$ locations of these tape markers are encoded into the virtual path program. Installation takes only seconds, and since the flat tape does not protrude into the aisle at all, there is little chance of damage from a passing fork truck.

A pair of Banner Q85VR3LP retroreflective proximity sensors mounted on the turret of the Navmaster robot face outward to either side as shown in Figure 7.5 These inexpensive sensors respond to reflections from the tape markers along the edges of the route, triggering a "snapshot" virtual path instruction that records the current side-sonar range values. The longitudinal position of the platform is updated to the known marker coordinate, while lateral position is inferred from the sonar data, assuming both conditions fall within specified tolerances.

The accuracy of the marker correction is much higher (and therefore assigned greater credibility) than that of the lateral sonar readings due to the markedly different uncertainties associated with the respective targets. The polarized Banner sensor responds only to the presence of a retroreflector while ignoringeven hi ghly specular surrounding surfaces, whereas the ultrasonic energy from the sonar will echo back from any reflective surface encountered by its relatively wide beam. Protruding objects in the vicinity of the tape (quite common in a warehouse environment) result in a shorter measured range value than the reference distance for the marker itself. The


Figure 7.5: Polarized retroreflective proximity sensors are used to locate vertical strips of retroreflective tape attached to shelving support posts in the Camp Elliott warehouse installation of the MDARS security robot [Everett et al, 1994]. overall effect on $\mathrm{x}-\mathrm{y}$ bias is somewhat averaged out in the longrun, as each time the vehicle executes a 90 -degree course change the association of x - and y -components with tape versus sonar updates is interchanged.

### 7.3.2 Caterpillar Self Guided Vehicle

Caterpillar Industrial, Inc., Mentor, OH, manufactures a free-ranging AGV for materials handling that relies on a scanning laser triangulation scheme to provide positional updates to the vehicle's onboard odometry system. The Class-I laser rotates at 2 rpm to illuminate passive retroreflective bar-code targets affixed to walls or support columns at known locations up to 15 meters ( 50 ft ) away [Gould, 1990; Byrne et al., 1992]. The bar-codes serve to positively identify the reference target and eliminate ambiguities


Figure 7.6: Retroreflective bar-code targets spaced 10 to 15 meters ( 33 to 49 ft ) apart are used by the Caterpillar SGV to triangulate position. (Adapted from [Caterpillar, 1991a].) due to false returns from other specular surfaces within the operating area. An onboard computer calculates x -y position updates through simple triangulation to null out accumulated odometry errors (see Figure 7.6).

Some target occlusion problems have been experienced in exterior applications where there is heavy fog, as would be expected, and minor difficulties have been encountered as well during periods when the sun was low on the horizon [Byrne, 1993]. Caterpillar's Self Guided Vehicle (SGV) relies on dead reckoning under such conditions to reliably continue its route for distances of up to 10 meters ( 33 ft ) before the next valid fix.

The robot platform is a hybrid combination of tricycle and differential drive, employing two independent series-wound DC motors powering 45 -centimeter ( 18 in ) rear wheels through sealed gear-boxes [CATERPILLAR, 1991]. High-resolution resolvers attached to the single front wheel continuously monitor steering angle and distance traveled. A pair of mechanically scanned nearinfrared proximity sensors sweeps the path in front of the vehicle for potential obstructions. Additional near infrared sensors monitor the area to either side of the vehicle, while ultrasonic sensors cover the back.

### 7.3.3 Komatsu Ltd, Z-shaped landmark

Komatsu Ltd. in Tokyo, Japan, is a manufacturer of construction machines. One of Komatsu's research projects aims at developing an unmanned dump truck. As early as 1984, researchers at Komatsu Ltd. developed an unmanned electric car that could follow a previously taught path around the company's premises. The vehicle had two onboard computers, a directional gyrocompass, two incremental encoders on the wheels, and a metal


Figure 7.7: Komatsu's Z-shaped landmarks are located at 50-meter (164 ft) intervals along the planned path of the autonomous vehicle. (Courtesy of [Matsuda and Yoshikawa, 1989].) sensor which detected special landmarks along the planned path (see Figure 7.7).

The accuracy of the vehicle's dead-reckoning system (gyrocompass and encoders) was approximately two percent on the paved road and during straight-line motion only. The mechanical gyrocompass was originally designed for deep-sea fishing boats and its static direction accuracy was 1 degree. On rough terrain the vehicle's dead-reckoning error deteriorated notably. For example, running over a $40-\mathrm{millimeter}(1.5 \mathrm{in})$ height bump and subsequently traveling along a straight line for 50 meters ( 164 ft ), the vehicle's positioning error was $1.4 \mathrm{~m}(55 \mathrm{in})$. However, with the Z-shaped landmarks used in this project for periodic recalibration the positioning could be recalibrated to an accuracy of 10 centimeters ( 4 in ). The 3 meter (118 in) wide landmark was made of 50 millimeter ( 2 in ) wide aluminum strips sandwiched between two rubber sheets. In order to distinguish between "legitimate" metal markings of the landmark and between arbitrary metal objects, additional parallel line segments were used (see Figure 7.8). The metal markers used as landmarks in this experiment are resilient to contamination even in harsh environments. Water, dust, and lighting condition do not affect the readability of the metal sensor [Matsuda and Yoshikawa, 1989].


Figure 7.8: The Z-shaped landmark. Note the secondary lines parallel to the horizontal Z-stripes. The secondary lines help distinguish the marker from random metal parts on the road. (Courtesy of [Matsuda and Yoshikawa, 1989].)

Each Z-shaped landmark comprises three line segments. The first and third line segments are in parallel, and the second one is located diagonally between the parallel lines (see Figure7.9). During operation, a metal sensor located underneath the autonomous vehicle detects the three crossing points $P_{1}, P_{2}$, and $P_{3}$. The distances, $L_{1}$ and $L_{2}$, are measured by the incremetal encoders using odometry. After traversing the Z -shaped landmark, the vehicle's lateral deviation $\mathrm{X}_{2}$ at point $\mathrm{P}_{2}$ can be computed from

$$
\begin{equation*}
X_{2}=W\left(\frac{L_{1}}{L_{1}+L_{2}}-\frac{1}{2}\right) \tag{7.1}
\end{equation*}
$$

where $X_{2}$ is the lateral position error at point $P_{2}$ based on odometry.

The lateral position error can be corrected after passing through the third crossing point $P_{3}$. Note that for this correction method the exact location of the landmark along the line of travel does not have to be known. However, if the location of the landmark is known, then the vehicle's actual position at $P_{2}$ can be calculated easily [Matsuda et al., 1989].

The size of the Z-shaped landmark can be varied, according to the expected lateral error of the vehicle. Larger landmarks can be buried under the surface of paved roads for unmanned cars. Smaller landmarks can be installed under factory floor coating or under office carpet. Komatsu has developed such smaller Z-shaped landmarks for indoor robots and AGVs.


Figure 7.9: The geometry of the Z-shaped landmark lends itself to easy and unambiguous computation of the lateral position error $X_{2}$. (Courtesy of [Matsuda and Yoshikawa, 1989].)

### 7.4 Line Navigation

Another type of landmark navigation that has been widely used in industry is line navigation. Line navigation can be thought of as a continuous landmark, although in most cases the sensor used in this system needs to be very close to the line, so that the range of the vehicle is limited to the immediate vicinity of the line. There are different implementations for line navigation:

- Electromagnetic Guidance or Electromagnetic Leader Cable.
- Reflecting Tape Guidance (also called Optical Tape Guidance).
- Ferrite Painted Guidance, which uses ferrite magnet powder painted on the floor [Tsumura, 1986].

These techniques have been in use for many years in industrial automation tasks. Vehicles using these techniques are generally called Automatic Guided Vehicles (AGVs).

In this book we don't address these methods in detail, because they do not allow the vehicle to move freely - the main feature that sets mobile robots apart from AGVs. However, two recently introduced variations of the line navigation approach are of interest for mobile robots. Both techniques are based on the use of short-lived navigational markers (SLNM). The short-lived nature of the markers has the advantage that it is not necessary to remove the markers after use.

One typical group of applications suitable for SLNM are floor coverage applications. Examples are floor cleaning, lawn mowing, or floor surveillance. In such applications it is important for the robot to travel along adjacent paths on the floor, with minimal overlap and without "blank" spots. With the methods discussed here, the robot could conceivably mark the outside border of the path, and trace that border line in a subsequent run. One major limitation of the current state-of-the-art is that they permit only very slow travel speeds: on the order of under $10 \mathrm{~mm} / \mathrm{s}(0.4 \mathrm{in} / \mathrm{s})$.

### 7.4.1 Thermal Navigational Marker

Kleeman [1992], Kleeman and Russell [1993], and Russell [1993] report on a pyroelectric sensor that has been developed to detect thermal paths created by heating the floor with a quartz halogen bulb. The path is detected by a pyroelectric sensor based on lithium-tantalate. In order to generate a differential signal required for path following, the position of a single pyroelectric sensor is toggled between two sensing locations 5 centimeters ( 2 in ) apart. An aluminum enclosure screens the sensor from ambient infrared light and electromagnetic disturbances. The 70 W quartz halogen bulb used in this system is located 30 millimeters (1-3/16 in) above the floor.

The volatile nature of this path is both advantageous and disadvantageous: since the heat trail disappears after a few minutes, it also becomes more difficult to detect over time. Kleeman and Russell approximated the temperature distribution T at a distance d from the trail and at a time t after laying the trail as
$\mathrm{T}(\mathrm{d}, \mathrm{t})=\mathrm{A}(\mathrm{t}) \mathrm{e}^{-(\mathrm{d} / \mathrm{w})^{2}}$
where $A(t)$ is a time-variant intensity function of the thermal path.
In a controlled experiment two robots were used. One robot laid the thermal path at a speed of $10 \mathrm{~mm} / \mathrm{s}(0.4 \mathrm{in} / \mathrm{s})$, and the other robot followed that path at about the same speed. Using a control scheme based on a Kalman filter, thermal paths could be tracked up to 10 minutes after being laid on a vinyl tiled floor. Kleeman and Russell remarked that the thermal footprint of peoples' feet could contaminate the trail and cause the robot to lose track.

### 7.4.2 Volatile Chemicals Navigational Marker

This interesting technique is based on laying down an odor trail and using an olfactory ${ }^{1}$ sensor to allow a mobile robot to follow the trail at a later time. The technique was described by Deveza et al. [1993] and Russell et al. [1994], and the experimental system was further enhanced as described by Russell [1995a; 1995b] at Monash University in Australia. Russell's improved system comprises a custom-built robot (see Figure 7.10) equipped with an odor-sensing system. The sensor system uses

[^2]controlled flows of air to draw odorladen air over a sensor crystal. The quartz crystal is used as a sensitive balance to weigh odor molecules. The quartz crystal has a coating with a specific affinity for the target odorant; molecules of that odorant attach easily to the coating and thereby increase the total mass of the crystal. While the change of mass is extremely small, it suffices to change the resonant frequency of the crystal. A $68 \mathrm{HC} 11 \mathrm{mi}-$ croprocessor is used to count the crystal's frequency, which is in the kHz region. A change of frequency is indicative of odor concentration. In Russell's system two such sensors are mounted at a distance of 30 millimeters (1-3/16 in) from each other, to provide a differential signal that can then be used for path tracking.

For laying the odor trail, Russell used a modified felt-tip pen. The odor-


Figure 7.10: The odor-laying/odor-sensing mobile robot was developed at Monash University in Australia. The olfactory sensor is seen in front of the robot. At the top of the vertical boom is a magnetic compass. (Courtesy of Monash University). laden agent is camphor, dissolved in alcohol. When applied to the floor, the alcohol evaporates quickly and leaves a 10 millimeter ( 0.4 in ) wide camphor trail. Russell measured the response time of the olfactory sensor by letting the robot cross an odor trail at angles of 90 and 20 degrees. The results of that test are shown in Figure 7.11. Currently, the foremost limitation of Russell's volatile chemical navigational marker is the robot's slow speed of $6 \mathrm{~mm} / \mathrm{s}(1 / 4 \mathrm{in} / \mathrm{s})$.


Figure 7.11: Odor sensor response as the robot crosses a line of camphor set at angle of a. $90^{\circ}$ and b. $20^{\circ}$ to the robot path. The robots speed was $6 \mathrm{~mm} / \mathrm{s}(1 / 4 \mathrm{in} / \mathrm{s})$ in both tests. (Adapted with permission from Russell [1995].)

### 7.5 Summary

Artificial landmark detection methods are well developed and reliable. By contrast, natural landmark navigation is not sufficiently developed yet for reliable performance under a variety of conditions. A survey of the market of commercially available natural landmark systems produces only a few. One is TRC's vision system that allows the robot to localize itself using rectangular and circular ceiling lights [King and Weiman, 1990]. Cyberworks has a similar system [Cyberworks]. It is generally very difficult to develop a feature-based landmark positioning system capable of detecting different natural landmarks in different environments. It is also very difficult to develop a system that is capable of using many different types of landmarks.

We summarize the characteristics of landmark-based navigation as follows:

- Natural landmarks offer flexibility and require no modifications to the environment.
- Artificial landmarks are inexpensive and can have additional information encoded as patterns or shapes.
- The maximal distance between robot and landmark is substantially shorter than in active beacon systems.
- The positioning accuracy depends on the distance and angle between the robot and the landmark. Landmark navigation is rather inaccurate when the robot is further away from the landmark. A higher degree of accuracy is obtained only when the robot is near a landmark.
- Substantially more processing is necessary than with active beacon systems.
- Ambient conditions, such as lighting, can be problematic; in marginal visibility, landmarks may not be recognized at all or other objects in the environment with similar features can be mistaken for a legitimate landmark.
- Landmarks must be available in the work environment around the robot.
- Landmark-based navigation requires an approximate starting location so that the robot knows where to look for landmarks. If the starting position is not known, the robot has to conduct a timeconsuming search process.
- A database of landmarks and their location in the environment must be maintained.
- There is only limited commercial support for this type of technique.


## Chapter 8 <br> Map-based Positioning

Map-based positioning, also known as "map matching," is a technique in which the robot uses its sensors to create a map of its local environment. This local map is then compared to a global map previously stored in memory. If a match is found, then the robot can compute its actual position and orientation in the environment. The prestored map can be a CAD model of the environment, or it can be constructed from prior sensor data.

The basic procedure for map-based positioning is shown in Figure 8.1.


Figure 8.1: General procedure for map-based positioning.

The main advantages of map-based positioning are as follows.

- This method uses the naturally occurring structure of typical indoor environments to derive position information without modifying the environment.
- Map-based positioning can be used to generate an updated map of the environment. Environment maps are important for other mobile robot tasks, such as global path planning or the avoidance of "local minima traps" in some local obstacle avoidance methods.
- Map-based positioning allows a robot to learn a new environment and to improve positioning accuracy through exploration.

Disadvantages of map-based positioning are the specific requirements for satisfactory navigation. For example, map-based positioning requires that:

- there be enough stationary, easily distinguishable features that can be used for matching,
- the sensor map be accurate enough (depending on the tasks) to be useful,
- a significant amount of sensing and processing power be available.

One should note that currently most work in map-based positioning is limited to laboratory settings and to relatively simple environments.

### 8.1 Map Building

There are two fundamentally different starting points for the map-based positioning process. Either there is a pre-existing map, or the robot has to build its own environment map. Rencken [1993] defined the map building problem as the following: "Given the robot's position and a set of measurements, what are the sensors seeing?" Obviously, the map-building ability of a robot is closely related to its sensing capacity.

Talluri and Aggarwal [1993] explained:
"The position estimation strategies that use map-based positioning rely on the robot's ability to sense the environment and to build a representation of it, and to use this representation effectively and efficiently. The sensing modalities used significantly affect the map making strategy. Error and uncertainty analyses play an important role in accurate position estimation and map building. It is important to take explicit account of the uncertainties; modeling the errors by probability distributions and using Kalman filtering techniques are good ways to deal with these errors explicitly."

Talluri and Aggarwal [1993] also summarized the basic requirements for a map:
"The type of spatial representation system used by a robot should provide a way to incorporate consistently the newly sensed information into the existing world model. It should also provide the necessary information and procedures for estimating the position and pose of the robot in the environment. Information to do path planning, obstacle avoidance, and other navigation tasks must also be easily extractable from the built world model."

Hoppen et al. [1990] listed the three main steps of sensor data processing for map building:

1. Feature extraction from raw sensor data.
2. Fusion of data from various sensor types.
3. Automatic generation of an environment model with different degrees of abstraction.

And Crowley [1989] summarized the construction and maintenance of a composite local world model as a three-step process:

1. Building an abstract description of the most recent sensor data (a sensor model).
2. Matching and determining the correspondence between the most recent sensor models and the current contents of the composite local model.
3. Modifying the components of the composite local model and reinforcing or decaying the confidences to reflect the results of matching.

A problem related to map-building is "autonomous exploration." In order to build a map, the robot must explore its environment to map uncharted areas. Typically it is assumed that the robot begins its exploration without having any knowledge of the environment. Then, a certain motion strategy is followed which aims at maximizing the amount of charted area in the least amount of
time. Such a motion strategy is called exploration strategy, and it depends strongly on the kind of sensors used. One example for a simple exploration strategy based on a lidar sensor is given by [Edlinger and Puttkamer, 1994].

### 8.1.1 Map-Building and Sensor Fusion

Many researchers believe that no single sensor modality alone can adequately capture all relevant features of a real environment. To overcome this problem, it is necessary to combine data from different sensor modalities, a process known as sensor fusion. Here are a few examples:

- Buchberger et al. [1993] and Jörg [1994; 1995] developed a mechanism that utilizes heterogeneous information obtained from a laser-radar and a sonar system in order to construct a reliable and complete world model.
- Courtney and Jain [1994] integrated three common sensing sources (sonar, vision, and infrared) for sensor-based spatial representation. They implemented a feature-level approach to sensor fusion from multisensory grid maps using a mathematical method based on spatial moments and moment invariants, which are defined as follows:

The two-dimensional $(p+q)$ th order spacial moments of a grid map $G(x, y)$ are defined as

$$
\begin{equation*}
m_{p q}=\sum_{x} \sum_{y} x^{p} y^{q} G(x, y) \quad p, q=0,1,2, . . \tag{8.1}
\end{equation*}
$$

Using the centroid, translation-invariant central moments (moments don't change with the translation of the grid map in the world coordinate system) are formulated:

$$
\begin{equation*}
\mu_{p q}=\sum_{x} \sum_{y}(x-\bar{x})^{p}(y-\bar{y})^{q} G(x, y) \tag{8.2}
\end{equation*}
$$

From the second- and third-order central moments, a set of seven moment invariants that are independent of translation, rotation, and scale can be derived. A more detailed treatment of spatial moments and moment invariants is given in [Gonzalez and Wintz, 1977].

### 8.1.2 Phenomenological vs. Geometric Representation, Engelson and McDermott [1992]

Most research in sensor-based map building attempts to minimize mapping errors at the earliest stage - when the sensor data is entered into the map. Engelson and McDermott [1992] suggest that this methodology will reach a point of diminishing returns, and hence further research should focus on explicit error detection and correction. The authors observed that the geometric approach attempts to build a more-or-less detailed geometric description of the environment from perceptual data. This has the intuitive advantage of having a reasonably well-defined relation to the real world. However, there is, as yet, no truly satisfactory representation of uncertain geometry, and it is unclear whether the volumes of information that one could potentially gather about the shape of the world are really useful.

To overcome this problem Engelson and McDermott suggested the use of a topological approach that constitutes a phenomenological representation of the robot's potential interactions with the world, and so directly supports navigation planning. Positions are represented relative to local
reference frames to avoid unnecessary accumulation of relative errors. Geometric relations between frames are also explicitly represented. New reference frames are created whenever the robot's position uncertainty grows too high; frames are merged when the uncertainty between them falls sufficiently low. This policy ensures locally bounded uncertainty. Engelson and McDermott showed that such error correction can be done without keeping track of all mapping decisions ever made. The methodology makes use of the environmental structure to determine the essential information needed to correct mapping errors. The authors also showed that it is not necessary for the decision that caused an error to be specifically identified for the error to be corrected. It is enough that the type of error can be identified. The approach has been implemented only in a simulated environment, where the effectiveness of the phenomenological representation was demonstrated.

### 8.2 Map Matching

One of the most important and challenging aspects of map-based navigation is map matching, i.e., establishing the correspondence between a current local map and the stored global map [Kak et al., 1990]. Work on map matching in the computer vision community is often focused on the general problem of matching an image of arbitrary position and orientation relative to a model (e.g., [Talluri and Aggarwal, 1993]). In general, matching is achieved by first extracting features, followed by determination of the correct correspondence between image and model features, usually by some form of constrained search [Cox, 1991].

Such matching algorithms can be classified as either icon-based or feature-based. Schaffer et al. [1992] summarized these two approaches:
"Iconic-based pose estimation pairs sensory data points with features from the map, based on minimum distance. The robot pose is solved for that minimizes the distance error between the range points and their corresponding map features. The robot pose is solved [such as to] minimize the distance error between the range points and their corresponding map features. Based on the new pose, the correspondences are recomputed and the process repeats until the change in aggregate distance error between points and line segments falls below a threshold. This algorithm differs from the feature-based method in that it matches every range data point to the map rather than corresponding the range data into a small set of features to be matched to the map. The feature-based estimator, in general, is faster than the iconic estimator and does not require a good initial heading estimate. The iconic estimator can use fewer points than the feature-based estimator, can handle less-than-ideal environments, and is more accurate. Both estimators are robust to some error in the map."

Kak et al. [1990] pointed out that one problem in map matching is that the sensor readings and the world model may be of different formats. One typical solution to this problem is that the approximate position based on odometry is utilized to generate (from the prestored global model), an estimated visual scene that would be "seen" by robot. This estimated scene is then matched against the actual scene viewed by the onboard sensors. Once the matches are established between the features of the two images (expected and actual), the position of the robot can be estimated with reduced uncertainty. This approach is also supported by Rencken [1994], as will be discussed in more detail below.

In order to match the current sensory data to the stored environment model reliably, several features must be used simultaneously. This is particularly true for a range image-based system since the types of features are limited to a range image map. Long walls and edges are the most commonly used features in a range image-based system. In general, the more features used in one match, the less likely a mismatch will occur, but the longer it takes to process. A realistic model for the odometry and its associated uncertainty is the basis for the proper functioning of a map-based positioning system. This is because the feature detection as well as the updated position calculation rely on odometric estimates [Chenavier and Crowley, 1992].

### 8.2.1 Schiele and Crowley [1994]

Schiele and Crowley [1994] discussed different matching techniques for matching two occupancy grids. The first grid is the local grid that is centered on the robot and models its vicinity using the most recent sensor readings. The second grid is a global model of the environment furnished either by learning or by some form of computer-aided design tool. Schiele and Crowley propose that two representations be used in environment modeling with sonars: parametric primitives and an occupancy grid. Parametric primitives describe the limits of free space in terms of segments or surfaces defined by a list of parameters. However, noise in the sensor signals can make the process of grouping sensor readings to form geometric primitives unreliable. In particular, small obstacles such as table legs are practically impossible to distinguish from noise.

Schiele and Crowley discuss four different matches:

- Matching segment to segment as realized by comparing segments in (1) similarity in orientation, (2) collinearity, and (3) overlap.
- Matching segment to grid.
- Matching grid to segment.
- Matching grid to grid as realized by generating a mask of the local grid. This mask is then transformed into the global grid and correlated with the global grid cells lying under this mask. The value of that correlation increases when the cells are of the same state and decreases when the two cells have different states. Finally finding the transformation that generates the largest correlation value.

Schiele and Crowley pointed out the importance of designing the updating process to take into account the uncertainty of the local grid position. The correction of the estimated position of the robot is very important for the updating process particularly during exploration of unknown environments.

Figure 8.2 shows an example of one of the experiments with the robot in a hallway. Experimental results obtained by Schiele and Crowley show that the most stable position estimation results are obtained by matching segments to segments or grids to grids.

### 8.2.2 Hinkel and Knieriemen [1988] — The Angle Histogram

Hinkel and Knieriemen [1988] from the University of Kaiserslautern, Germany, developed a worldmodeling method called the Angle Histogram. In their work they used an in-house developed lidar mounted on their mobile robot Mobot III. Figure 8.3 shows that lidar system mounted on Mobot III's


Figure 8.2: Schiele and Crowley's robot models its position in a hallway.
a. Raw ultrasonic range data projected onto external coordinates around the robot.
b. Local grid and the edge segments extracted from this grid.
c. The robot with its uncertainty in estimated position within the global grid.
d. The local grid imposed on the global grid at the position and orientation of best correspondence.
(Reproduced and adapted from [Schiele and Crowley, 1994].)
successor Mobot IV. (Note that the photograph in Figure 8.3 is very recent; it shows Mobot IV on the left, and Mobot $V$, which was built in 1995, on the right. Also note that an ORS-1 lidar from ESP, discussed in Sec. 4.2.2, is mounted on Mobot $V$.)

A typical scan from the in-house lidar is shown in Figure 8.4. The similarity between the scan quality of the University of Kaiserslautern lidar and that of the ORS-1 lidar (see Fig. 4.32a in Sec. 4.2.6) is striking.

The angle histogram method works as follows. First, a 360 degree scan of the room is taken with the lidar, and the resulting "hits" are recorded in a map. Then the algorithm measures the relative angle $\delta$ between any two adjacent hits (see Figure 8.5). After compensating for noise in the readings (caused by the inaccuracies in position between adjacent hits), the angle histogram shown in Figure 8.6a can be built. The uniform direction of the main walls are clearly visible as peaks in the angle histogram. Computing the histogram modulo $\pi$ results in only two main peaks: one for each pair of parallel walls. This algorithm is very robust with regard to openings in the walls, such as doors and windows, or even cabinets lining the walls.


Figure 8.3: Mobot IV (left) and Mobot $V$ (right) were both developed and built at the University of Kaiserslautern. The different Mobot models have served as mobile robot testbeds since the mid-eighties. (Courtesy of the University of Kaiserslautern.)

After computing the angle histogram, all angles of the hits can be normalized, resulting in the


Figure 8.4: A typical scan of a room, produced by the University of Kaiserslautern's in-house developed lidar system. (Courtesy of the University of Kaiserslautern.)
representation shown in Figure 8.6b. After this transformation, two additional histograms, one for the x - and one for the y -direction can be constructed. This time, peaks show the distance to the walls in x and y direction. During operation, new orientation and position data is updated at a rate of 4 Hz . (In conversation with Prof. Von Puttkamer, Director of the Mobile Robotics Laboratory at the University of Kaiserslautern, we learned that this algorithm had since been improved to yield a reliable accuracy of $0.5^{\circ}$.)

### 8.2.3 Weiß, Wetzler, and Puttkamer - More on the Angle Histogram

Weiß et al. [1994] conducted further experiments with the angle histogram method. Their work aimed at matching rangefinder scans from different locations. The purpose of this work was to compute the translational and rotational displacement of a mobile robot that had traveled during subsequent scans.

The authors pointed out that an angle


Figure 8.5: Calculating angles for the angle histogram. (Courtesy of [Weiß et al., 1994].) histogram is mostly invariant against rotation and translation. If only the orientation is altered between two scans, then the angle histogram of the second scan will show only a phase shift when compared to the first. However, if the position of the robot is altered, too, then the distribution of angles will also change. Nonetheless, even in that case the new angle histogram will still be a representation of the distribution of directions in the new scan. Thus, in the new angle histogram the same direction that appeared to be the local maximum in the old angle histogram will still appear as a maximum, provided the robot's displacement between the two scans was sufficiently small.


Figure 8.6: Readings from a rotating laser scanner generate the contours of a room.
a. The angle histogram allows the robot to determine its orientation relative to the walls.
b. After normalizing the orientation of the room relative to the robot, an $x-y$ histogram can be built form the same data points. (Adapted from [Hinkel and Knieriemen, 1988].)

Experiments show that this approach is highly stable against noise, and even moving obstacles do not distort the result as long as they do not represent the majority of matchable data. Figure 8.7a shows two scans taken from two different locations. The second scan represents a rotation of +43 degrees, a translation in x-direction of +14 centimeters and a translation in y-direction of +96 centimeters. Figure 8.7 b shows the angle histogram associated with the two positions. The maxima for the main directions are -24 and 19 degrees, respectively. These angles correspond to the rotation of the robot relative to the local main direction. One can thus conclude that the rotational displacement of the robot was $19^{\circ}-\left(-24^{\circ}\right)=+43^{\circ}$. Furthermore, rotation of the first and second range plot by -24 and 19 degrees, respectively, provides the normalized x - and y-plots shown in Fig 8.7c. The cross correlation of the x translation is shown in Figure 8.7d. The maximum occurs at -35 centimeters, which corresponds to -14 centimeters in the rotated scan (Fig. 8.7a). Similarly, the y-translation can be found to be +98 centimeters in the rotated scan. Figure 8.5 e shows the result of scan matching after making all rotational and translational corrections.


Definition
A cross-correlation is defined as
$c(y)=\lim _{x \rightarrow \infty} \frac{1}{2 X} \int_{-x}^{x} f(x) g(x+y) d x$.
$\mathrm{c}(\mathrm{y})$ is a measure of the cross-correlation between two stochastic functions regarding the phase shift $y$. The cross-correlation $c(y)$ will have an absolute maximum at $s$, if $f(x)$ is equal to $g(x+s)$. (Courtesy of [Weiß et al., 1994].)

### 8.2.4 Siemens' Roamer

Rencken [1993; 1994] at the Siemens Corporate Research and Development Center in Munich, Germany, has made substantial contributions toward solving the boot strap problem resulting from the uncertainty in position and environment. This problem exists when a robot must move around in an unknown environment, with uncertainty in its odometry-derived position. For example, when building a map of the environment, all measurements are necessarily relative to the carrier of the sensors (i.e., the mobile robot). Yet, the position of the robot itself is not known exactly, because of the errors accumulating in odometry.

Rencken addresses the problem as follows: in order to represent features "seen" by its 24 ultrasonic sensors, the robot constructs hypotheses about these features. To account for the typically unreliable information from ultrasonic sensors, features can be classified as hypothetical, tentative, or confirmed. Once a feature is confirmed, it is used for constructing the map as shown in Figure 8.8. Before the map can be updated, though, every new data point must be associated with either a plane, a corner, or an edge (and some variations of these features). Rencken devices a "hypothesis tree" which is a data structure that allows tracking of different hypotheses until a sufficient amount of data has been accumulated to make a final decision.

One further important aspect in making this decision is feature visibility. Based on internal models for different features, the robot's decisions are aided by a routine check on visibility. For example, the visibility of edges is smaller than that of corners. The visibility check further reduces the uncertainty and improves the robustness of the algorithm.


Figure 8.8: The basic map-building algorithm maintains a hypothesis tree for the three sensor reading categories: hypothetical, tentative, and confirmed. (Adapted from [Rencken, 1994].)

Based on the above methods, Rencken [1993] summarizes his method with the following procedure:

1. Predict the robot's position using odometry.
2. Predict the associated covariance of this position estimate.
3. Among the set of given features, test which feature is visible to which sensor and predict the measurement.
4. Compare the predicted measurements to the actual measurements.
5. Use the error between the validated and predicted measurements to estimate the robot's position.
6. The associated covariance of the new position estimate is also determined.

The algorithm was implemented on Siemens' experimental robot Roamer (see Fig. 8.9). In an endurance experiment, Roamer traveled through a highly cluttered office environment for approximately 20 minutes. During this time, the robot updated its internal position only by means of odometry and its map-building capabilities. At a relatively slow travel speed of $12 \mathrm{~cm} / \mathrm{s}(43 / 4 \mathrm{in} / \mathrm{s})$ Roamer's position accuracy was periodically recorded, as shown in Table 8.1.

Table 8.1: Position and orientation errors of Siemens' Roamer robot in an map-building "endurance test." (Adapted from [Rencken, 1994].)

| Time [min:sec] | Pos. Error <br> $[\mathrm{cm}] ~(i n)$ | Orientation <br> error [ ${ }^{\circ}$ ] |
| :---: | :---: | :---: |
| $5: 28$ | $5.8(2-1 / 4)$ | -7.5 |
| $11: 57$ | $5.3(2)$ | -6.2 |
| $14: 53$ | $5.8(2-1 / 4)$ | 0.1 |
| $18: 06$ | $4.0(1-1 / 2)$ | -2.7 |
| $20: 12$ | $2.5(1)$ | 3.0 |



Figure 8.9: Siemens' Roamer robot is equipped with 24 ultrasonic sensors. (Courtesy of Siemens).

### 8.2.5 Bauer and Rencken: Path Planning for Feature-based Navigation

Bauer and Rencken [1995] at Siemens Corporate Research and Development Center in Munich, Germany are developing path planning methods that assist a robot in feature-based navigation. This work extends and supports Rencken's feature-based navigation method described in Section 8.2.4, above.

One problem with all feature-based positioning systems is that the uncertainty about the robot's position grows if there are no suitable features that can be used to update the robot's position. The problem becomes even more severe if the features are to be detected with ultrasonic sensors, which are known for their poor angular resolution. Readings from ultrasonic sensors are most useful when the sound waves are being reflected from a wall that is normal to the incident waves, or from distinct corners.

During operation the robot builds a list of expected sonar measurements, based on earlier measurements and based on the robot's change of location derived from dead-reckoning. If actual sonar readings match the expected ones, these readings are used to estimate the robot's actual position. Non-matching readings are used to define new hypothesis about surrounding features, called tentative features. Subsequent reading will either confirm tentative features or remove them. The existence of confirmed features is important to the system because each confirmed feature offers essentially the benefits of a navigation beacon. If further subsequent readings match confirmed features, then the robot can use this data to reduce its own growing position uncertainty. Bauer and Rencken show that the growing uncertainty in the robot's position (usually visualized by so-called "uncertainty ellipses") is reduced in one or two directions, depending on whether a new reading matches a confirmed feature that is a line-type (see cases a. and b. in Fig. 8.10) or point-type (case c. in Fig. 8.10).


Figure 8.10: Different features can reduce the size of the robot's uncertainty ellipse in one or two directions.
a, c: Walls and corners reduce uncertainty in one direction
b.: Two adjacent walls at right angles reduce uncertainty in two directions.
(Courtesy of [Bauer and Rencken, 1995]).

One novel aspect of Bauer and Rencken's approach is a behavior that steers the robot in such a way that observed features stay in view longer and can thus serve as a navigation reference longer. Fig. 8.11 demonstrates this principle. In the vicinity of a confirmed feature "straight wall" (Fig. 8.11a), the robot will be steered alongside that wall; in the vicinity of a confirmed feature "corner" (Fig. 8.11b) the robot will be steered around that corner.

Experimental results with Bauer and Rencken's method are shown in Figures 8.12 and 8.13. In the first run (Fig. 8.12) the robot was programmed to explore its environment while moving from point A in the office in the upper left-hand corner to point E in the office in the lower right-hand corner. As the somewhat erratic trajectory shows, the robot backed up frequently in order to decrease its position uncertainty (by confirming more features). The actual position accuracy of the robot was mea-
 based positioning
a. Near walls, the robot tries to stay parallel to the wall for as long as possible.
b. Near corners the robot tries to trun around the corner for as long as possible.
(Courtesy of [Bauer and Rencken, 1995]).


Figure 8.12: Actual office environment and robot's trajectory during the exploratory travel phase. (Courtesy of [Bauer and Rencken, 1995]).


Figure 8.13: Gathered features and robot's return trajectory (Courtesy of [Bauer and Rencken, 1995]).
sured by hand at control points A through E, the results are listed in Table 8.2.

When the robot was programmed to return to its starting position, the resulting path looked much smoother. This is because of the many features that were stored during the outbound trip.

Table 8.2: Hand-measured position error of the robot at intermediate way-points during the exploration phase (Adapted from [Bauer and Rencken, 1995]).

| Point | Absolute $x, y-$ <br> coordinates $[\mathrm{cm}]$ | Pos. Error <br> $[\mathrm{cm}](\mathrm{in})$ | Orient. <br> Error $\left[{ }^{\circ}\right]$ |
| :---: | :---: | :---: | :---: |
| A | $(0,0)$ | $2.3(7 / 8)$ | 0.7 |
| B | $(150,-500)$ | $5.7(2-1 / 4)$ | 1.9 |
| C | $(1000,-500)$ | $9.1(3-1 / 2)$ | 5.3 |
| D | $(1800,-500)$ | $55.8(22)$ | 5.9 |
| E | $(1800,-800)$ | $63.2(25)$ | 6.8 |

### 8.3 Geometric and Topological Maps

In map-based positioning there are two common representations: geometric and topological maps. A geometric map represents objects according to their absolute geometric relationships. It can be a grid map, or a more abstracted map, such as a line map or a polygon map. In map-based positioning, sensor-derived geometric maps must be matched against a global map of a large area. This is often a formidable difficulty because of the robot's position error. By contrast, the topological approach is based on recording the geometric relationships between the observed features rather than their absolute position with respect to an arbitrary coordinate frame of reference. The resulting presentation takes the form of a graph where the nodes represent the observed features and the edges represent the relationships between the features. Unlike geometric maps, topological maps can be built and maintained without any estimates for the position of the robot. This means that the errors in this representation will be independent of any errors in the estimates for the robot position [Taylor, 1991]. This approach allows one to integrate large area maps without suffering from the accumulated odometry position error since all connections between nodes are relative, rather than absolute. After the map has been established, the positioning process is essentially the process of matching a local map to the appropriate location on the stored map.

### 8.3.1 Geometric Maps for Navigation

There are different ways for representing geometric map data. Perhaps the simplest way is an occupancy grid-based map. The first such map (in conjunction with mobile robots) was the Certainty Grid developed by Moravec and Elfes, [1985]. In the Certainty Grid approach, sensor readings are placed into the grid by using probability profiles that describe the algorithm's certainty about the existence of objects at individual grid cells. Based on the Certainty Grid approach, Borenstein and Koren [1991] refined the method with the Histogram Grid, which derives a pseudo-probability distribution out of the motion of the robot [Borenstein and Koren, 1991]. The Histogram Grid method is now widely used in many mobile robots (see for example [Buchberger et al., 1993; Congdon et al., 1993; Courtney and Jain, 1994; Stuck et al., 1994; Wienkop et al., 1994].)

A measure of the goodness of the match between two maps and a trial displacement and rotation is found by computing the sum of products of corresponding cells in the two maps [Elfes, 1987]. Range measurements from multiple points of view are symmetrically integrated into the map. Overlapping empty volumes reinforce each other and serve to condense the range of the occupied volumes. The map definition improves as more readings are added. The method deals effectively with clutter and can be used for motion planning and extended landmark recognition.

The advantages of occupancy grid-based maps are that they:

- allow higher density than stereo maps,
- require less computation and can be built more quickly,
- allow for easy integration of data from different sensors, and
- can be used to express statistically the confidence in the correctness of the data [Raschke and Borenstein, 1990].

The disadvantages of occupancy grid-based maps are that they:

- have large uncertainty areas associated with the features detected,
- have difficulties associated with active sensing [Talluri and Aggarwal, 1993],
- have difficulties associated with modeling of dynamic obstacles, and
- require a more complex estimation process for the robot vehicle [Schiele and Crowley, 1994].

In the following sections we discuss some specific examples for occupancy grid-based map matching.

### 8.3.1.1 Cox [1991]

One typical grid-map system was implemented on the mobile robot Blanche [Cox, 1991]. This positioning system is based on matching a local grid map to a global line segment map. Blanche is designed to operate autonomously within a structured office or factory environment without active or passive beacons. Blanche's positioning system consists of :

- an a priori map of its environment, represented as a collection of discrete line segments in the plane,
- a combination of odometry and a rotating optical range sensor to sense the environment,
- an algorithm for matching the sensory data to the map, where matching is constrained by assuming that the robot position is roughly known from odometry, and
- an algorithm to estimate the precision of the corresponding match/correction that allows the correction to be combined optimally (in a maximum likelihood sense) with the current odometric position to provide an improved estimate of the vehicle's position.

The operation of Cox's map-matching algorithm (item 2, above) is quite simple. Assuming that the sensor hits are near the actual objects (or rather, the lines that represent the objects), the distance between a hit and the closest line is computed. This is done for each point, according to the procedure in Table 8.3 (from [Cox, 1991]).

Table 8.3: Procedure for implementing Cox's [1991] map-matching algorithm .

1. For each point in the image, find the line segment in the model that is nearest to the point. Call this the target.
2. Find the congruence that minimizes the total squared distance between the image points and their target lines.
3. Move the points by the congruence found in step 2.
4. Repeat steps 1 to 3 until the procedure converges.

Figure 8.14 shows how the algorithm works on a set of real data. Figure 8.14 a shows the line model of the contours of the office environment (solid lines). The dots show hits by the range sensor. This scan was taken while the robot's position estimate was offset from its true position by 2.75 meters ( 9 ft ) in the x -direction and 2.44 meters ( 8 ft ) in the y -direction. A very small orientation error was also present. After running the map-matching procedure in Table 8.3, the robot corrected its internal position, resulting in the very good match between sensor data and line model, shown in Figure 8.14 b. In a longer run through corridors and junctions Blanche traveled at various slow speeds, on the order of $5 \mathrm{~cm} / \mathrm{s}(2 \mathrm{in} / \mathrm{s})$. The maximal deviation of its computed position from the actual position was said to be 15 centimeters ( 6 in ).


Figure 8.14: Map and range data a. before registration and b. after registration. (Reproduced and adapted from [Cox, 1991], © 1991 IEEE.)

## Discussion

With the grid-map system used in Blanche, generality has been sacrificed for robustness and speed. The algorithm is intrinsically robust against incompleteness of the image. Incompleteness of the model is dealt with by deleting any points whose distance to their target segments exceed a certain limit. In Cox's approach, a reasonable heuristic used for determining correspondence is the minimum Euclidean distance between the model and sensed data. Gonzalez et al. [1992] comment that this assumption is valid only as long as the displacement between the sensed data and the model is sufficiently small. However, this minimization problem is inherently non-linear but is linearized assuming that the rotation angle is small. To compensate for the error introduced due to linearization, the computed position correction is applied to the data points, and the process is repeated until no significant improvement can be obtained [Jenkin et al., 1993].

### 8.3.1.2 Crowley [1989]

Crowley's [1989] system is based on matching a local line segment map to a global line segment map. Crowley develops a model for the uncertainty inherent in ultrasonic range sensors, and he describes a method for the projection of range measurements onto external Cartesian coordinates. Crowley develops a process for extracting line segments from adjacent collinear range measurements, and he presents a fast algorithm for matching these line segments to a model of the geometric limits for the free-space of the robot. A side effect of matching sensor-based observations to the model is a correction to the estimated position of the robot at the time that the observation was made. The projection of a segment into the external coordinate system is based on the estimate of the position of the vehicle. Any uncertainty in the vehicle's estimated position must be included in the uncertainty of the segment before matching can proceed. This uncertainty affects both the position and orientation of the line segment. As each segment is obtained from the sonar data, it is matched to the composite model. Matching is a process of comparing each of the segments in the composite local
model against the observed segment, to allow detection of similarity in orientation, collinearity, and overlap. Each of these tests is made by comparing one of the parameters in the segment representation:
a. Orientation The square of the difference in orientation of the two candidates must be smaller than the sum of the variances.
b. Alignment The square of the difference of the distance from the origin to the two candidates must be smaller than the sum of the corresponding variance.
c. Over lap The difference of the distance between centerpoints to the sum of the half lengths must be smaller than a threshold.

The longest segment in the composite local model which passes all three tests is selected as the matching segment. The segment is then used to correct the estimated position of the robot and to update the model. An explicit model of uncertainty using covariance and Kalman filtering provides a tool for integrating noisy and imprecise sensor observations into the model of the geometric limits for the free space of a vehicle. Such a model provides a means for a vehicle to maintain an estimate of its position as it travels, even in the case where the environment is unknown.

Figure 8.15 shows the model of the ultrasonic range sensor and its uncertainties (shown as the hatched area A). The length of A is given by the uncertainties in robot orientation $\sigma_{w}$ and the width is given by the uncertainty in depth $\sigma_{\mathrm{D}}$. This area is approximated by an ellipse with the major and minor axis given by $\sigma_{w}$ and $\sigma_{D}$.


Figure 8.15: Model of the ultrasonic range sensor and its uncertainties. (Adapted from [Crowley, 1989].)

Figure 8.16 shows a vehicle with a circular uncertainty in position of 40 centimeters ( 16 in ) detecting a line segment. The ultrasonic readings are illustrated as circles with a radius determined by its uncertainty as defined in Figure 8.15. The detected line segment is illustrated by a pair of parallel lines. (The actual line segment can fall anywhere between the two lines. Only uncertainties associated with sonar readings are considered here.)

Figure 8.16 b shows the segment after the uncertainty in the robot's position has been added to the segment uncertainties. Figure 8.16 c shows the uncertainty in position after correction by matching a model segment. The position uncertainty of the vehicle is reduced to an ellipse with a minor axis of approximately 8 centimeters ( 3.15 in ).

In another experiment, the robot was placed inside the simple environment shown in Figure 8.17. Segment 0 corresponds to a wall covered with a textured wall-paper. Segment 1 corresponds to a metal cabinet with a sliding plastic door. Segment 2 corresponds to a set of chairs pushed up against


Figure 8.16:
a. A vehicle with a position uncertainty of 40 cm ( 15.7 in ), as shown by the circle around the centerpoint (cross), is detecting a line segment.
b. The boundaries for the line segment grow after adding the uncertainty for the robot's position.
c. After correction by matching the segment boundaries with a stored map segment, the uncertainty of the robot's position is reduced to about 8 cm ( 3.15 in ) as shown by the squat ellipse around the robot's center (cross). Courtesy of [Crowley, 1989].


Figure 8.17: Experimental setup for testing Crowley's map-matching method. Initially, the robot is intentionally set-off from the correct starting position.
two tables. The robot system has no a priori knowledge of its environment. The location and orientation at which the system was started were taken as the origin and x -axis of the world coordinate system. After the robot has run three cycles of ultrasonic acquisition, both the estimated position and orientation of the vehicle were set to false values. Instead of the correct position ( $x=0, y=0$, and $\theta=0$ ), the position was set to $x=0.10 \mathrm{~m}, \mathrm{y}=0.10 \mathrm{~m}$ and the orientation was set to 5 degrees. The uncertainty was set to a standard deviation of 0.2 meters in x and y , with a uncertainty in orientation of 10 degrees. The system was then allowed to detect the "wall" segments around it. The resulting estimated position and covariance is listed in Table 8.4].

Table 8.3: Experimental results with Crowley's map-matching method. Although initially placed in an incorrect position, the robot corrects its position error with every additional wall segment scanned.
$\left.\begin{array}{|l|ll||}\hline \text { Initial estimated position (with deliberate initial error) } & x, y, \theta=(0.100,0.100,5.0) \\ \text { Covariance } & 0.040 & 0.000 \\ & 0.000 \\ & 0.000 & 0.040 \\ 0.000 \\ \hline \text { After match with segment 0 } & & \\ \text { estimated position: } & x, y, \theta=(0.102,0.019,1.3\end{array}\right)$

### 8.3.1.3 Adams and von Flüe

The work by Adams and von Flüe follows the work by Leonard and Durrant-Whyte [1990] in using an approach to mobile robot navigation that unifies the problems of obstacle detection, position estimation, and map building in a common multi-target tracking framework. In this approach a mobile robot continuously tracks naturally occurring indoor targets that are subsequently treated as "beacons." Predicted targets (i.e., those found from the known environmental map) are tracked in order to update the position of the vehicle. Newly observed targets (i.e., those that were not predicted) are caused by unknown environmental features or obstacles from which new tracks are initiated, classified, and eventually integrated into the map.

Adams and von Flüe implemented the above technique using real sonar data. The authors note that a good sensor model is crucial for this work. For this reason, and in order to predict the expected observations from the sonar data, they use the sonar model presented by Kuc and Siegel [1987].


Figure 8.18: a. Regions of constant depth (RCD's) extracted from 15 sonar range scans.
b. True (x), odometric (+), and estimated (*) positions of the mobile robot using two planar (wall) "beacons" for localization. (Courtesy of Adams and von Flüe.)

Figure 8.18a shows regions of constant depth (RCDs) [Kuc and Siegel, 1987] that were extracted from 15 sonar scans recorded from each of the locations marked " $\times$."

The model from Kuc and Siegel's work suggests that RCDs such as those recorded at the positions marked A in Figure 8.18a correspond to planar surfaces; RCDs marked B rotate about a point corresponding to a 90 degree corner and RCDs such as C , which cannot be matched, correspond to multiple reflections of the ultrasonic wave.

Figure 8.18 b shows the same mobile robot run as Figure 8.18a, but here the robot computes its position from two sensed "beacons," namely the wall at D and the wall at E in the right-hand scan in Figure 8.18 b . It can be seen that the algorithm is capable of producing accurate positional estimates
of the robot, while simultaneously building a map of its sensed environment as the robot becomes more confident of the nature of the features.

### 8.3.2 Topological Maps for Navigation

Topological maps are based on recording the geometric relationships between the observed features rather than their absolute position with respect to an arbitrary coordinate frame of reference. Kortenkamp and Weymouth [1994] defined the two basic functions of a topological map:
a. Place Recognition With this function, the current location of the robot in the environment is determined. In general, a description of the place, or node in the map, is stored with the place. This description can be abstract or it can be a local sensory map. At each node, matching takes place between the sensed data and the node description.
b. Route Selection With this function, a path from the current location to the goal location is found.

The following are brief descriptions of specific research efforts related to topological maps.

### 8.3.2.1 Taylor [1991]

Taylor, working with stereo vision, observed that each local stereo map may provide good estimates for the relationships between the observed features. However, because of errors in the estimates for the robot's position, local stereo maps don't necessarily provide good estimates for the coordinates of these features with respect to the base frame of reference. The recognition problem in a topological map can be reformulated as a graph-matching problem where the objective is to find a set of features in the relational map such that the relationships between these features match the relationships between the features on the object being sought. Reconstructing Cartesian maps from relational maps involves minimizing a non-linear objective function with multiple local minima.

### 8.3.2.2 Courtney and Jain [1994]

A typical example of a topological map-based approach is given by Courtney and Jain [1994]. In this work the coarse position of the robot is determined by classifying the map description. Such classification allows the recognition of the workspace region that a given map represents. Using data collected from 10 different rooms and 10 different doorways in a building (see Fig. 8.19), Courtney and Jain estimated a 94 percent recognition rate of the rooms and a 98 percent recognition rate of the doorways. Courtney and Jain concluded that coarse position estimation, or place recognition, in indoor domains is possible through classification of grid-based maps. They developed a paradigm wherein pattern classification techniques are applied to the task of mobile robot localization. With this paradigm the robot's workspace is represented as a set of grid-based maps interconnected via topological relations. This representation scheme was chosen over a single global map in order to avoid inaccuracies due to cumulative dead-reckoning error. Each region is represented by a set of multi-sensory grid maps, and feature-level sensor fusion is accomplished through extracting spatial descriptions from these maps. In the navigation phase, the robot localizes itself by comparing features extracted from its map of the current locale with representative features of known locales in the
environment. The goal is to recognize the current locale and thus determine the workspace region in which the robot is present.
8.3.2.3 Kortenkamp and Weymouth [1993]

Kortenkamp and Weymouth implemented a cognitive map that is based on a topological map. In their topological map, instead of looking for places that are locally distinguishable from other places and then storing the distinguishing features of the place in the route map, their algorithm looks for places that mark the transition between one space in the environment and another space (gateways). In this algorithm sonar and vision sensing is


Figure 8.19: Based on datasets collected from 10 different rooms and 10 different doorways in a building, Courtney and Jain estimate a 94 percent recognition rate of the rooms and a 98 percent recognition rate of the doorways. (Adapted from [Courtney and Jain, 1994].) combined to perform place recognition for better accuracy in recognition, greater resilience to sensor errors, and the ability to resolve ambiguous places. Experimental results show excellent recognition rate in a well-structured environment. In a test of seven gateways, using either sonar or vision only, the system correctly recognized only four out of seven places. However, when sonar and vision were combined, all seven places were correctly recognized. Figure 8.20 shows the experimental space for place recognition. Key locations are marked in capital letters. Table 8.5 a and Table 8.5 b show the probability for each place using only vision and sonar, respectively. Table 8.5 c shows the combined probabilities (vision and sonar) for each place. In spite of the good results evident from Table 8.5 c , Kortenkamp and Weymouth pointed out several drawbacks of their system:

The robot requires several initial, guided traversals of a route in order to acquire a stable set of location cues so that it can navigate autonomously.


Figure 8.20: An experiment to determine if the robot can detect the same place upon return at a later time. In this case, multiple paths through the place can be "linked" together to form a network. (Adapted from [Kortenkamp and Weymouth, 1994].)

- Acquiring, storing, and matching visual scenes is very expensive, both in computation time and storage space.
- The algorithm is restricted to highly structured, orthogonal environments.

Table 8.5a: Probabilities for each place using only vision.

| Stored Places |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A |  |  |  |  |  |  |  |  | B | C | D | E | F | G |
| A | 0.43 | 0.09 | 0.22 | 0.05 | 0.05 | 0.1 | 0.06 |  |  |  |  |  |  |  |
| B | 0.05 | 0.52 | 0.21 | 0.06 | 0.05 | 0.05 | 0.05 |  |  |  |  |  |  |  |
| C | 0.10 | 0.12 | 0.36 | 0.2 | 0.04 | 0.13 | 0.04 |  |  |  |  |  |  |  |
| D | 0.14 | 0.05 | 0.24 | 0.43 | 0.05 | 0.04 | 0.05 |  |  |  |  |  |  |  |
| E | 0.14 | 0.14 | 0.14 | 0.14 | 0.14 | 0.14 | 0.14 |  |  |  |  |  |  |  |
| F | 0.14 | 0.14 | 0.14 | 0.16 | 0.14 | 0.14 | 0.14 |  |  |  |  |  |  |  |
| G | 0.14 | 0.14 | 0.14 | 0.14 | 0.14 | 0.14 | 0.14 |  |  |  |  |  |  |  |

Table 8.5b: Probabilities for each place using only sonar.

| Stored Places |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | A | B | C | D | E | F | G |
| A | 0.82 | 0.04 | 0.04 | 0.04 | 0.04 | 0 | 0 |
| B | 0.02 | 0.31 | 0.31 | 0.31 | 0.06 | 0 | 0 |
| C | 0.02 | 0.31 | 0.31 | 0.31 | 0.06 | 0 | 0 |
| D | 0.02 | 0.31 | 0.31 | 0.31 | 0.61 | 0 | 0 |
| E | 0.04 | 0.12 | 0.12 | 0.12 | 0.61 | 0 | 0 |
| F | 0 | 0 | 0 | 0 | 0 | 0.90 | 0.10 |
| G | 0 | 0 | 0 | 0 | 0 | 0.10 | 0.90 |

Table 8.5c: Combined probabilities (vision and sonar) for each place.

| Stored Places |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | A | B | C | D | E | F | G |
| A | 0.95 | 0.01 | 0.02 | 0.01 | 0.01 | 0 | 0 |
| B | 0 | 0.65 | 0.26 | 0.07 | 0.01 | 0 | 0 |
| C | 0 | 0.17 | 0.52 | 0.29 | 0.01 | 0 | 0 |
| D | 0.01 | 0.07 | 0.33 | 0.58 | 0.01 | 0 | 0 |
| E | 0.04 | 0.12 | 0.12 | 0.12 | 0.61 | 0 | 0 |
| F | 0 | 0 | 0 | 0 | 0 | 0.90 | 0.1 |
| G | 0 | 0 | 0 | 0 | 0 | 0.09 | 0.91 |

### 8.4 Summary

Map-based positioning is still in the research stage. Currently, this technique is limited to laboratory settings and good results have been obtained only in well-structured environments. It is difficult to judge how the performance of a laboratory robot scales up to a real world application. Kortenkamp and Weymouth [1994] noted that very few systems tested on real robots are tested under realistic conditions with more than a handful of places.

We summarize relevant characteristics of map-based navigation systems as follows:
Map-based navigation systems:

- are still in the research stage and are limited to laboratory settings,
- have not been tested extensively in real-world environments,
- require a significant amount of processing and sensing capability,
- need extensive processing, depending on the algorithms and resolution used,
- require initial position estimates from odometry in order to limit the initial search for features to a smaller area.

There are several critical issues that need to be developed further:

- Sensor selection and sensor fusion for specific applications and environments.
- Accurate and reliable algorithms for matching local maps to the stored map.
- Good error models of sensors and robot motion.
- Good algorithms for integrating local maps into a global map.


## Chapter 9 Vision-Based Positioning

A core problem in robotics is the determination of the position and orientation (often referred to as the pose) of a mobile robot in its environment. The basic principles of landmark-based and map-based positioning also apply to the vision-based positioning or localization which relies on optical sensors in contrast to ultrasound, dead-reckoning and inertial sensors. Common optical sensors include laser-based range finders and photometric cameras using CCD arrays.

Visual sensing provides a tremendous amount of information about a robot's environment, and it is potentially the most powerful source of information among all the sensors used on robots to date. Due to the wealth of information, however, extraction of visual features for positioning is not an easy task.The problem of localization by vision has received considerable attention and many techniques have been suggested. The basic components of the localization process are:

- representations of the environment,
- sensing models, and
- localization algorithms.

Most localization techniques provide absolute or relative position and/or the orientation of sensors. Techniques vary substantially, depending on the sensors, their geometric models, and the representation of the environment.

The geometric information about the environment can be given in the form of landmarks, object models and maps in two or three dimensions. A vision sensor or multiple vision sensors should capture image features or regions that match the landmarks or maps. On the other hand, landmarks, object models, and maps should provide necessary spatial information that is easy to be sensed. When landmarks or maps of an environment are not available, landmark selection and map building should be part of a localization method.

In this chapter, we review vision-based positioning methods which have not been explained in the previous chapters. In a wider sense, "positioning" means finding position and orientation of a sensor or a robot. Since the general framework of landmark-based and map-based positioning, as well as the methods using ultrasound and laser range sensors have been discussed, this chapter focuses on the approaches that use photometric vision sensors, i.e., cameras. We will begin with a brief introduction of a vision sensor model and describe the methods that use landmarks, object models and maps, and the methods for map building.

### 9.1 Camera Model and Localization

Geometric models of photometric cameras are of critical importance for finding geometric position and orientation of the sensors. The most common model for photometric cameras is the pin-hole camera with perspective projection as shown in Fig. 9.1. Photometric cameras using optical lens can be modeled as a pin-hole camera. The coordinate system ( $\mathrm{X}, \mathrm{Y}, \mathrm{Z}$ ) is a three-dimensional camera coordinate system, and ( $\mathrm{x}, \mathrm{y}$ ) is a sensor (image) coordinate system. A three-dimensional feature in


Figure 9.1: Perspective camera model.
an object is projected onto the image plane ( $\mathrm{x}, \mathrm{y}$ ). The relationship for this perspective projection is given by

$$
\begin{equation*}
\mathrm{x}=\mathrm{f} \frac{\mathrm{X}}{\mathrm{Z}}, \quad \mathrm{y}=\mathrm{f} \frac{\mathrm{Y}}{\mathrm{Z}} \tag{9.1}
\end{equation*}
$$

Although the range information is collapsed in this projection, the angle or orientation of the object point can be obtained if the focal length f is known and there is no distortion of rays due to lens distortion. The internal parameters of the camera are called intrinsic camera parameters and they include the effective focal length f , the radial lens distortion factor, and the image scanning parameters, which are used for estimating the physical size of the image plane. The orientation and position of the camera coordinate system (X, Y, Z) can be described by six parameters, three for orientation and three for position, and they are called extrinsic camera parameters. They represent the relationship between the camera coordinates $(\mathrm{X}, \mathrm{Y}, \mathrm{Z})$ and the world or object coordinates ( $\mathrm{X}_{\mathrm{W}}$, $\mathrm{Y}_{\mathrm{W}}, \mathrm{Z}_{\mathrm{W}}$ ). Landmarks and maps are usually represented in the world coordinate system.

The problem of localization is to determine the position and orientation of a sensor (or a mobile robot) by matching the sensed visual features in one or more image(s) to the object features provided by landmarks or maps. Obviously a single feature would not provide enough information for position and orientation, so multiple features are required. Depending on the sensors, the sensing schemes, and the representations of the environment, localization techniques vary significantly.

### 9.2 Landmark-Based Positioning

The representation of the environment can be given in the form of very simple features such as points and lines, more complex patterns, or three-dimensional models of objects and environment. In this section, the approaches based on simple landmark features are discussed.

### 9.2.1 Two-Dimensional Positioning Using a Single Camer a

If a camera is mounted on a mobile robot with its optical axis parallel to the floor and vertical edges of an environment provide landmarks, then the positioning problem becomes two-dimensional. In this case, the vertical edges provide point features and two-dimensional positioning requires identification of three unique features. If the features are uniquely identifiable and their positions are known, then the position and orientation of the pin-hole camera can be uniquely determined as illustrated in Fig. 9.2a. However, it is not always possible to uniquely identify simple features such as points and lines in an image. Vertical lines are not usually identifiable unless a strong constraint is imposed. This is illustrated in Fig. 9.2b.

a.

b. smonecat wat

Figure 9.2: Localization using landmark features.

Sugihara [1988] considered two cases of point location problems. In one case the vertical edges are distinguishable from each other, but the exact directions in which the edges are seen are not given. In this case, the order in which the edges appear is given. If there are only two landmark points, the measurement of angles between the corresponding rays restricts the possible camera position to part of a circle as shown in Fig. 9.3a. Three landmark points uniquely determine the camera position which is one of the intersections of the two circles determined by the three mark points as depicted in Fig. 9.3b. The point location algorithm first establishes a correspondence between the three landmark points in the environment and three observed features in an image. Then, the algorithm measures the angles between the rays. To measure the correct angles, the camera should be calibrated for its intrinsic parameters. If there are more than three pairs of rays and landmarks, only the first three pairs are used for localization, while the remaining pairs of rays and landmarks can be used for verification.

In the second case, in which k vertical edges are indistinguishable from each other, the location algorithm finds all the solutions by investigating all the possibilities of correspondences. The algorithm first chooses any four rays, say $r_{1}, r_{2}, r_{3}$, and $r_{4}$. For any ordered quadruplet ( $\mathrm{p}, \mathrm{p}, \mathrm{p}, \mathrm{p}_{\mathrm{n}}$ ) out of n mark points $p_{1}, \ldots, p_{n}$, it solves for the position based on the assumption that $\underset{\underline{x},}{ }{ }_{3} r, r$, and $r$ correspond to $p_{i}, p_{j}, p_{p}$, and $p_{m}$, respectively. For $n(n-1)(n-2)(n-3)$ different quadruples, the algorithm can solve for the position in $\mathrm{O}\left(\mathrm{n}^{4}\right)$ time. Sugihara also proposed an algorithm that runs in $\mathrm{O}\left(\mathrm{n}^{3} \log \right.$ n) time with $O(n)$ space or in $O\left(n^{3}\right)$ time with $O\left(n^{2}\right)$ space. In the second part of the paper, he considers the case where the marks are distinguishable but the directions of rays are inaccurate. In this case, an estimated position falls in a region instead of a point.

a. Possible camera locations (circular arc) determined by two rays and corresponding mark points.
b. Unique camera position determined by three rays and corresponding mark points.
c. Possible camera locations (shaded region) determined by two noisy rays and corresponding mark points.
(Adapted from [Sugihara 1988; Krotkov 1989]).

Krotkov [1989] followed the approach of Sugihara and formulated the positioning problem as a search in a tree of interpretation (pairing of landmark directions and landmark points). He developed an algorithm to search the tree efficiently and to determine the solution positions, taking into account errors in the landmark direction angle. According to his analysis, if the error in angle measurement is at most $\delta \theta$, then the possible camera location lies not on an arc of a circle, but in the shaded region shown in Fig. 3c. This region is bounded by two circular arcs.

Krotkov presented simulation results and analyses for the worst-case errors and probabilistic errors in ray angle measurements. The conclusions from the simulation results are:

- the number of solution positions computed by his algorithm depends significantly on the number of angular observations and the observation uncertainty $\delta \theta$.
- The distribution of solution errors is approximately a Gaussian whose variance is a function of $\delta \theta$ for all the angular observation errors he used: a. uniform, b. normal, and c. the worst-case distribution.
Betke and Gurvits [1994] proposed an algorithm for robot positioning based on ray angle measurements using a single camera. Chenavier and Crowley [1992] added an odometric sensor to landmark-based ray measurements and used an extended Kalman filter for combining vision and odometric information.


### 9.2.2 Two-Dimensional Positioning Using Stereo Cameras

Hager and Atiya [1993] developed a method that uses a stereo pair of cameras to determine correspondence between observed landmarks and a pre-loaded map, and to estimate the twodimensional location of the sensor from the correspondence. Landmarks are derived from vertical edges. By using two cameras for stereo range imaging the algorithm can determine the twodimensional locations of observed points - in contrast to the ray angles used by single-camera approaches.

Hager and Atiya's algorithm performs localization by recognizing ambiguous sets of correspondences between all the possible triplets of map points $p_{i}, p_{j}, p_{k}$ and those of observed points $o_{a}, o_{b}, o_{c}$. It achieves this by transforming both observed data and stored map points into a representation that is invariant to translation and rotation, and directly comparing observed and stored entities. The permissible range of triangle parameters due to sensor distortion and noise is computed and taken into account.

For $n$ map points and $m$ observed points, the off-line initialization stage consumes $O\left(n^{3} \log n\right)$ time to compute and sort all triangle parameters from the map points. At run time, the worst case complexity is $\mathrm{O}\left(\mathrm{m}^{3}\left(\mathrm{n}^{3}+\log \mathrm{n}\right)\right.$ ). However, an efficient strategy of marking and scanning reduces the search space and real-time performance (half a second) is demonstrated for five observed and 40 stored landmarks.

### 9.3 Camera-Calibration Approaches

The camera-calibration approaches are more complex than the two-dimensional localization algorithms discussed earlier. This is because calibration procedures compute the intrinsic and extrinsic camera parameters from a set of multiple features provided by landmarks. Their aim is to establish the three-dimensional position and orientation of a camera with respect to a reference coordinate system. The intrinsic camera parameters include the effective focal length, the lens distortion parameters, and the parameters for image sensor size. The computed extrinsic parameters provide three-dimensional position and orientation information of a camera coordinate system relative to the object or world coordinate system where the features are represented.

The camera calibration is a complex problem because of these difficulties:

- All the intrinsic and extrinsic parameters should be computed from the two-dimensional projections of a limited number of feature points,
- the parameters are inter-related, and
- the formulation is non-linear due to the perspectivity of the pin-hole camera model.

The relationship between the three-dimensional camera coordinate system (see Fig. 1)

$$
\begin{equation*}
\underline{\mathrm{X}}=[\mathrm{X}, \mathrm{Y}, \mathrm{Z}]^{\mathrm{T}} \tag{9.2}
\end{equation*}
$$

and the object coordinate system
$\underline{X}_{W}=\left[X_{W}, Y_{W}, Z_{W}\right]^{T}$
is given by a rigid body transformation

$$
\begin{equation*}
\underline{\mathrm{X}}=\underline{\mathrm{R} X_{W}}+\underline{\mathrm{T}} \tag{9.4}
\end{equation*}
$$

where

$$
\underline{\mathrm{R}}=\left[\begin{array}{lll}
\mathrm{r}_{\mathrm{XX}} & \mathrm{r}_{\mathrm{XY}} & \mathrm{r}_{\mathrm{XZ}}  \tag{9.5}\\
\mathrm{r}_{\mathrm{rXX}} & \mathrm{r}_{\mathrm{YY}} & \mathrm{r}_{\mathrm{YZ}} \\
\mathrm{r}_{\mathrm{ZX}} & \mathrm{r}_{\mathrm{ZY}} & \mathrm{r}_{\mathrm{ZZ}}
\end{array}\right], \quad \underline{\mathrm{T}}=\left[\begin{array}{l}
\mathrm{t}_{\mathrm{X}} \\
\mathrm{t}_{\mathrm{Y}} \\
\mathrm{t}_{\mathrm{Z}}
\end{array}\right]
$$

are the rotation and translation matrices, respectively.
Determination of camera position and orientation from many image features has been a classic problem of photogrammetry and has been investigated extensively [Slama 1980; Wolf 1983]. Some photogrammetry methods (as described in [Wolf 1983]) solved for the translation and rotation parameters by nonlinear least-squares techniques. Early work in computer vision includes that by Fischler and Bolles [1981] and Ganapathy [1984]. Fischler and Bolles found the solution by first computing the length of rays between the camera center (point O in Fig. 9.1) and the feature projections on the image plane ( $\mathrm{x}, \mathrm{y}$ ). They also established results on the number of solutions for various number of feature points. According to their analysis, at least six points are required to get a unique solution. Ganapathy [1984] showed similar results and presented somewhat simplified algorithms.


Figure 9.4: Camera calibration using multiple features and a radial alignment constraint.
More recently several newer methods were proposed for solving for camera position and orientation parameters. The calibration technique proposed by Tsai [1986] is probably the most complete and best known method, and many versions of implementation code are available in the public domain. The Tsai's algorithm decomposes the solution for 12 parameters (nine for rotation and three for translation) into multiple stages by introducing a constraint. The radial alignment constraint
assumes that the lens distortion occurs only in the radial direction from the optical axis Z of the camera. Using this constraint, six parameters $r_{X X}, r_{X X}, r_{Y X}, r_{Y Y}, t_{X}$, and $t_{Y}$ are computed first, and the constraint of the rigid body transformation $\underline{R R}{ }^{T}=\underline{I}$ is used to compute $r_{X Z}, r_{Y Z}, r_{z X}, r_{z Y}$, and $\underline{\xi}_{z}$. Among the remaining parameters, the effective focal length $f$ and $t_{z}$ are first computed neglecting the radial lens distortion parameter $\kappa$, and then used for estimating $\kappa$ by a nonlinear optimization procedure. The values of $f$ and $t_{z}$ are also updated as a result of the optimization. Further work on camera calibration has been done by Lenz and Tsai [1988].

Liu et al. [1990] first suggested the use of straight lines and points as features for estimating extrinsic camera parameters. Line features are usually abundant in indoor and some outdoor environments and less sensitive to noise than point features. The constraint used for the algorithms is that a three-dimensional line in the camera coordinate system ( $\mathrm{X}, \mathrm{Y}, \mathrm{Z}$ ) should lie in the plane formed by the projected two-dimensional line in the image plane and the optical center O in Fig 9.1. This constraint is used for computing nine rotation parameters separately from three translation parameters. They present linear and nonlinear algorithms for solutions. According to Liu et al.'s analysis, eight-line or six-point correspondences are required for the linear method, and three-line or three-point correspondences are required for the nonlinear method. A separate linear method for translation parameters requires three-line or two-point correspondences.

Haralick et al. [1989] reported their comprehensive investigation for position estimation from two-dimensional and three-dimensional model features and two-dimensional and three-dimensional sensed features. Other approaches based on different formulations and solutions include Kumar [1988], Yuan [1989], and Chen [1991].

### 9.4 Model-Based Approaches

A priori information about an environment can be given in more comprehensive form than features such as two-dimensional or three-dimensional models of environment structure and digital elevation maps (DEM). The geometric models often include three-dimensional models of buildings, indoor structure and floor maps. For localization, the two-dimensional visual observations should capture the features of the environment that can be matched to the preloaded model with minimum uncertainty. Figure 5 illustrates the match between models and image features. The problem is that the two-dimensional observations and the three-dimensional world models are in different forms. This is basically the problem of object recognition in computer vision: (1) identifying objects and (2) estimating pose from the identified objects.


Figure 9.5: Finding correspondence between an internal model and an observed scene.

### 9.4.1 Three-Dimensional Geometric Model-Based Positioning

Fennema et al. [1990] outlined a system for navigating a robot in a partially modeled environment. The system is able to predict the results of its actions by an internal model of its environment and models of its actions. Sensing is used to correct the model's predictions about current location or to progress towards some goal. Motions are composed in a hierarchical planner that sketches overall paths and details the short term path. Control of the robot is broken down into the action level, the plan level, and the goal level. Landmarks are chosen to measure progress in the plan. The system must receive perceptual confirmation that a step in the plan has been completed before it will move to the next part of the plan. Later steps in a plan expand in detail as earlier steps are completed. The environment is modeled in a graph structure of connected nodes called locales. Locales may exist at a variety of scales in different hierarchies of the map. Other information is kept in the system associated with each locale to provide more detail. Using these models the robot operates in a planand monitor-cycle, confirming and refining plans to achieve overall goals.

The algorithm by Fennema et al. [1990] matches images to the map by first matching the twodimensional projection of landmarks to lines extracted from the image. The best fit minimizes the difference between the model and the lines in the data. Once the correspondence between model and two-dimensional image is found, the relation of the robot to the world coordinate system must be found. This relation is expressed as the rotation and translation that will match the robot- and worldsystems. Matching is done by considering all possible sets of three landmarks. Once a close correspondence is found between data and map, the new data is used to find a new estimate for the actual pose.

Kak et al. [1990] used their robot's encoders to estimate its position and heading. The approximate position is used to generate a two-dimensional scene from their three-dimensional world model and the features in the generated scene are matched against those extracted from the observed image. This method of image matching provides higher accuracy in position estimation.

Talluri and Aggarwal [1991; 1992] reported their extensive work on model-based positioning. They use three-dimensional building models as a world model and a tree search is used to establish a set of consistent correspondences. Talluri and Aggarwal [1993] wrote a good summary of their algorithms as well as an extensive survey of some other vision-based positioning algorithms.


Figure 9.6: Finding a location on a digital elevation maps (DEM) that matches a visual scene observed from a point. The 'x' marks a possible location in the DEM that could generate the observed visual scene to the right.

### 9.4.2 Digital Elevation Map-Based Localization

For outdoor positioning, Thompson et al. [1993] developed a hierarchical system that compares features extracted from a visual scene to features extracted from a digital elevation maps (DEM). A number of identifiable features such as peaks, saddles, junctions, and endpoints are extracted from the observed scene. Similarly, features like contours and ridges are extracted from the DEM. The objective of the system is to match the features from the scene onto a location in the map. The feature matching module interacts with each feature extractor as well as with a geometric inference module. Each module may request information and respond to the others. Hypotheses are generated and tested by the interaction of these feature extractors, geometric inference, and feature matching modules.

In order to make matching more tractable, configurations of distinctive and easily identified features are matched first. Using a group of features cuts down dramatically on the number of possible comparisons. Using rare and easily spotted features is obviously advantageous to making an efficient match. A number of inference strategies that express viewpoint constraints are consulted in the geometric inference module. These viewpoint constraints are intersected as more features are considered, narrowing the regions of possible robot location.

Sutherland [1993] presented work on identifying particular landmarks for good localization. A function weighs configurations of landmarks for how useful they will be. It considers the resulting area of uncertainty for projected points as well as relative elevation. Sutherland showed that a careful choice of landmarks usually leads to improved localization.

Talluri and Aggarwal [1990] formulated position estimation using DEM as a constrained search problem. They determined an expected image based on a hypothetical location and compared that to the actual observed image. Possible correspondences are eliminated based on geometric constraints between world model features and their projected images. A summary of their work is given in [Talluri and Aggarwal, 1993].

### 9.5 Feature-Based Visual Map Building

The positioning methods described above use a priori information about the environment in the form of landmarks, object models or maps. Sometimes pre-loaded maps and absolute references for positions can be impractical since the robot's navigation is restricted to known structured environments. When there is no a priori information, a robot can rely only on the information obtained by its sensors.

The general framework for map-building has been discussed in the previous chapter. For constructing the environment model, vision systems usually use image features detected at one or more robot positions. According to the computer vision theory of structure from motion and stereo vision, correct correspondences of image features detected in several locations can provide information about the motion of the sensor (both translation and rotation), as well as of the threedimensional structure of the environment at the feature locations. The trajectory of the sensor can be obtained by visual dead-reckoning, i.e., the integration of the estimated incremental motion. This is illustrated in Fig. 9.7.

The object features detected in a sensor location become the relative reference for the subsequent sensor locations. When correspondences are correctly established, vision methods can provide higher
accuracy in position estimation than odometry or inertial navigation systems. On the other hand, odometry and inertial sensors provide reliable position information up to certain degree and this can assist the establishment of correspondence by limiting the search space for feature matching. A visual map based on object features is a sparse description of environment structure.


Figure 9.7: Illustration of map building and trajectory integration.
Moravec [1981] used stereo cameras with variable baseline for obtaining environment structure in the form of feature locations and estimating position of the sensors. A feature selection method was suggested and coarse-to-fine correlation feature matching was used. The suggested error measure is that the uncertainty in feature location is proportional to the distance from the sensor.

Matthies and Shafer [1987] proposed a more systematic and effective error measure using a threedimensional Gaussian distribution. A Kalman filter was used for updating robot positions based on the Gaussian error distribution of detected features.

Ayache and Faugeras [1987] used trinocular stereo and three-dimensional line features for building, registering and fusing noise visual maps. They used an extended Kalman filter for combining measurements obtained at different locations.

### 9.6 Summary and Discussion

We reviewed some of the localization methods based only on photometric camera sensors. These methods use:

- landmarks
- object models
- maps
- feature-based map-building

Most of the work discussed suggests methodologies that relate detected image features to object features in an environment. Although the vision-based techniques can be combined with the methods using dead-reckoning, inertial sensors, ultrasonic and laser-based sensors through sensor fusion, tested methods under realistic conditions are still scarce.

Similar to the landmark-based and map-based methods that were introduced in the previous chapters, vision-based positioning is still in the stage of active research. It is directly related to most of the computer vision methods, especially object recognition which involves identification of object class and pose estimation from the identified object. As the research in many areas of computer vision and image processing progresses, the results can be applied to vision-based positioning. In addition to object recognition, relevant areas include structure from stereo, motion and contour, vision sensor modeling, and low-level image processing. There are many vision techniques that are potentially useful but have not been specifically applied to mobile robot positioning problems and tested under realistic conditions.

## APPENDIX A

## A Word on Kalman Filters

The most widely used method for sensor fusion in mobile robot applications is the Kalman filter. This filter is often used to combine all measurement data (e.g., for fusing data from different sensors) to get an optimal estimate in a statistical sense. If the system can be described with a linear model and both the system error and the sensor error can be modeled as white Gaussian noise, then the Kalman filter will provide a unique statistically optimal estimate for the fused data. This means that under certain conditions the Kalman filter is able to find the best estimates based on the "correctness" of each individual measurement.

The calculation of the Kalman filter is done recursively, i.e., in each iteration, only the newest measurement and the last estimate will be used in the current calculation, so there is no need to store all the previous measurements and estimates. This characteristic of the Kalman filter makes it appropriate for use in systems that don't have large data storage capabilities and computing power. The measurements from a group of $n$ sensors can be fused using a Kalman filter to provide both an estimate of the current state of a system and a prediction of the future state of the system.

The inputs to a Kalman filter are the system measurements. The a priori information required are the system dynamics and the noise properties of the system and the sensors. The output of the Kalman filter is the estimated system state and the innovation (i.e., the difference between the predicted and observed measurement). The innovation is also a measure for the performance of the Kalman filter.

At each step, the Kalman filter generates a state estimate by computing a weighted average of the predicted state (obtained from the system model) and the innovation. The weight used in the weighted average is determined by the covariance matrix, which is a direct indication of the error in state estimation. In the simplest case, when all measurements have the same accuracy and the measurements are the states to be estimated, the estimate will reduce to a simple average, i.e., a weighted average with all weights equal. Note also that the Kalman filter can be used for systems with timevariant parameters.

The extended Kalman filter is used in place of the conventional Kalman filter if the system model is potentially numerically instable or if the system model is not approximately linear. The extended Kalman filter is a version of the Kalman filter that can handle non-linear dynamics or non-linear measurement equations, or both [Abidi and Gonzalez, 1992].

## Appendix B <br> Unit Conversions and Abbreviations

To convert from
(Angles)
degrees ( ${ }^{\circ}$ )
radian (rad)
milliradians (mrad)
(Length)
inch (in)
inch (in)
inch (in)
foot (ft)
mile (mi), (U.S. statute)
mile (mi), (international nautical)
yard (yd)
(Area)
inch ${ }^{2}\left(\mathrm{in}^{2}\right)$
foot ${ }^{2}\left(\mathrm{ft}^{2}\right)$
$\operatorname{yard}^{2}\left(\mathrm{yd}^{2}\right)$
(Volume)
foot ${ }^{3}\left(\mathrm{ft}^{3}\right)$
inch ${ }^{3}\left(\right.$ in $\left.^{3}\right)$
(Time)
nanosecond (ns)
microsecond ( $\mu \mathrm{s}$ )
millisecond (ms)
second (s)
minute (min)
hour (hr)
(Frequency)
Hertz (Hz)
Kilohertz (KHz)
Megahertz (MHz)
Gigahertz (GHz)

To
$\begin{array}{ll}\text { radian }(\mathrm{rad}) & 0.01745 \\ \text { degrees }\left({ }^{\circ}\right) & 57.2958 \\ \text { degrees }\left({ }^{\circ}\right) & 0.0573\end{array}$
meter (m) 0.0254
centimeter $(\mathrm{cm}) \quad 2.54$
millimeter (mm) 25.4
meter (m) 30.48
meter $(\mathrm{m}) \quad 1,609$
meter $(\mathrm{m}) \quad 1,852$
meter (m) 0.9144

| $\operatorname{meter}^{2}\left(\mathrm{~m}^{2}\right)$ | $6.4516 \times 10^{-4}$ |
| :--- | :--- |
| $\operatorname{meter}^{2}\left(\mathrm{~m}^{2}\right)$ | $9.2903 \times 10^{-2}$ |
| meter $^{2}\left(\mathrm{~m}^{2}\right)$ | 0.83613 |

meter ${ }^{3}\left(\mathrm{~m}^{3}\right)$
$2.8317 \times 10^{-2}$
meter $^{3}\left(\mathrm{~m}^{3}\right)$
$1.6387 \times 10^{-5}$

| second (s) | $10^{-9}$ |
| :--- | :--- |
| second (s) | $10^{-6}$ |
| second (s) | $10^{-3}$ |
|  |  |
| second (s) | 60 |
| second (s) | 3,600 |

cycle/second $\left(\mathrm{s}^{-1}\right) \quad 1$
Hz
1,000
$\mathrm{Hz} \quad 10^{6}$
$\mathrm{Hz} \quad 10^{9}$

| To convert from | To | Multiply by |
| :---: | :---: | :---: |
| (Velocity) |  |  |
| foot/minute ( $\mathrm{ft} / \mathrm{min}$ ) | meter/second (m/s) | $5.08 \times 10^{-3}$ |
| foot/second (ft/s) | meter/second (m/s) | 0.3048 |
| knot (nautical mi/h) | meter/second (m/s) | 0.5144 |
| mile/hour (mi/h) | meter/second (m/s) | 0.4470 |
| mile/hour (mi/h) | kilometer/hour (km/h) | 1.6093 |
| (Mass, Weight) |  |  |
| pound mass (lb) | kilogram (kg) | 0.4535 |
| pound mass (lb) | grams (gr) | 453.59 |
| ounce mass (oz) | grams (gr) | 28.349 |
| slug ( $\mathrm{lbf} \cdot \mathrm{s}^{2} / \mathrm{ft}$ ) | kilogram (kg) | 14.594 |
| ton (2000 lbm) | kilogram (kg) | 907.18 |
| (Force) |  |  |
| pound force (lbf) | newton (N) | 4.4482 |
| ounce force | newton (N) | 0.2780 |
| (Energy, Work) |  |  |
| foot-pound force ( $\mathrm{ft} \cdot \mathrm{lbf}$ ) | joule (J) | 1.3558 |
| kilowatt-hour (kW •h) | joule (J) | $3.60 \times 10^{6}$ |
| (Acceleration) |  |  |
| foot/second ${ }^{2}$ ( $\mathrm{ft} / \mathrm{s}^{2}$ ) | meter/second ${ }^{2}\left(\mathrm{~m} / \mathrm{s}^{2}\right)$ | 0.3048 |
| inch/second (in./s ${ }^{2}$ ) | meter/second ${ }^{2}\left(\mathrm{~m} / \mathrm{s}^{2}\right)$ | $2.54 \times 10^{-2}$ |
| (Power) |  |  |
| foot-pound/minute ( $\mathrm{ft} \cdot \mathrm{lbf} / \mathrm{min}$ ) | watt (W) | $2.2597 \times 10^{-2}$ |
| horsepower ( $550 \mathrm{ft} \cdot \mathrm{lbf} / \mathrm{s}$ ) | watt (W) | 745.70 |
| milliwatt (mW) | watt (W) | $10^{-3}$ |
| (Pressure, stress) |  |  |
| atmosphere (std) ( $14.7 \mathrm{lbf} / \mathrm{in}^{2}$ ) | newton/meter ${ }^{2}\left(\mathrm{~N} / \mathrm{m}^{2}\right.$ or Pa$)$ | 101,330 |
| pound/foot ${ }^{2}\left(\mathrm{lbf} / \mathrm{ft}^{2}\right)$ | newton/meter ${ }^{2}\left(\mathrm{~N} / \mathrm{m}^{2}\right.$ or Pa$)$ | 47.880 |
| pound/inch ${ }^{2}$ (lbf/in ${ }^{2}$ or psi) | newton/meter ${ }^{2}\left(\mathrm{~N} / \mathrm{m}^{2}\right.$ or Pa$)$ | 6,894.8 |
| (Temperature) degree Fahrenheit $\left({ }^{\circ} \mathrm{F}\right)$ | degree Celsius ( ${ }^{\circ} \mathrm{C}$ ) | ${ }^{\circ} \mathrm{C}=\left({ }^{\circ} \mathrm{F}-32\right) \times 5 / 9$ |
| (Electrical) |  |  |
| Volt (V); Ampere (A); Ohm ( $\Omega$ ) |  |  |

# Appendix C Systems-at-A-Glance Tables 

| Name | Computer | Onboard <br> Equipment | Accuracy- <br> position $[\mathrm{mm}]$ | Accuracy - <br> orientation $\left[{ }^{\circ}\right]$ | Sampling <br> Rate $[\mathrm{Hz}]$ | Features <br> Range, Notes | Reference |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |


| General |  |  | $0.01 \%-5 \%$ of traveled distance |  | 100-10,000 or analog | Error accumulation | Unlimited, internal, local | [Parish and Grabbe, 1993] <br> Omnitech Robotics, Inc. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| TRC Labmate | $486-33 \mathrm{MHz}$ | Each quad-encoder pulse corresponds to 0.012 mm wheel displacement | $4 \times 4$ meters bidirectional square path ${ }^{*}: 310 \mathrm{~mm}$ | On smooth concrete*: $6{ }^{\circ}$ With ten bumps*: $8^{\circ}$ | Very high <br> $\sim 1 \mathrm{KHz}$ | Short wheelbase | Unlimited | [TRC] Transition Research Corp. |
| Cybermotion | Onboard proprietory | Drive and steer encoders | $4 \times 4$ meters bidirectional square path*: 63 mm | On smooth concrete*: 1 to $3.8^{\circ}$ With ten bumps*: $4^{\circ}$ |  | Synchro-drive design |  | Cybermotion |
| Blanche | MC68020 | Uses a pair of knife-edge non-load-bearing wheels for odometry |  |  |  |  |  | [Cox, 1991] NEC Research Institute |
| Model-reference adaptive motion control | 386-20 MHZ <br> TRC Labmate | Wheel encoders and sonars for orientation measurements | Average after a $2 \times 2 \mathrm{~m}$ square path: 20 mm | Average after $2 \times 2 \mathrm{~m}$ square path: $0.5^{\circ}$ | 20 Hz | Can only compensate for systematic error | Unlimited | [Feng et al., 1994] Univ. of Michigan |
| Multiple robots |  | Two cooperative robots: one moves and one stays still and measures the motion of the moving one | Simulation: 8 mm after 100 meters movement at 2 m step |  |  | Capable of maintaining good position estimate over long distance | Umlimited | [Sugiyama, 1993] <br> NTT Communication Science Lab. |
| CLAPPER: <br> Dual-drive robot with internal correction of Odometry | $486-33 \mathrm{MHz}$ | Two TRC Labmates, connected by a compliant linkage; two absolute rotary encoders, one linear encoder | $4 \times 4 \mathrm{~m}$ square path: no bumps: 22 mm With 10 bumps ${ }^{1}: 44 \mathrm{~mm}$ | On smooth concrete*: <br> $22^{\circ}$ <br> With 10 <br> bumps*: $0.4^{\circ}$ | 25 Hz | Capable of compensating for random disturbance | Require additional robot or trailer | [Borenstein, 1994] <br> Univ. of Michigan |
| UMBmark calibration for reduction of sytematic odometry errors | $486-33 \mathrm{MHz}$ or any onboard computer | Any differential-drive mobile robot; tests here performed with TRC LabMate | $4 \times 4 \mathrm{~ms}$ square path: average return position error: $30-40 \mathrm{~mm}$ |  | 25 Hz | Designed for reduction of errors; this calibration rou any differential-drive robo tooling or instrumentation | stematic odometry e can be applied to requires no special | [Borenstein and Feng, 1995a,b, c] Univ. of Michigan |
| Fluxgate magnetometer |  |  |  | $\pm 1- \pm 4^{\circ}$ | 10-1000 or analog | External, global, \$1002000 <br> Prone to magnetic disturbance | Unlimited | [Parish and Grabble, 1993] <br> Omnitech Robotics, Inc. |

* This result is based on running the University of Michigan Benchmark (UMBmark) test for dead-reckoning accuracy. This test is described in detail in [Borenstein and Feng, 1994].

| Name | Computer | Onboard <br> Equipment | Accuracy- <br> position $[\mathrm{mm}]$ | Accuracy - <br> orientation $\left[{ }^{\circ}\right]$ | Sampling <br> Rate $[\mathrm{Hz}]$ | Features <br> Range, Notes | Reference |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |


| Angular rate gyro (laser or optical fiber) |  | Very accurate models available at $\$ 1 \mathrm{~K}$ - 5 K Problems are time dependent drift, andminimum detectable rate of rotation Gyro will not "catch" slow rotation errors |  | $0.01 \%-5 \%$ of full scale rate. | $\begin{aligned} & 10-1000 \text { or } \\ & \text { analog } \end{aligned}$ | Internal, local, \$1K-20K. | Unlimited | [Parish and Grabble, 1993] Omnitech Robotics, Inc. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Radar velocimeter (Doppler) |  |  | $0.01 \%-5 \%$ of full scale rate |  | $\begin{aligned} & 100-1000 \text { or } \\ & \text { analog } \end{aligned}$ | Internal, local, \$1K-10K | Unlimited | [Parish and Grabble, 1993] Omnitech Robotics, Inc. |
| Filtered/inertial sensor suite (direction gyros and accelerometer based) |  |  | $0.01 \%-5 \%$ of distance traveled, also time dependent drift |  | $\begin{aligned} & \begin{array}{l} 10-1000 \text { or } \\ \text { analog } \end{array} \\ & \hline \end{aligned}$ | Internal, local, $\$ 3 \mathrm{~K}-$ \$150K+ | Unlimited | [Parish and Grabble, 1993] Omnitech Robotics, Inc. |
| MiniRover MKI | Underwater vehicle | Fluxgate magnetic sensor |  | Accuracy: $\pm 2 \%$ max. <br> Resultion: $2^{\circ}$ | analog |  | $0^{\circ}-359^{\circ}$ | [BENTHOS] BENTHOS, Inc |
| Futaba model helicopter gyro FP-G154 | Output: pulsewidth modulated signal |  |  | Drift: $>1{ }^{\circ} / \mathrm{s}$ | 20 ms | \$150 |  | [TOWER] |
| Gyration GyroEngine | RS232 interface |  |  | Drift: $9 \%$ min |  | \$300 | Unlimited | [GYRATION] <br> Gyration, Inc. |
| Murata Gyrostar ENV-05H | Analog interface | Piezoelectric triangular prism. Drift: $9^{\circ} / \mathrm{sec}$ (maximum rated by manufacturer. Actual drift is lower) |  | $\begin{aligned} & \text { Measured drift: } \\ & 3-15 \% / \mathrm{min} \end{aligned}$ |  | small, light (42 gr), \$300 | Unlimited | [Murata] |
| Angular rate gyros, general (Laser or Optical Fiber) |  | Very accurate models available at $\$ 1 \mathrm{~K}-5 \mathrm{~K}$ Problems are time dependent drift, andminimum detectable rate of rotation Gyro will not "catch" slow rotation errors |  | $0.01 \%-5 \%$ of full scale rate. | $\begin{aligned} & \text { 10-1000 or } \\ & \text { analog } \end{aligned}$ | Internal, local, \$1K-20K. | Unlimited | [Parish and Grabble, 1993], Omnitech Robotics, Inc. |
| Hitachi OFG-3 | RS232 interface or TTL | Originally designed for automotive navigation systems |  | Drift: $0.0028^{\circ} / \mathrm{s}$ | 100 Hz |  | Unlimited | Komoriya and Oyama [1994], [HITACHI] |
| Andrew Autogyro and Autogyro Navigator | RS232 interface | Quoted minimum detectable rotation rate: $\pm 0.02 \% / \mathrm{s}$ Actual minimum detectable rate limited by deadband after A/D conversion: $0.0625 \%$ |  | Drift: $0.005 \%$ | 10 Hz | \$1000 | Unlimited | [ANDREW] <br> Andrew Corporation |
| Complete inertial navigation system including ENV-O5S Gyrostar solid state rate gyro, the START solid state gyro, one triaxial linear accelerometer and two inclinometers |  |  | Position drift rate 1 to $8 \mathrm{~cm} / \mathrm{s}$ depending on the freq. of acceleration change | Gyro drift 5-15\%/min. After compensation: drift $0.75 \%$ min | $\begin{aligned} & 100-1000 \text { or } \\ & \text { analog } \end{aligned}$ | Internal, global | unlimited | [Barshan and Durrant-Whyte, 1993, 1995];[GEC]; [MURATA] |
| Non-Wire Guidance System for AGV's | VCC-2 vehicle control computer | Solid state gyroscope, position code reader | Position codes (landmarks) |  |  |  |  | [CONTROL] <br> Control Engineering <br> Company |


| Name | GPS Type | Static position <br> error mean <br> $[\mathrm{m}$ (feet) $]$ | Static position error <br> standard dev. <br> $[\mathrm{m}($ feet $)]$ | Time to <br> first fix <br> [min] | City driving: Percent <br> of time navigation <br> data available |
| :--- | :--- | :--- | :--- | :--- | :--- |


| Magnavox 6400 (10-year old system, outdated) | 2-channel sequencing receiver | 33.48 (110) | 23.17 (76) | ~30 | no nav. data: 10.3\% only 2-D data: $0.2 \%$ full 3-D data: 89.4\% | [MAGNAVOX] <br> Magnavox Advanced Products and Systems |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Magellan OEM GPS Module | 5-channel GPS receiver, OEM type | 22.00 (72) | 16.06 (53) | $\sim 1$ to 2 | no nav. data: $0.0 \%$ only 2-D data: $25.8 \%$ full 3-D data: 74.2\% | [MAGELLAN] <br> Magelan Systems Corp. |
| Magnavox GPS Engine | 5-channel GPS receiver, OEM type | 30.09 (99) | 20.27 (67) | $\sim 1$ to 2 | no nav. data: $3.4 \%$ only 2-D data:5.3\% full 3-D data: 91.2\% | [ROCKWELL] <br> Rockwell International |
| Rockwell NavCore V | 5-channel GPS receiver, OEM type | 28.01 (92) | 19.76 (65) | $\sim 1$ to 2 | no nav. data: $0.0 \%$ only 2-D data: $1.1 \%$ full 3-D data: $98.9 \%$ | [MAGNAVOX] <br> Magnavox Advanced Products and Systems |
| Trimble Placer | 5-channel GPS receiver, OEM type | 29.97 (98) | 23.58 (77) | $\sim 1$ to 2 | no nav. data: $0.0 \%$ only 2-D data:5.2\% full 3-D data: $94.8 \%$ | [TRIMBLE] Trimble Navigation |


| Name | Computer | Onboard <br> Components | Stationary <br> Components | Accuracy <br> - position $[\mathrm{mm}]$ | Accuracy - <br> orientation $\left[{ }^{\circ}\right]$ | Sampling <br> rate $[\mathrm{Hz}]$ | Features | Effective <br> Range |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |


| CONAC (computerized opto-electronic navigation and control) | $486-33 \mathrm{MHz}$ | Structured optoelectronic acquisition beacon (STROAB) | Networked optoelectronic acquisition datum (NOAD) | Indoor $\pm 1.3 \mathrm{~mm}$ outdoor $\pm 5 \mathrm{~mm}$ | Indoor and outdoor $\pm 0.05^{\circ}$ | 25 Hz | 3-D - At least 3 NOADS for one acre. Networkable for unlim. area | Need line-of-sight for at least three NOADS | $\begin{aligned} & \text { [MacLeod, 1993] } \\ & \text { (MTI) } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ROBOSENSE |  | Scanning laser rangefinder | Retroreflective targets | System measures directionand distance to beacons with accuracy $<0.17^{\circ}$ and $<20 \mathrm{~mm}$, respectively Accuracy for robot location and orientation not specified |  | $10-40 \mathrm{~Hz}$ | 2-D - Measure both angle and distance to target | 0.3-30 m | [SIMAN] <br> SIMAN Sensors \& Intelligent Machines Ltd. |
| NAMCO LASERNET beacon tracking system | RS-232 serial interface provided | Rotating mirror pans a near-infrared laser beam through a horizontal arc of $90^{\circ}$ | Retroreflective targets of known dimensions | Angular accuracy is within $\pm 0.05 \%$ with a resolution of $0.006^{\circ}$ Accuracy for robot location and orientation not specified. |  | 20 Hz | Derives distance from computing time of sweep over target of known width | 15 meters (50 ft) | [NAMCO, 1989] |
| TRC beacon navigation system | 6808 integrated computer, RS232 interface | Rotating mirror for scanning laser beam | Retroreflective targets, usually mounted on standalone poles | Resolution is $120 \mathrm{~mm}(4-3 / 4 \mathrm{in})$ in range and $0.125^{\circ}$ in bearing for full $360^{\circ}$ coverage in a horizontal plane |  | 1 Hz | Currently limited to single work area of $80 \times 80 \mathrm{ft}$ | $24.4 \mathrm{~m}(80 \mathrm{ft})$ | [TRC] |
| LASERNAV | 64180 microcomputer | Laser scanner | Retroreflective bar codes. Up to 32 can be distinguished. | $\begin{aligned} & \pm 1 \text { in moving at } 2 \mathrm{ft} / \mathrm{sec} ; \\ & \pm 0.5 \text { in stationary } \end{aligned}$ | $\pm 0.03^{\circ}$. | 90 Hz | 2-D - Measures only angles to reflectors | 30 meters ( 100 ft ) With active reflectors: up to 183 m | [Benayad-Cherif, 1992] and [DBIR] |
| Odyssey | Hand-held | Pole- or wandmounted receiver | Two laser-beam transmitters | Horizontal: $\pm 1 \mathrm{~mm}$ <br> Vertical: $\pm 1 \mathrm{~mm}$ |  | 5 Hz | ~\$90,000 | Indoor: 75 m (250ft) outdoor: <br> 150 m (500ft) | [SPSi] <br> Spatial Positioning Systems, inc |
| BNS (beacon navigation system); 30.5 m |  | Optical IR detector ( $\pm 10^{\circ}$ field of view in horizontal and vertical axes) | Infrared beacon transmitter (uniquely identifiable, 128 codes) |  | $0.3^{\circ}$ in the $\pm 5^{\circ}$ central area and $\pm 1^{\circ}$ out to the periphery of the sensitive area | 10 Hz |  | 500 ft suitable for long corridors | [Benayad-Cherif, 1992] (Denning) |
| Laser scanner + corner cubes | 8086 | Laser scanner | Three corner cubes | $\begin{aligned} & \text { LN-10: } \pm 500 \\ & \text { LN-20: } \pm 20 \\ & \text { LN-30: } \pm 500 \\ & \text { LN-40: } \pm 20 \end{aligned}$ | $\begin{aligned} & \text { LN-10: } \pm 1^{\circ} \\ & \text { LN-20: } \pm 0.1^{\circ} \\ & \text { LN-30: } \pm 1^{\circ} \\ & \text { LN-40: } \pm 0.1^{\circ} \end{aligned}$ | 0.5 Hz |  | LN-10 50 m <br> LN-20 50 m <br> LN-30 200 m <br> LN-40 200 m | [Nishide et al., 1986]. Tokyo Aircraft Instrument Co., Ltd. |
| Laser scanner + bar code |  | Laser scanner | Barcoded target |  |  | 0.033 Hz |  |  | [Murray, 1991] Caterpillar |
| Magnetic markers |  |  | Magnetic markers buried under path ( 50 ft apart) |  |  |  |  |  | [Murray, 1991] <br> Eaton-Kenway |


| Name | Computer | Onboard <br> Components | Stationary <br> Components | Accuracy - <br> position [mm] | Accuracy - <br> orientation [ $\left.{ }^{\circ}\right]$ | Sampling <br> rate [Hz] | Features <br> \&References |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |


| Three object triangulation | $486-33 \mathrm{MHz}$ | Computer vision system |  | Mean error <br> (I) $x=234, y=225$ <br> (G) $x=304, y=301$ <br> (N) $x=17, y=17$ <br> (C) $x=35, y=35$ | Mean error <br> (I) $4.75^{\circ}$ <br> (G) $141.48^{\circ}$ <br> (N) $2.41^{\circ}$ <br> (C) $5.18^{\circ}$ | Mean time <br> (I) 3048.7 <br> (G) 3.8 <br> (N) 33.5 <br> (C) 4.8 | Computer simulation for comparative study of four triangulation algorithms Accuracies are sensitive to landmark location | (I) Iterative Search <br> (G) Geometric triangulation <br> (N) Newton- <br> Raphson <br> (C) Circle intersection | [Cohen and Koss, 1992] <br> Univ. of Michigan |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Laser beam <br> + corner cube | 8086 | Four laser transceivers (transmitter and receiver) | Two corner cube reflectors on both sides of the path | $\begin{aligned} & x=30 \\ & y=2 \end{aligned}$ |  | 10 Hz |  |  | $\begin{aligned} & \text { [Tsumura et al., } \\ & \text { 1988] } \end{aligned}$ |
| Ultrasonic beacons |  | Eight sonar receiver array ( $45^{\circ}$ apart) | Six sonar beacons in a $12 \mathrm{~m}^{2}$ space | Measured standard dev. of path error of 40 mm |  | 150 ms |  |  | [Kleeman, 1992] |
| Infrared beacons |  | One optical infrared scanner | Infrared beacons | $25 \mathrm{~m}^{2}$ test area, beacons $(0,0),(5,0)$ and ( 5,4 ); worst error $=70$ | $\pm 0.2^{\circ}$ |  |  |  | [McGillem and Rappaport, 1988] |
| Laser scanner + corner cube | Z80 | Laser scanner | Retro-reflector <br> $45 \times 45 \mathrm{~m}$ space, 3 <br> reflectors at <br> $\mathrm{A}(0,0), \mathrm{B}(45,0)$, <br> $\mathrm{C}(0,45)$ | Inside DABC: <br> Mean=57, $\sigma .=25$ <br> Outside DABC: <br> mean $=140, \sigma=156$ <br> On line AB or AC <br> mean $=74, \sigma=57$ | Inside DABC : mean $=0.07 \sigma=0.06$ Outside DABC: mean $=0.13, \sigma=0.16$ On line $A B$ or $A C$ : mean $=0.12 \rho=0.05$ |  |  |  | [Tsumura and Hashimoto, 1986] |
| Vision camera + retro-reflectors |  | Vision camera + light source | Retro-reflectors on the path | Path error within 10 mm , at $1 \mathrm{~m} / \mathrm{s}$ |  | 10 Hz |  |  | $\begin{aligned} & \text { [Takeda et al., } \\ & \text { 1986] } \end{aligned}$ |
| Three target triangulation |  | Detector | Active beacon | 100 with very noisy measurement |  |  | Optimize using all beacon data, reweighted least square criterion |  | $\begin{aligned} & \text { [Durieu et al., } \\ & \text { 1989] } \end{aligned}$ |
| Direction measure of several identical beacons |  | Laser scanner | Strips of reflective tapes | At $0.3 \mathrm{~m} / \mathrm{s}$, error $<2 \mathrm{~cm}$ At $1 \mathrm{~m} / \mathrm{s}$, is stable At $1.5 \mathrm{~m} / \mathrm{s}$, instable |  |  | Can navigate on wet rainy field, even when the drive wheels were spinning |  | [Larsson et al, 1994] <br> University of Lulea |
| Triangulation with more than 3 landmarks |  |  | 3 to 20 beacons. | $6.5 \mathrm{~cm} \text { in } 10 \times 10 \mathrm{~m}$ area. | Simulation results only, but simulation includes model of large measurement errors When many beacons available, system can identify and discard outliers (i.e., large errors in the measured angles to some of the beacons) |  |  |  | [Betke and Gurvitz, 1994], MIT |


| Name | Computer | Onboard <br> Components | Features used | Accuracy - <br> position $[\mathrm{mm}]$ | Accuracy - <br> orientation $\left[{ }^{\circ}\right]$ | Sampling <br> Rate $[\mathrm{Hz}]$ | Features | Effective <br> Range, Notes | Reference |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |


| Camera vision robot position and slippage control system | PC | Vision camera | Rectangular ceiling lights, concentric circle | $<100 \mathrm{~mm}$ |  | $>1 \mathrm{~Hz}$ |  |  | Cyberworks, Inc. [CYB] |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Absolute positioning using a single image | 68030, 25 MHz | Fixed vision camera ( 6 m high) discretization $9.5 \times 6.0 \mathrm{~mm}$ for one pixel | Known pattern composed of coplanar points (IR diodes) Test pattern: $1.0 \times 2.8$ m. 84 uniformly distributed points | Accuracy: <br> mean=2,max:10 <br> repeatability X : <br> mean $=0.7$,max: 2 $\sigma=0.8$ <br> Y: mean: 2 <br> max: 5, std. 2 | Repeatability mean: $0.3^{\circ}$ <br> max: $0.7^{\circ}$ <br> std. $0.4^{\circ}$ | 4 Hz | Can monitor robot operation at the same time. 3-D operation. |  | [Fleury and Baron, 1992] <br> Laboratoire d'Automatique et d'Analyse des Systemes |
| Real-time visionbased robot localization | Sun 4/280 computer Karlsruhe mobile robot (KAMRO) | $780 \times 580$ CCDcamera, $\mathrm{f}=8 \mathrm{~mm}$ VISTA real-time image processing system | Vertical edges matching using stored map | 15 mm | $0.1^{\circ}$ | 2 Hz | Correspondence between observed landmarks and a stored map, give bond on the localization error 2-D operation |  | [Atiya and Hager, 1993] <br> University of Karlsruhe |
| Robot localization using common object shapes | Sun workstation | $640 \times 400 \times 4 \mathrm{~b} \text { CCD }$ camera, PC-EYE imaging interface | Objects with a polygon-shaped top and a lateral surface perpendicular to the top | <5\% |  |  | Sensitive at certain orientations |  | [Chen and Tsai, 1991] <br> National Chaio Tung University |
| Omnidirectional vision navigation with beacon recognition |  | Vision camera with fish-eye lens | A light array (3x3) | 40 mm | $0.3{ }^{\circ}$ |  |  |  | [Cao et al., 1986] University of Cincinnati |
| Vision algorithm for mobile vehicle navigation | TRC Labmate | Vision camera | Two sets of four coplanar points are necessary | $\begin{aligned} & 7 \mathrm{~m} \text { distance } \\ & 10 \% \end{aligned}$ |  |  |  |  | [D'Orazio et al., 1991] <br> Istituto <br> Elaborazione <br> Segnali ed Immagini |
| Adaptive position estimation | Litton S-800 486 control MC68000 positioning | Camera, strobe, landmark | Two circles of different radii | 5 mm |  |  | Convergence 120 measurements | Adapt system model using maximum like lihood algorithm | [Lapin, 1992] <br> Georgia Institute of Technology |
| Guidance system using optical reflectors | Sun | Camera, strobe light, (only on 0.3 s ) | Reflector pattern mounted on the ceiling 2 m high |  |  |  |  |  | [Mesaki and Masuda, 1992] Secom Intelligent Systems Laboratory |
| Positioning using a single calibrated object |  | Camera | A sphere with horizontal and vertical calibration great circles | 5\% | $5^{\circ}$ |  | 3-D angle error increases as great circles approach the edge of the sphere Distance error increases with the distance between the robot and landmark |  | [Magee and <br> Aggarwal, 1984] <br> University of Texas |


| Name | Computer | Onboard Components | Features used | Accuracy position [mm] | Accuracy orientation [ ${ }^{\circ}$ ] | Sampling <br> Rate [Hz] | Features | Effective <br> Range, Notes | Reference |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |


| Model based vision system | TRC LabMate $68040$ | $512 \times 512$ gray-level CCD camera, $\mathrm{f}=6$ mm | Corners of the room | $\begin{aligned} & 100 \mathrm{~mm} \\ & \text { middle error 2\% } \end{aligned}$ | $\pm 3^{\circ}$ |  | 3-D orientation error $<0.5^{\circ}$. if the corner is in the center of the image Large error when corner is off image center and angle coefficients of L and R are too small |  | [D'Orazio et al., 1993] Istituto Elaborazione Segnali ed Immagini |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Pose estimation | 9200 image processor | Fairchild 3000 <br> CCD camera $(256 \times 256),$ <br> $\mathrm{f}=13 \mathrm{~mm}$ <br> Perceptics | Quadrangular target $\mathrm{s} 12=77.5, \mathrm{~s} 13=177.5$ <br> $\mathrm{s} 14=162, \mathrm{~s} 23=160$ <br> s24=191,s34=104 | At 1500 mm : <br> 11 mm | At 1500 mm : $1.5^{\circ}$. |  | 3-D volume measurement of tetrahedra composed of feature point triplets extracted from an arbitrary quadrangular target and the lens center |  | [Abidi and Chandra, 1990] University of Tennessee |
| Positioning using standard pattern |  |  | Relative displacement pattern: circle, half white \& half black Identification pattern: bar code | At 5000 mm : $2.2 \%$ | Largest error: $2^{\circ}$ |  | Errors increase with increasing distance, angle between landmark and camera too small or too large |  | [Kabuka and Arenas, 1987] <br> University of Miami |
| TV image processing for robot positioning |  |  | Diamond shape, $90^{\circ}$ angle and 23 cm each side | At 4000 mm : <br> 70 mm | $\begin{aligned} & \text { At } 4000 \mathrm{~mm} \text { : } \\ & \pm 2^{\circ} \end{aligned}$ | 90 s processing time | 2-D | Errors increase with distance and angle too small or too large | [Fukui, 1981] <br> Agency of Industrial Science and Technology |
| Single landmark navigation | ARCTEC Gemini robot | Infrared detector (angular resolution $\pm 4^{\circ}$ ) | Infrared beacons | At 4000 mm : <br> 400 mm <br> At 2400 mm : <br> 200 mm |  |  | 2-D, error increases with the increase of distance between the vehicle and beacon | Running fix: using dead-reckoning info to use measurement obtained at $\mathrm{t}(\mathrm{k}-1)$ at time $\mathrm{t}(\mathrm{k})$ | [Case, 1986] US Army Construction Eng. Research Lab. |
| Robot positioning using opto-electronic processor | $386 \text { PC }$ <br> Image-100 image processing board | $256 \times 256$ camera, $\mathrm{f}=16 \mathrm{~mm}$ Hough transform filter ( $128 \times 128$ ) | Circle ( $\mathrm{R}=107 \mathrm{~mm}$ ) | At 2000 mm 35 mm |  | 30 Hz | 2-D, the result is the fusion of dead reckoning and observed | Errors are function o the distance and angle | [Feng et al., 1992] <br> University of Michigan |
| Global vision |  | Camera mounted at fixed points in the environment |  |  |  |  | Large range over which obstacles can be detected, allows global path planning | Main problems: how many cameras and where to put them? | [Kay and Luo, 1993] <br> North Carolina State University |
| Robot localization using a single image |  | Sony CCD camera, $\mathrm{f}=8.5 \mathrm{~mm}$ resolution $=$ $0.12 \%$ pixel at image center | Vertically oriented parts of fixed objects, e.g., doors, desks and wall junctions Stored map |  | Min. distance to landmark: 1000 mm . orientation $0.2^{\circ}$ |  | 2-D | Utilizes the good angular resolution of a CCD camera, avoids feature correspondence and 3-D reconstruction | [Krotkov, 1991] <br> Laboratoire d'Automatique et d'Analyse des Systemes |
| Autonomous robot for a known environment (ARK) | Two VMEbased cards | CCD camera, IR spot laser rangefinder, custommade pan/tilt table | "Natural" landmarks, e.g., semipermanent structures, doorways) | On the order of centimeters |  |  |  | On the order of $<10 \mathrm{~m}$. | [AECL] |


| Name | Computer | Onboard <br> Components | Features used | Accuracy - <br> position $[\mathrm{mm}]$ | Accuracy - <br> orientation $\left[{ }^{\circ}\right]$ | Sampling <br> Rate $[\mathrm{Hz}]$ | Features | Effective <br> Range, Notes | Reference |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |


| Scanning laser rangefinder |  |  |  | 0.5\%-5\% |  | 1 to 10 kHz or analog | External, local, \$10K100K | 300 m | [Parish and Grabble, 1993], Omnitech Robotics, Inc. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Scanning IR rangefinder |  |  |  | 1\%-10\% |  | 100-1000 or analog | External, local, \$5K20K | 5-50 m | [Parish and Grabble, 1993], Omnitech Robotics, Inc. |
| Scanning (or arrayed) ultrasonic rangefinder |  |  |  | 1\%-10\% |  | 1-100 | External, local, \$1005K | $1-10 \mathrm{~m}$ | [Parish and Grabble, 1993], Omnitech Robotics, Inc. |
| Visual |  |  |  | 1\%-20\% |  | 0.1-100 | External, local, \$50050K | 1-10000 | [Parish and Grabble, 1993], Omnitech Robotics, Inc. |
| Navigation by multi-sensory integration | TRC Labmate | Cohu CCD camera, $\mathrm{f}=16 \mathrm{~mm}$ dead reckoning |  |  |  |  | Integrates position estimates from vision system with odometry using Kalman filter framework |  | [D'Orazio et al., 1993] <br> CNR-IESI |
| Laserradar and sonar based world modeling | Tricycle robot | 24 sonars. four laser rangefinders, rotate at $360^{\circ} / \mathrm{s}$, each scan 720 range points |  |  |  |  | Utilizes heterogeneous info from laser radar and sonars |  | [Buchberger et al., 1993] <br> Kaiserslautern University |
| Vision directed navigation | Sun Sparc for vision, MicroVAX as host, ROBMAC100 tricycle type vehicle | Vision camera | Doors, columns | $\pm 5.0 \mathrm{~cm}$ | $2.0^{\circ}$ | 2 Hz <br> Convex and concave polygons | 3-D |  | University of Waterloo [Wong and Gao, 1992] |
| Robot localization by tracking geometric beacons | Sun-3 for localization Sun-4 vehicle control | One rotating sonar or six fixed sonars | Geometric beacon naturally occurring environment feature |  |  | 1 Hz | EKF utilizes matches between observed geometric beacons anda priori map of beacon locations |  | [Leonard and Durrant-Whyte, 1991] <br> University of Oxford |
| Position estimation using vision and odometry | Differential-drive vehicle $386 \text { PC }$ | $\begin{aligned} & 756 \times 581 \mathrm{CCD} \\ & \text { camera } \\ & \mathrm{f}=12.5 \mathrm{~mm} \end{aligned}$ | Vertical edges and stored map | 40 mm | $0.5^{\circ}$ |  | 2-D - Realistic odometry model and its uncertainty is used to detect and calculate position update fused with observation | Extended Kalman filter to correct the vehicle pose from the error between the observed and estimate angle to each landmark | [Chenavier and Crowley, 1992] LETI-DSYS |


| Name | Computer | Onboard Components | Features used | Accuracy position [mm] | Accuracy orientation [ ${ }^{\circ}$ ] | Sampling <br> Rate [Hz] | Features | Effective <br> Range, Notes | Reference |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |


| Recognize world location with stereo vision |  | Stereo cameras | Long, near vertical stereo features |  |  |  | 1000 real-world data recognition test, under $10 \%$ false negative, zero false positive | Least-squares to find the best fit of model to data and evaluate that fit | [Braunegg, 1993] MITRE Corp. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Environment learning using a distributed representation | Omnidirectional three-wheeled base | a ring of 12 sonars and a compass | Left wall, right wall, corridors |  |  |  | Dynamic landmark detection utilizing robot's motion | Learn the largespace structure of environment by recording its permanent features | $\begin{aligned} & \text { [Mataric, 1990] } \\ & \text { MIT } \end{aligned}$ |
| Localization in structured environment | Motorola M68020 | A ring of 24 sonars | Classify objects into edges, corners, walls, and unknown objects |  |  | 0.1 Hz | Positions resulting from all possible mappings are calculated and then analyzed for clusters The biggest cluster is assumed to be at the true robot position | Each mapping of two model objects onto two reference objects correspond to a certain robot position | [Holenstein et al., 1992] <br> Swiss Federal Inst. of Technology |
| Localization using sonar | SUN 4 | Linear array of three sonars: A. reduce the angular uncertainty, B. help identify the target's class | Local map: feature map (extended reflectors, e.g., wall, and point reflectors) | $<10 \mathrm{~mm}$ | $<1^{\circ}$ |  | Local map: feature extra Matching: least squares EKF for estimating the g different targets and rela | ion <br> metric parameters of d uncertainty | [Sabatini and <br> Benedetto, 1994] <br> Scuola Superiore di <br> Studi Universitari |
| Sonar-based realworld mapping | Neptune mobile robot | Sonars | Probability based occupancy grid map | Map with 30006 in ce well spaced readings ft room can be matche ment and $3^{\circ}$ rotation in | s made from 200 <br> a cluttered $20 \times 20$ <br> with 6 in displace- <br> s of VAX time |  | Map matching by convo displacement and rotatio map into registration with measure of the goodness | ing them It gives the that best brings one the other, with a f match | [Elfes, 1987] Carnegie-Mellon University |
| Comparison of grid-type map building by index of performance (IOP) | Cybermotion K2A synchrodrive robot 38620 MHz PC | A ring of 24 sonars | Histogramic inmotion mapping (HIMM) and heuristic probability function | HIMM results in a sen entries in close proxim locations have a a favo performance value | or grid in which y to actual object able (low) Index of |  | Index of performance (IO correlation between the se objects, as computed by th algorithm, and the actual measured manually The I measure of the differences maps produced by each a | ) computes the sed position of e map-building bject position, as OP gives quantitative in the sensor grid gorithm type | [Raschke and Borenstein, 1990] University of Michigan |
| Comparison of position estimation using occupancy grid |  |  | Local map: grid map Global map: grid map | Best result obtained by matching segment to segment |  |  | Grid to segment matching: generating a mask for the segment and correlating it with the grid map | Segment to segment matching: A. orientation <br> B. collinearity <br> C. overlap | [Schiele and Crowley, 1994] LIFIA |


| Name | Computer | Onboard <br> Components | Features used | Accuracy - <br> position $[\mathrm{mm}]$ | Accuracy - <br> orientation $\left[{ }^{\circ}\right]$ | Sampling <br> Rate $[\mathrm{Hz}]$ | Features | Effective <br> Range, Notes | Reference |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |


| Blanche | MC68020 Tricycle-type mobile robot | Optical rangefinder, res. $=1$ in at $5 \mathrm{ft}, 1000$ samples/rev. in one s. Odometry | 24 line-segment environments map for a $300 \times 200$ in room | 6 in path following |  | Position update every 8 s for a 180 points image and a map of 24 lines. 2-D map. | (1) Least-square for data and model matching <br> (2) Combine odometry and matching for better position estimate using maximum likelihood | Segments Assume the displacement between the data and model is small | [Cox, 1991] <br> NEC Research Institute |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Range map pose estimation | SPARC1+ | 1-D Laser range finder 1000 points/rev | Line segment, corner | Mean error <br> Feature-based: 60 <br> Iconic estimator: 40 <br> In a $10 \times 10 \mathrm{~m}$ space | Max under $1.2^{\circ}$ for both | Feature-based: 0.32 s Iconic: 2 s | 1000 points/rev. <br> Iconic approach matches to the map rather than co small set of features to be | very range data point densing data into a matched to the map | [Schaffer et al., 1992] <br> CMU |
| Positioning using model-based maps |  | A rotatable ring of 12 polaroid sonars | Line segments | $3-5 \mathrm{~cm}$ <br> Coverge if initial estimate is within 1 meters of the true position |  |  | Classification of data points <br> Weighted voting of correction vectors | Clustering sensor data points. Line fitting. | [MacKenzie and Dudek, 1994] McGill University |
| Positioning using optical range data | INMOS-T805 transputer | Infrared scanner | Line segment | The variance never exceeds 6 cm |  |  | Kalman filter position estimation Line fitting Matching, only good matches are accepted | When scans were taken from erronrous pos. matches consistently fail | [Borthwick et al., 1994] <br> University of Oxford |
| World modeling and localization using sonar ranging |  | A ring of 24 sonars | Line segments | $\mathrm{x}=33 \mathrm{~mm}$ <br> covariance: 1 $\mathrm{y}=17 \mathrm{~mm}$ <br> covariance: 1 | $\begin{aligned} & 0.20^{\circ} \\ & \text { covariance: } \\ & 17.106 \end{aligned}$ | A model for the uncertainty in sonars, and the projection of range measurement into external Cartesian coordinate | Extracting line segments from adjacent collinear range measurements and matching these line segments to a stored model | Matching includes: orientation, collinearity, and overlap by comparing one of the parameters in segment representation | [Crowley, 1989] <br> LIFIT(IMAG) |
| 2-D laser rangefinder map building | Sun Sparc | Cyclone 2-D laser rangefinder accuracy $\pm 20 \mathrm{~cm}$, range 50 m | Local map: line segment map Global map: line segments | Max. 5 cm average 3.8 cm |  | On SUN Sparc, 80 ms for local map building and 135 ms for global map update | Matching: remove segment already in the global map from local map, add new segment | Local map: <br> clustering clustering segmentation line fitting | [Gonzalez et al., 1994] <br> Universidad de malaga |


| Name | Computer | Onboard <br> Components | Features used | Accuracy - <br> position $[\mathrm{mm}]$ | Accuracy - <br> orientation $\left[{ }^{\circ}\right]$ | Sampling <br> Rate $[\mathrm{Hz}]$ | Features | Effective <br> Range, Notes | Reference |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |


| Iconic position estimator | Locomotion emulator, all-wheel drive and allwheel steer, Sun Sparc 1 | Cyclone laser range scanner, resolution $=10 \mathrm{~cm}$ range $=50 \mathrm{~m}$ 1000 readings per rev. | In general, has a large number of short line segments | Max. 36 mm mean 19.9 mm | Max. $1.8^{\circ}$ mean $0.73^{\circ}$ |  | Iconic method works directly on the raw sensed data, minimizing the discrepancy between it and the model | Assume small displacement between sensed data and model Two parts: sensor to map data correspondence \& error minimization | [Gonzalez et al., 1992] <br> Carnegie Mellon University |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Environment representation from image data |  |  | Geometrical relationships between observed features rather than their absolute position |  |  |  | A graph where the nodes represent the observed features and edges represent the relationships between features | The recognition problem can be formulated as a graph matching problem | [Taylor, 1991] <br> Yale University |
| Localization via classification of multi-sensor maps |  | Sonars <br> Lateral motion vision <br> Infrared proximity sensor | Local map: multisensor $100 \times 100$ grid maps, cell $20 \times 20 \mathrm{~cm}$ | Using datasets from 10 rooms and hallways, estimate a $94 \%$ recognition rate for rooms, and $98 \%$ for hallways |  | Local grid maps <br> Feature-level sensor fusion by extracting spatial descriptions from these maps | Positioning by classifying the map descriptions to recognize the workspace region that a given map represents | Matching: K-nearest neighbor and minimum Mahalanobis distance | [Courtney and Jain, 1994] <br> Texas Instruments, Inc. |


| Name | Computer | Onboard <br> Components | Maps and <br> Features | Accuracy - <br> position $[\mathrm{mm}]$ | Accuracy - <br> orientation <br> $\left[{ }^{\circ}\right]$ | Sampling <br> Rate $[\mathrm{Hz}]$ | Features <br> Range, <br> Nnotes l |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |


| Guide path sensor (magnetic, optical, inductive, etc.) |  | $0.01-0.1 \mathrm{~m}$ | 100-1000 or analog | External, local, or waypoint indication, \$100-\$5K | 0.01-0.2 m | [Parish and Grabble, 1993] Omnitech Robotics, Inc. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Odor trails for navigation | Applicator for laying volatile chemicals on the floor; olfactory sensor |  |  |  | Unlimited | $\begin{aligned} & \hline \text { [Russell et al., } \\ & \text { 1994] } \\ & \text { Monash University } \end{aligned}$ |
| Thermal path following | Quartz halogen <br> bulb and <br> pyroelectric sensor |  | 0.833 | No need to remove markers after use | Unlimited | [Kleeman and Russell, 1993] <br> Monash University |

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University of Michigan grad. student Ulrich Raschke verifies the proper alignment of ultrasonic sensors. All three robots in this picture use $15^{\circ}$-angular spacing between the sensors. Many researchers agree that $15^{\circ}$ spacing assures complete coverage of the area around the robot.

## References

1. Abidi, M. and Chandra, T., 1990, "Pose Estimation for Camera Calibration and Landmark Tracking." Proceedings of IEEE International Conference on Robotics and Automation Cincinnati, OH, May 13-18, pp. 420-426.
2. Abidi, M. and Gonzalez, R., Editors, 1992, Data Fusion in Robotics and Machine Intelligence Academic Press Inc., San Diego, CA.Acuna, M.H. and Pellerin, C.J., 1969, "A Miniature TwoAxis Fluxgate Magnetometer." IEEE Transactions on Geoscience Electronics Vol. GE-7, pp 252-260.
3. Adams, M.D., 1992, "Optical Range Data Analysis for Stable Target Pursuit in Mobile Robotics." Ph.D. Thesis, Robotics Research Group, University of Oxford, U.K.
4. Adams, M. et al., 1994, "Control and Localisation of a Post Distributing Mobile Robot." 1994 International Conference on Intelligent Robots andSystems (IROS '94), Munich, Germany, Sept. 12-16, pp. 150-156.
5. Adams, M., 1995, "A 3-D Imaging Scanner for Mobile Robot Navigation." Personal Communication. Contact: Dr. Martin Adams, Institute of Robotics, Leonhardstrasse 27, ETH Centre, CH-8092, Switzerland. Ph.: +41-1-632-2539. E-mail: adams@ifr.ethz.ch.
6. Adams, M.D. and Probert, P.J., 1995, "The Interpretation of Phase and Intensity Data from A.M.C.W. Light Detection Sensors for Reliable Ranging." Accepted for publication in the IEEE International Journal of Robotics Research April.
7. Adrian, P., 1991, "Technical Advances in Fiber-Optic Sensors: Theory and Applications." Sensors, Sept.pp. 23-45.
8. Agent, A., 1991, "The Advantages of Absolute Encoders for Motion Control." Sensors, April, pp. 19-24.
9. Allen, D., Bennett, S.M., Brunner, J., and Dyott, R.B., 1994, "A Low Cost Fiber-optic Gyro for Land Navigation." Presented at the SPIE Annual Meeting, San Diego, CA, July.
10. Arkin, R.C., 1989, "Motor-Schema-Based Mobile Robot Navigation." International Journal of Robotics Research, Vol. 8., No. 4, Aug., pp. 92-112.
11. Aronowitz, F., 1971, "The Ring Laser Gyro," Laser Applications, Vol. 1, M. Ross, ed., Academic Press.
12. Arradondo-Perry, J., 1992, "GPS World Receiver Survey." GPS World, January, pp. 46-58.
13. Atiya, S. and Hager, G., 1993, "Real-time Vision-based Robot Localization." IEEE Transactions on Robotics and Automation Vol. 9, No. 6, pp. 785-800.
14. Aviles, W.A. et al., 1991, "Issues in Mobile Robotics: The Unmanned Ground Vehicle Program Teleoperated Vehicle (TOV)." Proceedings of the SPIE - The International Society for Optical Engineering, Vol: 1388 p. 587-97.
15. Avolio, G., 1993, "Principles of Rotary Optical Encoders." Sensors, April, pp. 10-18.
16. Ayache N. and Faugeras, O.D., 1987, "Building a Consistent 3-D Representation of a Mobile Robot Environment by Combining Multiple Stereo Views." Proc. Internaltional Joint Conference on Aritificial Intelligence, pp. 808-810.
17. Baines, N. et al., 1994, "Mobile Robot for Hazardous Environments." Unpublished paper. Atomic Energy of Canada, Ltd., Sheridan Research Park, 2251 Speakman Drive, Mississauga, Ontario, L5K 1B2, Canada, 416-823-9040.
18. Baker, A., 1993, "Navigation System Delivers Precision Robot Control." Design News, Dec. 20, p. 44.
19. Banzil, G., et. al., 1981, "A Navigation Subsystem Using Ultrasonic Sensors for the Mobile Robot Hilare." Proceedings of $1^{\text {st }}$ Conference on Robot Vision and Sensory Control, Stratford/Avon, U.K., April 13.
20. Barrett, C.R., Nix, W.D., and Tetelman, A.S., 1973, "The Principles of Engineering Materials." Prentice Hall, Englewood Cliffs, NJ.
21. Barshan, B. and Durrant-Whyte, H.F., 1993, "An Inertial Navigation System for a Mobile Robot." Proceedings of the 1993 IEEE/RSJ International Conference on Intelligent Robotics and Systems, Yokohama, Japan, July 26-30, pp. 2243-2248.
22. Barshan, B. and Durrant-Whyte, H.F., 1994, "Orientation Estimate for Mobile Robots Using Gyroscopic Information." 1994 International Conference on Intelligent Robots and Systems (IROS '94). Munich, Germany, Sept. 12-16, pp. 1867-1874.
23. Barshan, B. and Durrant-Whyte, H.F., 1995, "Inertial Navigation Systems Mobile Robots." IEEE Transactions on Robotics and Automation Vol. 11, No. 3, June, pp. 328-342.
24. Bauer, R. and Rencken, W. D., 1995, "Sonar Feature Based Exploration." Proceedings of the IEEE/RSJ/GI International Conference on Intelligent Robots and Systems (IROS'95) Pittsburgh, Pennsylvania, August 5-9,, pp. 148-153.
25. Benayad-Cherif, F., Maddox, J., and Muller, L., 1992, "Mobile Robot Navigation Sensors." Proceedings of the 1992 SPIE Conference on Mobile Robots Boston, MA, Nov. 18-20, pp. 378-387.
26. Bennett, S. and Emge, S.R., 1994, "Fiber-optic Rate Gyro for Land Navigation and Platform Stabilization." Presented at Sensors Expo '94, Cleveland, OH, Sept. 20.
27. Betke, M and Gurvits, L., 1994, "Mobile Robot Localization Using Landmarks." 1994 International Conference on Intelligent Robots and Systems (IROS'94) Munich, Germany, Sept. 12-16, pp.135-142.
28. Beyer, J., Jacobus, C., and Pont, F., 1987, "Autonomous Vehicle Guidance Using Laser Range Imagery." SPIE Vol. 852, Mobile Robots II, Cambridge, MA, Nov, pp. 34-43.
29. Biber, C., Ellin, S., and Shenk, E., 1987, "The Polaroid Ultrasonic Ranging System." Audio Engineering Society, $67^{\text {th }}$ Convention, New York, NY, Oct.-Nov.
30. Binger, N. and Harris, S.J., 1987, "Applications of Laser Radar Technology." Sensors, April, pp. 42-44.
31. Boltinghouse, S., Burke, J., and Ho, D., 1990, "Implementation of a 3D Laser Imager Based Robot Navigation System with Location Identification." SPIE Vol. 1388, Mobile Robots V, Boston, MA, Nov., pp. 14-29.
32. Boltinghouse, S. and Larsen, T., 1989, "Navigation of Mobile Robotic Systems Employing a 3D Laser Imaging Radar." ANS Third Topical Meeting on Robotics and Remote Systems Section 2-5, Charleston, SC, March, pp. 1-7.
33. Bolz, R.E. and Tuve, G.L., Ed., 1979, CRC Handbook of Tables for Applied Engineering Science, CRC Press, Boca Raton, FL.
34. Borenstein, J. and Koren, Y., 1985, "A Mobile Platform For Nursing Robots." IEEE Transactions on Industrial Electronics, Vol. 32, No. 2, pp. 158-165.
35. Borenstein, J. and Koren, Y., 1986, "Hierarchical Computer System for Autonomous Vehicle." Proceedings of the 8th Israeli Convention on CAD/CAM and Robotics Tel-Aviv, Israel, December 2-4.
36. Borenstein, J., 1987, "The Nursing Robot System." Ph. D. Thesis, Technion, Haifa, Israel, June, pp. 146-158.
37. Borenstein, J. and Koren, Y., 1987, "Motion Control Analysis of a Mobile Robot." Transactions of ASME, Journal of Dynamics, Measuremert and Control, Vol. 109, No. 2, pp. 73-79.
38. Borenstein, J. and Koren, Y., 1990, "Real-Time Obstacle Avoidance for Fast Mobile Robots in Cluttered Environments." IEEE International Conference on Robotics and Automation, Vol. CH2876-1, Cincinnati, OH, pp. 572-577, May.
39. Borenstein, J. and Koren, Y., 1991a, "The Vector Field Histogram - Fast Obstacle-Avoidance for Mobile Robots." IEEE Journal of Robotics and Automation, Vol. 7, No. 3., June, pp. 278-288.
40. Borenstein, J, and Koren, Y., 1991, "Histogramic In-motion Mapping for Mobile Robot Obstacle Avoidance." IEEE Journal of Robotics and Automation Vol. 7, No. 4, 1991, pp. 535-539.
41. Borenstein, J., 1992, "Compliant-linkage Kinematic Design for Multi-degree-of-freedom Mobile Robots ." Proceedings of the SPIE Symposium on Advances in Intelligent Systems Mobile Robots VII, Boston, MA, Nov. 15-20, pp. 344-351.
42. Borenstein, J., 1993, "Multi-layered Control of a Four-Degree-of-Freedom Mobile Robot With Compliant Linkage." Proceedings of the 1993 IEEE International Conerence on Robotics and Automation, Atlanta, GA, May 2-7, pp. 3.7-3.12.
43. Borenstein, J., 1994a, "The CLAPPER: A Dual-drive Mobile Robot with Internal Correction of Dead-reckoning Errors." Proceedings of IEEE International Conference on Robotics and Automation, San Diego, CA, May 8-13, pp. 3085-3090.
44. Borenstein, J., 1994b, "Internal Correction of Dead-reckoning Errors With the Smart Encoder Trailer." 1994 International Conference on Intelligent Robots and Systems (IROS '94) Munich, Germany, Sept. 12-16, pp. 127-134.
45. Borenstein, J., 1994c, "Four-Degree-of-Freedom Redundant Drive Vehicle With Compliant Linkage." Video Proceedings of the 1994 IEEE International Conference on Robotics ard Automation, San Diego, CA, May 8-13.
46. Borenstein, J. and Feng, L., 1994, "UMBmark - A Method for Measuring, Comparing, and Correcting Dead-reckoning Errors in Mobile Robots." Technical Report, The University of Michigan UM-MEAM-94-22, Dec.
47. Borenstein, J., 1995a, "Control and Kinematic Design for Multi-degree-of-freedom Mobile Robots With Compliant Linkage." IEEE Transactions on Robotics and Automation Vol. 11, No. 1, Feb., pp. 21-35.
48. Borenstein, J., 1995b, "Internal Correction of Dead-reckoning Errors With the Compliant Linkage Vehicle." Journal of Robotic Systems, Vol. 12, No. 4, April, pp. 257-273.
49. Borenstein, J. and Koren, Y., 1995, "Error Eliminating Rapid Ultrasonic Firing for Mobile Robot Obstacle Avoidance." IEEE Transactions on Robotics and Automation Vol. 11, No. 1, Feb., pp 132-138.
50. Borenstein, J., Wehe, D., Feng, C., and Koren, Y., 1995, "Mobile Robot Navigation in Narrow Aisles with Ultrasonic Sensors." Presented at the ANS 6th Topical Meeting on Robotics and Remote Systems, Monterey, CA, Feb. 5-10.
51. Borenstein, J. and Feng, L., 1995a, "Measurement and Correction of Systematic Odometry Errors in Mobile Robots." Accepted for publication as a regular paper in the IEEE Transactions on Robotics and Automation Apr.
52. Borenstein, J. and Feng. L., 1995b, "Correction of Systematic Dead-reckoning Errors in Mobile Robots.' Proceedings of the 1995 International Conference on Intelligent Robots and Systems (IROS '95), Pittsburgh, PA, Aug. 5-9, pp. 569-574.
53. Borenstein, J. and Feng. L., 1995c, "UMBmark: A Benchmark Test for Measuring Deadreckoning Errors in Mobile Robots." 1995 SPIE Conference on Mobile Robots, Philadelphia, October 22-26.
54. Borenstein, J., 1995, Video, "The CLAPPER: A Dual-drive Mobile Robot With Internal Correction of Dead-reckoning Errors." Video Proceedings of the 1995 IEEE International Conference on Robotics and Automation, Nagoya, Japan, May 21-27.
55. Borenstein J. and Feng, L., 1996, "Gyrodometry: A New Method for Combining Data from Gyros and Odometry in Mobile Robots." Accepted for presentation at the 1996 IEEE International Conference on Robotics and Automation Minneapolis, Apr. 22-28, 1996.
56. Brooks, R., 1985, "Visual Map Making for a Mobile Robot." Proceedings of IEEE International Conference on Robotics and Automation St. Louis, MO, March 25-28, pp. 824829.
57. Brown, R.G., Hwang, P.Y.C., 1992, Introduction to Random Signals and Applied Kalman Filtering. 2nd ed., John Wiley and Sons, New York, NY.
58. Buchberger, M., Jörg, K., and Puttkamer, E., 1993, "Laserradar and Sonar Based World Modeling and Motion Control for Fast Obstacle Avoidance of the Autonomous Mobile Robot

MOBOT-IV." Proceedings of IEEE International Conference on Robotics and Automation Atlanta, GA, May 10-15, pp. 534-540.
59. Buholz, N. and Chodorow, M., 1967, "Acoustic Wave Amplitude Modulation of a Multimode Ring Laser." IEEE Journal of Quantum Electronics, Vol. QE-3, No. 11, Nov., pp. 454-459.
60. Bulkeley, D., 1993, "The Quest for Collision-Free Travel." Design News, Oct. 4.
61. Burns, W.K., Chen, C.L., and Moeller, R.P., 1983, "Fiber-Optic Gyroscopes with Broad-Band Sources." IEEE Journal of Lightwave Technology, Vol. LT-1, p. 98.
62. Byrd, J.S. and DeVries, K.R., 1990, "A Six-Legged Telerobot for Nuclear Applications Development, International Journal of Robotics Research Vol. 9, April, pp. 43-52.
63. Byrne, R.H., 1993, "Global Positioning System Receiver Evaluation Results." Sandia Report SAND93-0827, Sandia National Laboratories, Albuquerque, NM, Sept.
64. Byrne, R.H., Klarer, P.R., and Pletta, J.B., 1992, "Techniques for Autonomous Navigation." Sandia Report SAND92-0457, Sandia National Laboratories, Albuquerque, NM, March.
65. Cao, Z., Roning, J., and Hall, E., 1986, "Omnidirectional Vision Navigation Integrating Beacon Recognition with Positioning." Proceedings of the 1986 SPIE Conference on Mobile Robots, Cambridge, MA, Oct. 30-31, pp. 213-220.
66. Carter, E.F., Ed., 1966, Dictionary of Inventions and Discoveries, Crane, Russak, and Co., New York, NY.
67. Case, M., 1986, "Single Landmark Navigation by Mobile Robot." Proceedings of the 1986 SPIE Conference on Mobile Robots, Cambridge, MA, Oct. 30-31, pp. 231-237.
68. Chao, S., Lim, W.L., and Hammond, J.A., 1984, "Lock-in Growth in a Ring Laser Gyro." Proceedings, Physics and Optical Ring Gyros Conference, SPIE Vol 487, Snowbird, UT, January, pp. 50-57.
69. Chen, H.H., 1991, "Pose Estimation from Line-to-Plane Correspondences." IEEE Transaction on Pattern Analysis and Machine Intelligence, vol. 13, no. 6, pp. 530-541.
70. Chen, S. and Tsai, W., 1991, "Determination of Robot Locations by Common Object Shapes." IEEE Transactions on Robotics and Automation Vol. 7, No. 1, pp. 149-156.
71. Chen, Y.D., Ni, J., and Wu, S.M., 1993, "Dynamic Calibration and Compensation of a 3D Lasar Radar Scanning System." IEEE International Conference on Robotics and Automation, Atlanta, GA, Vol. 3, May, pp. 652-664.
72. Chenavier, F. and Crowley, J., 1992, "Position Estimation for a Mobile Robot Using Vision and Odometry." Proceedings of IEEE International Conference on Robotics and Automation, Nice, France, May 12-14, pp. 2588-2593.
73. Chesnoy, J., 1989, "Picosecond Gyrolaser." Optics Letters, Vol 14, No. 18, Sept., pp. 990992.
74. Chow, W.W., Gea-Banacloche, J., Pedrotti, L.M., Sanders, V.E., Schleich, W., and Scully, M.O., 1985, "The Ring Laser Gyro." Reviews of Modern Physics, Vol. 57, No. 1, January, pp. 61-104.
75. Christian, W.R.and Rosker, M.J., 1991, "Picosecond Pulsed Diode Ring Laser Gyroscope." Optics Letters, Vol. 16, No. 20, Oct., pp. 1587-1589.
76. Clark, R.R., 1994, "A Laser Distance Measurement Sensor for Industry and Robotics." Sensors, June, pp. 43-50.
77. Cohen, C. and Koss, F., 1992, "A Comprehensive Study of Three Object Triangulation." Proceedings of the 1993 SPIE Conference on Mobile Robots,Boston, MA, Nov. 18-20, pp. 95-106.
78. Congdon, C., et al, 1993, CARMEL Versus FLAKEY - A Comparison of Two Winners. AI Magazine, Winter, pp. 49-56.
79. Conrad, D.J. and Sampson, R.E., 1990, "3D Range Imaging Sensors." in Traditional and Non-Traditional Robotic Sensors, T.C. Henderson, ed., NATO ASI Series, Vol. F63, SpringerVerlag, pp. 35-47.
80. Cooper, S. and Durrant-Whyte, H., 1994, "A Kalman Filter for GPS Navigation of Land Vehicles." 1994 International Conference on Intelligent Robots and Systems (IROS '94) Munich, Germany, Sept. 12-16, pp. 157-163.
81. Courtney, J. and Jain, A., 1994, "Mobile Robot Localization via Classification of Multisensor Maps." Proceedings of IEEE International Conference on Robotics and Automation San Diego, CA, May 8-13, pp. 1672-1678.
82. Cox, I.J., 1991, "Blanche - An Experiment in Guidance and Navigation of an Autonomous Mobile Robot." IEEE Transactions Robotics and Automation 7(3), pp. 193-204.
83. Crowley, J., 1989, "World Modeling and Position Estimation for a Mobile Robot Using Ultrasonic Ranging." Proceedings of IEEE International Conference on Robotics and Automation, Scottsdale, AZ, May 14-19, pp. 674-680.
84. Crowley, J.L. and Reignier, P., 1992, "Asynchronous Control of Rotation and Translation for a Robot Vehicle." Robotics and Autonomous Systems, Vol. 10, pp. 243-251.
85. DeCorte, C., 1994, "Robots Train for Security Surveillance." Access Control, June, pp. 37-38.
86. Deveza, R., Thiel, D., Russell, R.A., and Mackay-Sim, A., 1994, "Odour Sensing for Robot Guidance." The International Journal of Robotics Research, Vol. 13, No. 3, June, pp. 232239.
87. D'Orazio, T., Capozzo, L., Ianigro, M., and Distante, A., 1993, "Model Based Vision System for Mobile Robot Position Estimation." Proceedings of the 1993 SPIE Conference on Mobile Robots, Boston, MA, Sept. 9-10, pp. 38-49.
88. D'Orazio, T., Distante, A., Attolico, G., Caponetti, L., and Stella, E., 1991, "A Vision Algorithm for Mobile Vehicle Navigation." Proceedings of the 1991 SPIE Conference an Mobile Robots, Boston, MA, Nov. 14-15, pp. 302-309.
89. D'Orazio, T., Ianigro, M., Stella, E., Lovergine, F., and Distante, A., 1993, "Mobile Robot Navigation by Multi-Sensory Integration." Proceedings of IEEE International Conference on Robotics and Automation, Atlanta, GA, May 10-15, pp. 373-379.
90. Dahlin, T. and Krantz, D., 1988, "Low-Cost, Medium-Accuracy Land Navigation System." Sensors, Feb., pp. 26-34.
91. Depkovich, T. and Wolfe, W., 1984, "Definition of Requirements and Components for a Robotic Locating System." Final Report No. MCR-83-669, Martin Marietta Aerospace, Denver, CO, February.
92. Dibburn, U. and Petersen, A., 1983, "The Magnetoresistive Sensor - A Sensitive Device for Detecting Magnetic Field Variations." Electronic Components and Applications, Vol. 5, No. 3, June.
93. Dodington, S.H., 1989, "Electronic Navigation Systems." Electronic Engineer's Handbook, D. Christiansen and D. Fink, eds., 3rd edition, McGraw Hill, New York, pp. 76-95.
94. Dunlap, G.D. and Shufeldt, H.H., Dutton's Navigation and Piloting, Naval Institute Press, pp. 557-579.
95. Durieu, C., Clergeot, H., and Monteil, F., 1989, "Localization of a Mobile Robot with Beacons Taking Erroneous Data Into Account." Proceedings of IEEE International Conference an Robotics and Automation, Scottsdale, AZ, May 14-19, pp. 1062-1068.
96. Duchnowski, L.J., 1992, "Vehicle and Driver Analysis with Real-Time Precision Location Techniques." Sensors, May, pp. 40-47.
97. Edlinger, T. and Puttkamer, E., 1994, "Exploration of an Indoor Environment by an Autonomous Mobile Robot." International Conference on Intelligent Robots and Systens (IROS '94). Munich, Germany, Sept. 12-16, pp. 1278-1284.
98. Elfes, A., 1987, "Sonar-Based Real-World Mapping and Navigation." IEEE Journal of Robotics and Automation, Vol. RA-3, No. 3, pp. 249-265.
99. Elfes, A., 1989, "Using Occupancy Grids for Mobile Robot Perception and Navigation." Computer, June, pp. 46-57.
100. Ellowitz, H.I., 1992, "The Global Positioning System." Microwave Journal, April, pp. 24-33.
101. Engelson, S. and McDermott, D., 1992, "Error Correction in Mobile Robot Map Learning." Proceedings of IEEE International Conference on Robotics and Automation Nice, France, May 12-14, pp. 2555-2560.
102. Evans, J. M., 1994, "HelpMate: An Autonomous Mobile Robot Courier for Hospitals." 1994 International Conference on Intelligent Robots and Systems (IROS '94). Munich, Germany, Sept. 12-16, pp. 1695-1700.
103. Everett, H.R., 1982, "A Computer Controlled Autonomous Sentry Robot." Masters Thesis, Naval Postgraduate School, Monterey, CA, October.
104. Everett, H.R., 1985, "A Multi-Element Ultrasonic Ranging Array." Robotics Age, July, pp. 13-20.
105. Everett, H.R., Gilbreth, G.A., Tran, T., and Nieusma, J.M., 1990, "Modeling the Environment of a Mobile Security Robot." Technical Document 1835, Naval Command Control and Ocean Surveillance Center, San Diego, CA, June.
106. Everett, H.R., Gage, D.W., Gilbreth, G.A., Laird, R.T., and Smurlo, R.P., 1994, "Real-World Issues in Warehouse Navigation." Proceedings SPIE Mobile Robots IX Volume 2352, Boston, MA, Nov.2-4.
107. Everett, H. R., 1995, Sensors for Mobile Robots: Theory and Application ISBN 1-56881-048-2, A K Peters, Ltd., Wellesley, MA.
108. Ezekial, S. and Arditty, H.J., Ed., "Fiber Optic Rotation Sensors and Related Technologies." Proceedings of the First International Conference, MIT, Springer-Verlag, New York.
109. Fan, Z., Borenstein, J., Wehe, D., and Koren, Y., 1994, "Experimental Evaluation of an Encoder Trailer for Dead-reckoning in Tracked Mobile Robots." Technical Report, The University of Michigan, UM-MEAM-94-24, December.
110. Fan, Z., Borenstein, J., Wehe, D., and Koren, Y.,1995, "Experimental Evaluation of an Encoder Trailer for Dead-reckoning in Tracked Mobile Robots" To be presented at the 10th IEEE International Symposium on Intelligent Control Aug. 27-29.
111. Feng, L., Koren, Y., and Borenstein, J., 1994, "A Model-Reference Adaptive Motion Controller for a Differential-Drive Mobile Robot." Proceedings of IEEE International Conference on Robotics and Automation, San Diego, CA, May 8-13, pp. 3091-3096.
112. Feng, L., Fainman, Y., and Koren, Y., 1992, "Estimate of Absolute Position of Mobile Systems by Opto-electronic Processor," IEEE Transactions on Man, Machine and Cybernetics Vol. 22, No. 5, pp. 954-963.
113. Fenn, R.C., Gerver, M.J., Hockney, R.L., and Johnson, B.G., 1992, "Microfabricated Magnetometer Using Young's Modulous Changes in Magnetoelastic Materials." SPIE Vol. 1694.
114. Fennema, C., Hanson, A., Riseman, E., Beveridge, J.R., and Kumar, R., 1990, "Model-Directed Mobile Robot Navigation." IEEE Transactions on Systems, Man, and Cybernetics, vol 20, no 6, November, pp. 1352-1369.
115. Figueroa, J.F. and Lamancusa, J.S., 1992, "A Method for Accurate Detection of Time of Arrival: Analysis and Design of an Ultrasonic Ranging System." Journal of the Acoustical Society of America, Vol. 91, No. 1, January, pp. 486-494.
116. Figueroa, J.F., Doussis, E., and Barbieri, E., 1992, "Ultrasonic Ranging System for 3-D Tracking of a Moving Target." 92-WA/DSC-3, Proceedings, Winter Annual Meeting, American Society of Mechanical Engineers, Anaheim, CA, November.
117. Figueroa, J.F. and Barbieri, E., 1991, "Increased Measurement Range Via Frequency Division in Ultrasonic Phase Detection Methods." Acustica, Vol. 73, pp. 47-49.
118. Figueroa, J.F. and Mahajan, A., 1994, "A Robust Navigation System for Autonomous Vehicles Using Ultrasonics." Control Engineering Practice, Vol. 2, No. 1, pp. 49-59.
119. Fischler, M.A. and Bolles, R.C. , 1981, "Random Sample Consensus: A Paradigm for Model Fitting with Application to Image Analysis and Automated Cartography" Commumination ACM, vol. 24, no. 6, pp. 381-395.
120. Fisher, D., Holland, J.M., and Kennedy, K.F., 1994, "K3A Marks Third Generation SynchroDrive." American Nuclear Society Winter Meeting, Proceedings of Robotics and Remot Systems, New Orleans, LA, June.
121. Fleury, S. and Baron, T., 1992, "Absolute External Mobile Robot Localization Using a Single Image." Proceedings of the 1992 SPIE Conference onMobile Robots, Boston, MA, Nov. 1820, pp. 131-143.
122. Fox, K., 1993, "Indoor Robots Starts Flying Blind." Science, Vol. 261, Aug. 6, pp. 685.
123. Fraden, J., 1993, AIP Handbook of Modern Sensors, ed., Radebaugh, R., American Institute of Physics, New York.
124. Frederiksen, T.M. and Howard, W.M., 1974, "A Single-Chip Monolithic Sonar System." IEEE Journal of Solid State Circuits, Vol. SC-9, No. 6, December.
125. Fukui, I., 1981, "TV Image Processing to Determine the Position of a Robot Vehicle." Pattern Recognition, Vol. 14, pp. 101-109.
126. Ganapathy, S., 1984, "Decomposition of Transformation Matrices for Robot Vision." Proceedings of the IEEE International Conference on Robdics and Automation, pp. 130-139.
127. Getting, I.A., 1993, "The Global Positioning System," IEE Spectrum, December, pp. 36-47.
128. Geyger, W.A., 1957, Magnetic Amplifier Circuits, $2^{\text {nd }}$ ed., McGraw-Hill, New York.
129. Gilbert, W., 1992, "De Magnete." 1600. (Translation: P.F. Mottelay, John Wiley, 1893.)
130. Gonzalez, J., Stentz, A., and Ollero, A., 1992, "An Iconic Position Estimator for a 2D Laser RangeFinder." Proceedings of IEEE International Conference on Robotics and Automation Nice, France, May 12-14, pp. 2646-2651.
131. Gonzalez, R. and Wintz, P., 1977, "Digital Image Processing." Addison-Wesley, Reading, MA.
132. Gonzalez, J., Ollero, A., and Reina, A., 1994, "Map Building for a Mobile Robot Equipped with a 2D Laser Rangefinder." Proceedings of IEEE International Conference on Robotics and Automation, San Diego, CA, May 8-13, pp. 1904-1909.
133. Gothard, B.M., Etersky, R.D., and Ewing, R.E., 1993, "Lessons Learned on a Low-Cost Global Navigation System for the Surrogate Semi-Autonomous Vehicle." SPIE Proceedings, Vol. 2058, Mobile Robots VIII, pp. 258-269.
134. Gould, L., 1990, "Is Off-Wire Guidance Alive or Dead?" Managing Automation, May, pp. 38-40.
135. Gourley, C. and Trivedi, M., 1994, "Sensor Based Obstacle Avoidance and Mapping for Fast Mobile Robots." Proceedings of IEEE International Conference on Robotics and Automation, San Diego, CA, May 8-13, pp. 1306-1311.
136. GPS Report. November 5, 1992. Potomac, MD: Phillips Business Information.
137. Grenoble, B., 1990, "Sensor and Logic Form Digital Compass." Electronic Design News, Dec. 6, pp. 228-229.
138. Gunther, J., 1994, "Robot Asks, Where Am I?" Popular Science, Feb., pp. 32.
139. Hager, G. and Atiya, S., 1993, "Real-Time Vision-Based Robot Localization." IEEE Transaction on Robotics and Automation, vol. 9, no. 6, pp. 785-800.
140. Hammond, W., 1993, "Smart Collision Avoidance Sonar Surpasses Conventional Systems." Industrial Vehicle Technology '93: Annual Review of Industrial Vehicle Design ard Engineering, UK and International Press, pp. 64-66.
141. Haralick R.M. et al., 1989, "Pose Estimation from Corresponding Point Data." IEEE Transactions on Systems, Man, and Cybernetics vol 19, no 6, pp. 1426-1445.
142. Harmon, S.Y., 1986, "USMC Ground Surveillance Robot (GSR): Lessons Learned." Mobile Robots, SPIE Vol. 727, Cambridge, MA, pp. 336-343.
143. Harris, J.C., 1994, "An Infogeometric Approach to Telerobotics," Proceedings, IEEE National Telesystems Conference, San Diego, CA, May, pp. 153-156.
144. Henkel, S.L., 1987, "Optical Encoders: A Review." Sensors, September, pp. 9-12.
145. Henkel, S.L., 1994, "GMR Materials Advance Magnetic Field Detection." Sensors, June, p.8.
146. Hine, A., 1968, Magnetic Compasses and Magnetometers, Adam Hilger Ltd., London.
147. Hinkel, R. and Knieriemen, T., 1988, "Environment Perception with a Laser Radar in a Fast Moving Robot." Symposium on Robot Control 1988 (SYROCO '88), Karlsruhe, Germany, October 5-7, pp. 68.1-68.7.
148. Holenstein, A., Muller, M., and Badreddin, E., 1992, "Mobile Robot Localization in a Structured Environment Cluttered with Obstacles." Proceedings of IEEE International Conference on Robotics and Automation, Nice, France, May 12-14, pp. 2576-2581.
149. Holland, J.M., 1983, Basic Robotics Concepts, Howard W. Sams, Macmillan, Inc., Indianapolis, IN.
150. Holle, S., 1990, "Incremental Encoder Basics." Sensors, April, pp. 22-30.
151. Hollingum, J., 1991, "Caterpillar make the earth move: automatically." The Industrial Robot, Vol. 18, No. 2, pp. 15-18.
152. Hongo, T., Arakawa, H., Sugimoto, G., Tange, K., and Yamamoto, Y., 1987, "An Automated Guidance System of a Self-Controlled Vehicle." IEEE Transactions on Industrial Electronics, Vol. IE-34, No. 1, pp. 5-10.
153. Hoppen, P., Knieriemen, T., and Puttkamer, E., 1990, "Laser-Radar Based Mapping and Navigation for an Autonomous Mobile Robot." Proceedings of IEEE International Conference on Robotics and Automation, Cincinnati, OH, May 13-18, pp. 948-953.
154. Hurn, J., 1993, GPS, A Guide to the Next Utility, No. 16778, Trimble Navigation, Sunnyvale, CA, Nov.
155. Institute of Navigation. 1992. Class notes from "Introduction to GPS/INS Integration," Institute of Navigation GPS-92 Conference, Tutorials, Albuquerque, NM, September 14-15, 1992. Arlington, VA: Navtech Seminars, Inc.
156. Janet, J., Luo, R., Aras, C., and Kay, M., 1993, "Sonar Windows and Geometrically Represented Objects for Mobile Robot Self-Referencing." Proceedings of the 1993 IEEE/RSJ International Conference on Intelligent Robotics and Systems, Yokohama, Japan, July 26-30, pp. 1324-1331.
157. Jenkin, M., Milios, E., Jasiobedzki, P., Bains, N., and Tran, K., 1993, "Global Navigation for ARK." Proceedings of the 1993 IEEE/RSJ International Conference on Intelligent Robotics and Systems, Yokohama, Japan, July 26-30, pp. 2165-2171.
158. Jörg, K.W., 1994, "Echtzeitfähige Multisensorintegration für autonome mobile Roboter" ISBN 3-411-16951-6, B.I. Wissenschaftsverlag, Mannheim, Leipzig, Wien, Zürich.
159. Jörg, K.W., 1995, "World Modeling for an Autonomous Mobile Robot Using Heterogenous Sensor Information." Robotics and Autonomous Systems, Vol. 14, pp. 159-170.
160. Jones, J.L. and Flynn, A., 1993, Mobile Robots: Inspiration to Implementation ISBN 1-56881-011-3, A K Peters, Ltd. Wellesley, MA.
161. Kabuka, M and Arenas, A., 1987, "Position Verification of a Mobile Robot Using Standard Pattern." IEEE Journal of Robotics and Automation Vol. RA-3, No. 6, pp. 505-516.
162. Kadonoff, M.B., 1986, "Navigation Techniques for the Denning Sentry."MS86-757, RI/SME $2^{\text {nd }}$ International Conference on Robotics Research Scottsdale, AZ, August.
163. Kak, A., Andress, K., Lopez-Abadia, and Carroll, M., 1990, "Hierarchical Evidence Accumulation in the PSEIKI System and Experiments in Model-driven Mobile Robot Navigation." in Uncertainty in Artificial Intelligence, Vol. 5, Elsevier Science Publishers B. V., North-Holland, pp. 353-369.
164. Kay, M. and Luo, R., 1993, "Global Vision for the Control of Free-Ranging AGV Systems." Proceedings of IEEE International Conference on Robotics and Automation Atlanta, GA, May 10-15, pp. 14-19.
165. Kenny, T.W., Waltman, S.B., Reynolds, J.K., and Kaiser, W.J., 1991, "Micromachined Silicon Tunnel Sensor for Motion Detection." Applied Physics Letters, Vol. 58, No. 1, January.
166. Kerr, J.R., 1988, "Real Time Imaging Rangefinder for Autonomous Land Vehicles." SPIE Vol. 1007, Mobile Robots III, Cambridge, MA, November, pp. 349-356.
167. Kihara, M. and Okada, T., 1984, "A Satellite Selection Method and Accuracy for the Global Positioning System." Navigation: Journal of the Institute of Navigation Vol. 31, No. 1, Spring., pp. 8-20.
168. Killough, S.M., Pin, F.G., 1992, "Design of an Omnidirectional Holonomic Wheeled Platform Prototype." Proceedings of the IEEE Conference on Robotics and Automation Nice, France, May, pp. 84-90.
169. Kim, E.J., 1986, "Design of a Phased Sonar Array for a Mobile Robot." Bachelor's Thesis, MIT, Cambridge, MA, May.
170. King, S. and Weiman, C., 1990, "HelpMate Autonomous Mobile Robot Navigation System." Proceedings of the 1990 SPIE Conference on Mobile Robots,Boston, MA, Nov. 8-9, pp. 190198.
171. Klarer, P.R., 1988, "Simple 2-D Navigation for Wheeled Vehicles." Sandia Report SAND880540, Sandia National Laboratories, Albuquerque, NM, April.
172. Kleeman, L., 1992, "Optimal Estimation of Position and Heading for Mobile Robots Using Ultrasonic Beacons and Dead-reckoning." Proceedings of IEEE International Conference on Robotics and Automation, Nice, France, May 12-14, pp. 2582-2587.
173. Kleeman, L. and Russell, R., 1993, "Thermal Path Following Robot Vehicle: Sensor Design and Motion Control." Proceedings of the 1993 IEEE/RSJ International Conference on Intelligent Robotics and Systems, Yokohama, Japan, July 26-30, pp. 1319-1323.
174. Koenigsburg, W.D., 1982, "Noncontact Distance Sensor Technology." GTE Laboratories, Inc., 40 Sylvan Rd., Waltham, MA, 02254, March, pp. 519-531.
175. Komoriya, K. and Oyama, E., 1994, "Position Estimation of a Mobile Robot Using Optical Fiber Gyroscope (OFG)." International Conference on Intelligent Robots and Systems (IROS '94). Munich, Germany, Sept. 12-16, pp. 143-149.
176. Koper, J.G., 1987, "A Three-Axis Ring Laser Gyroscope," Sensors, March, pp. 8-21.
177. Kortenkamp, D. and Weymouth, T., 1994, "Combining Sonar and Vision Sensing in the Construction and Use of Topological Maps for Mobile Robots." Submitted to the IEEE Transactions on Robotics and Automation
178. Krotkov, E., 1991, "Mobile Robot Localization Using a Single Image." Proceedings of IEEE International Conference on Robotics and Aubmation, Sacramento, CA, April 9-11, pp. 978983.
179. Kumar, 1988, "Determination of the Camera Location and Orientation." Proc. Image Understanding Workshop 88, pp. 870-881.
180. Kuc, R., and Siegel, M.W., 1987, "A physically-based simulation model for acoustic sensor robot navigation." IEEE Trans. Pattern Analysis and Machine Intelligence PAMI-9, No. 6, pp. 766 -778.
181. Kwiatkowski, W. and Tumanski, S., 1986, "The Permalloy Magnetoresistive Sensors Properties and Applications." J. Phys. E: Sci. Instrum, Vol. 19, pp. 502-515.
182. La, W.H.T., Koogle, T.A., Jaffe, D.L., and Leifer, L.J., 1981, "Microcomputer-Controlled Omnidirectional Mechanism for Wheelchairs." Proceedings, IEEE Frontiers of Engineering in Health Care, CH1621-2/81/0000-0326.
183. Langer, D. and Thorpe, C., 1992, "Sonar Based Outdoor Vehicle Navigation and Collision Avoidance." International Conference on Intelligent Robots and Systems, IROS ‘92, Raleigh, NC, July.
184. Langley, R.B., 1991, "The Mathematics of GPS." GPS World, July/Aug., pp. 45-49.
185. Lapin, B., 1992, "Adaptive Position Estimation for an Automated Guided Vehicle." Proceedings of the 1992 SPIE Conference on Mobile Robots,Boston, MA, Nov. 18-20, pp. 82-94.
186. Larson, T.R. and Boltinghouse, S., 1988, "Robotic Navigation Within Complex Structures." SPIE Vol. 1007, Mobile Robots III, Cambridge, MA, Nov., pp. 339-348.
187. Larsson, U., Zell, C., Hyyppa, K., and Wernersson, A., 1994, "Navigating an Articulated Vehicle and Reversing with a Trailer." Proceedings of IEEE International Conference on Robotics and Automation, San Diego, CA, May 8-13, pp. 2398-2404.
188. Lefevre, H.C., 1992, "The Interferometric Fiber-Optic Gyroscope." in Fiber Optic Sensors, Udd, E., Editor, Vol. CR44, SPIE Optical Engineering Press, Bellingham, WA, Sept.
189. Lenz, J.E., 1990, "A Review of Magnetic Sensors." Proceedings of the IEEE, Vol. 78, No. 6, June.
190. Lenz, R.K. and Tsai, R.Y., 1988, "Techniques for Calibration of the Scale Factor and Image Center for High Accuracy 3-D Machine Vision Metrology." IEEE Transaction on Pattern Analysis and Machine Intelligence, vol. 10, no. 5, pp. 713-720.
191. Leonard, J. and Durrant-Whyte, H.F., 1990, "Application of Multi-Target Tracking to SonarBased Mobile Robot Navigation." International Conference on Decision and Control
192. Leonard, J. and Durrant-Whyte, H. F., 1991, "Mobile Robot Localization by Tracking Geometric Beacons." IEEE Transactions on Robotics and Automaion, Vol. 7, No. 3, pp. 376382.
193. Lewis, R.A. and Johnson, A.R., 1977, "A Scanning Laser Rangefinder for a Robotic Vehicle." 5th International Joint Conference on Artificial Intelligence pp. 762-768.
194. Liu, Y., Huang, T.S., and Faugeras, O.D., 1990, "Determination of Camera Location from 2-D to 3-D Line and Point Correspondence." IEEE Transaction on Pattern Analysis and Machine Intelligence, vol. 12, no. 1, pp. 28-37, 1990.
195. MacLeod, E. and Chiarella, M., 1993, "Navigation and Control Breakthrough for Automated Mobility." Proceedings of the 1993 SPIE Conference on Mobile Robots,Boston, MA, Sept. 9-10, pp. 57-68.
196. Maddox, J., 1994, "Smart Navigation Sensors for Automatic Guided Vehicles." Sensors, April, pp. 48-50.
197. Maenaka, K., Ohgusu, T., Ishida, M., and Nakamura, T., 1987, "Novel Vertical Hall Cells in Standard Bipolar Technology, Electronic Letters, Vol. 23, pp. 1104-1105.
198. Maenaka, K., Tsukahara, M., and Nakamura, T., 1990, "Monolithic Silicon Magnetic Compass." Sensors and Actuators, pp. 747-750.
199. Magee, M. and Aggarwal, J., 1984, "Determining the Position of a Robot Using a Single Calibrated Object." Proceedings of IEEE International Conference on Robotics and Automation, Atlanta, GA, March 13-15, pp. 140-149.
200. Mahajan, A., 1992, "A Navigation System for Guidance and Control of Autonomous Vehicles Based on an Ultrasonic 3-D Location System." Master's Thesis, Mechanical Engineering Department, Tulane University, July.
201. Manolis, S., 1993, "Resolvers vs. Rotary Encoders For Motor Commutation and Position Feedback." Sensors, March, pp. 29-32.
202. Martin, G.J., 1986, "Gyroscopes May Cease Spinning." IEEE Spectrum, February, pp. 48-53.
203. Mataric, M., 1990, "Environment Learning Using a Distributed Representation." Proceedings of IEEE International Conference on Robotics and Automation, Cincinnati, OH, May 13-18, pp. 402-406.
204. Matsuda, T. and Yoshikawa, E., 1989, "Z-shaped Position Correcting Landmark for AGVs." Proceedings of the 28th SICE Annual Conference July 25-27, pp. 425-426.
205. Matsuda T. et al., 1989, "Method of Guiding an Unmanned Vehicle." U.S. Patent \#4,866,617. Issued Sep. 12.
206. Matthies, L. and Shafer, S.A., 1987, "Error Handling in Stereo Navigation." IEEE Transaction on Robotics and Automation, vol. 3, pp. 239-248.
207. McGillem, C. and Rappaport, T., 1988, "Infra-red Location System for Navigation of Autonomous Vehicles." Proceedings of IEEE International Conference on Robotics and Automation, Philadelphia, PA, April 24-29, pp. 1236-1238.
208. McPherson, J.A., 1991, "Engineering and Design Applications of Differential Global Positioning Systems (DGPS) for Hydrographic Survey and Dredge Positioning." Engineering Technical Letter No 1110-1-150, US Army Corps of Engineers Washington, DC, July 1.
209. Menegozzi, L.N., Lamb, W.E., 1973, "Theory of a Ring Laser." Physical Review A, Vol. 1, No. 4, October, pp. 2103-2125.
210. Mesaki, Y. and Masuda, I., 1992, "A New Mobile Robot Guidance System Using Optical Reflectors." Proceedings of the 1992 IEEE/RSJ International Conference on Intelligent Robots and Systems, Raleigh, NC, July 7-10, pp. 628-635.
211. Miller, G.L. and Wagner, E.R., 1987, "An Optical Rangefinder for Autonomous Robot Cart Navigation." Proceedings of the Advances in Intelligent Robotic Systems: SPIE Mobie Robots II.
212. Moravec, H.P., 1981, "Robot Rover Visual Navigation." UMI Research Press, Ann Arbor, Michigan.
213. Moravec, H.P. and Elfes, A., 1985, "High Resolution Maps from Wide Angle Sonar." Proceedings of the IEEE Conference on Robotics and Automation Washington, D.C., pp. 116-121.
214. Moravec, H.P., 1988, "Sensor Fusion in Certainty Grids for Mobile Robots." AI Magazine, Summer, pp. 61-74.
215. Motazed, B., 1993, "Measure of the Accuracy of Navigational Sensors for Autonomous Path Tracking." Proceedings, SPIE Vol. 2058, Mobile Robots VIII pp. 240-249.
216. Murray, C., 1991, "AGVs Go Wireless." Design News, June, pp. 27-28.
217. Nickson, P., 1985, "Solid-State Tachometry." Sensors, April, pp. 23-26.
218. Nishide, K., Hanawa, M., and Kondo, T., 1986, "Automatic Position Findings of Vehicle by Means of Laser." Proceedings of IEEE International Conference on Robđics and Automation, San Francisco, CA, Apr. 7-10, pp. 1343-1348.
219. Nitzan, D. et al. 1977, "The Measurement and Use of Registered Reflectance and Range Data in Scene Analysis." Proceedings of IEEE, Vol. 65, No. 2, Feb., pp. 206-220.
220. Nolan, D.A., Blaszyk, P.E., and Udd, E., 1991, "Optical Fibers." Fiber Optic Sensors: An Introduction for Engineers and Scientists E. Udd, Ed., John Wiley and Sons, Inc., New York, pp. 9-26.
221. Parish, D. and Grabbe, R., 1993, "Robust Exterior Autonomous Navigation." Proceedings of the 1993 SPIE Conference on Mobile Robots,Boston, MA, Sept. 9-10, pp. 280-291.
222. Patterson, M.R., Reidy, J.J., and Rudolph, R.C., 1984, "Guidance and Actuation Systems for an Adaptive-Suspension Vehicle." Final Technical Report, Battelle Columbus Division OH, AD\#A139111, March 20.
223. Pessen, D.W., 1989, "Industrial Automation." ISBN 0-471-60071-7, John Wiley and Sons, Inc.
224. Petersen, A., 1989, "Magnetoresistive Sensors for Navigation." Proceedings, 7th International Conference on Automotive Electronics, London, England, Oct, pp. 87-92.
225. Pin, F.G. and Killough, M., 1994, "A New Family of Omnidirectional and Holonomic Wheeled Platforms for Mobile Robots." IEEE Transactions on Robotics and Automation, Vol. 10, No. 4, Aug., pp. 480-489.
226. Pin, F.G. et al., 1989, "Autonomous Mobile Robot Research Using the HERMIES-III Robot." IROS International Conference on Intelligent Robot and Systems Tsukuba, Japan, Sept.
227. Pin, F.G. and Watanabe, Y., 1993, "Using Fuzzy Behaviors for the Outdoor Navigation of a Car with Low-Resolution Sensors." IEEE International Conference on Robotics and Automation, Atlanta, Georgia, May 2-7, pp. 548-553.
228. Pletta, J.B., Amai, W.A., Klarer, P., Frank, D., Carlson, J., and Byrne, R., 1992, "The Remote Security Station (RSS) Final Report." Sandia Report SAND92-1947 for DOE under Contract DE-AC04-76DP00789, Sandia National Laboratories Albuquerque, NM, Oct.
229. Premi, K.S. and Besant, C.B., 1983, "A Review of Various Vehicle Guidance Techiques That Can be Used by Mobile Robots or AGVS." 2nd International Conference on Automated Guided Vehicle Systems, Stuttgart, Germany, June.
230. Primdahl, F., 1970, "The Fluxgate Mechanism, Part I: The Gating Curves of Parallel and Orthogonal Fluxgates." IEEE Transactions on Magnetics, Vol. MAG-6, No. 2, June.
231. Primdahl, F., 1979, "The Fluxgate Magnetometer." J. Phys. E: Sci. Instrum., Vol. 12, pp. 241253.
232. Purkey, M., 1994, "On Target." Golf Magazine, May, pp. 120-121.
233. Raschke, U. and Borenstein, J., 1990, "A Comparison of Grid-type Map-building Techniques by Index of Performance." Proceedings of IEEE International Conference on Robotics and Automation, Cincinnati, CA, May 13-18, pp. 1828-1832.
234. Reister, D.B., 1991, "A New Wheel Control System for the Omnidirectional HERMIES-III Robot." Proceedings of the IEEE Conference on Robotics and Automation Sacramento, California, April 7-12, pp. 2322-2327.
235. Reister, D.B. et al., 1991, "DEMO 89 - The Initial Experiment With the HERMIES-III Robot." Proceedings of the 1991 IEEE Conference on Robdics and Automation Sacramento, California, April, pp. 2562-2567.
236. Reister, D.B. and Unseren, M.A., 1992, "Position and Force Control of a Vehicle with Two or More Steerable Drive Wheels." Internal Report ORNL/TM-12193, Oak Ridge National Laboratories.
237. Reister, D.B. and Unseren, M.A., 1993, "Position and Constraint Force Control of a Vehicle with Two or More Steerable Drive Wheels." IEEE Transactions on Robotics and Automation.Vol. 9, No. 6, December, pp. 723-731.
238. Rencken, W.D., 1993, "Concurrent Localization and Map Building for Mobile Robots Using Ultrasonic Sensors." Proceedings of the 1993 IEEE/RSJ International Conference on Intelligent Robotics and Systems, Yokohama, Japan, July 26-30, pp. 2192-2197.
239. Rencken, W.D., 1994, "Autonomous Sonar Navigation in Indoor, Unknown, and Unstructured Environments." 1994 International Conference on Intelligent Robots and Systems (IROS '94) Munich, Germany, Sept. 12-16, pp. 127-134.
240. Reunert, M.K., 1993, "Fiber Optic Gyroscopes: Principles and Applications." Sensors, August, pp. 37-38.
241. Russell, R.A., Thiel, D., and Mackay-Sim, A., 1994, "Sensing Odor Trails for Mobile Robot Navigation." Proceedings of IEEE International Conference on Robotcs and Automation, San Diego, CA, May 8-13, pp. 2672-2677.
242. Russell, R.A. 1993, "Mobile Robot Guidance Using a Short-lived Heat Trail." Robotica, Vol 11, Part 5, pp. 427-431.
243. Russell, R.A., 1995a, "A Practical Demonstration of the Application of Olfactory Sensing to Robot Navigation." Proceedings of the International Advanced Robotics Programme (IARP), Sydney, Australia, May 18-19, pp. 35-43.
244. Russell, R.A., 1995b, "Laying and Sensing Odor Markings as a Strategy for Assisting Mobile Robot Navigation Tasks." IEEE Robotics and Automation Magazine, Vol. 2, No. 3, Sept., pp. 3-9.
245. Sabatini, A. and Benedetto, O., 1994, "Towards a Robust Methodology for Mobile Robot Localization Using Sonar." Proceedings of IEEE International Conference on Robotics and Automation, San Diego, CA, May 8-13, pp. 3142-3147.
246. Sagnac, G.M., 1913, "L'ether lumineux demontre par l'effet du vent relatif d'ether dans un interferometre en rotation uniforme." C.R. Academy of Science, 95, pp. 708-710.
247. Sammarco, J.J., 1994, "A Navigational System for Continuous Mining Machines." Sensors, Jan., pp. 11-17.
248. Sammarco, J.J., 1990, "Mining Machine Orientation Control Based on Inertial, Gravitational, and Magnetic Sensors." Report of Investigations 9326, US Bureau of Mines, Pittsburgh, PA.
249. Sanders, G.A., 1992, "Critical Review of Resonator Fiber Optic Gyroscope Technology." in Fiber Optic Sensors, Udd, E., Ed., Vol. CR44, SPIE Optical Engineering Press, Bellingham, WA, Sept.
250. Schaffer, G., Gonzalez, J., and Stentz, A., 1992, "Comparison of Two Range-based Pose Estimators for a Mobile Robot." Proceedings of the 1992 SPIE Conference on Mobile Robots, Boston, MA, Nov. 18-20, pp. 661-667.
251. Schiele, B. and Crowley, J., 1994, "A Comparison of Position Estimation Techniques Using Occupancy Grids." Proceedings of IEEE International Conference on Robotics and Automation, San Diego, CA, May 8-13, pp. 1628-1634.
252. Schiele, B. and Crowley, J., 1994, "A Comparison of Position Estimation Techniques Using Occupancy Grids." Robotics and Autonomous Systems, Vol. 12, pp. 163-171.
253. Schultz, W., 1993, "Traffic and Vehicle Control Using Microwave Sensors." Sensors, October, pp. 34-42.
254. Schulz-DuBois, E.O., 1966, "Alternative Interpretation of Rotation Rate Sensing by Ring Laser." IEEE Journal of Quantum Electronics, Vol. QE-2, No. 8, Aug., pp. 299-305.
255. Shoval, S., Benchetrit, U., and Lenz, E., 1995, "Control and Positioning of an AGV for Material Handling in an Industrial Environment." Proceedings of the 27th CIRP International Seminar on Manufacturing Systems, Ann Arbor, MI, May 21-23, pp. 473-479.
256. Siuru, B., 1994, "The Smart Vehicles Are Here." Popular Electronics, Vol. 11, No. 1, Jan., pp. 41-45.
257. Slama, C.C., Editor, 1980, "Manual of Photogrammetry." American Society of Photogrammetry, Falls Church, Virginia, fourth edition.
258. Stokes, K.W., 1989, "Remote Control Target Vehicles for Operational Testing." Association for Unmanned Vehicles Symposium, Washington, DC, July.
259. Stuart, W.F., 1972, "Earth's Field Magnetometry, Reports on Progress in Physics, J.M. Zinman, Ed., Vol. 35, Part 2, pp. 803-881.
260. Stuck, E. R., Manz, A., Green, D. A., and Elgazzar, S., 1994, "Map Updating and Path Planning for Real-Time Mobile Robot Navigation."1994 International Conference on Intelligent Robots and Systems (IROS '94). Munich, Germany, Sept. 12-16, pp. 753-760.
261. Sugihara, K., 1988, "Some Location Problems for Robot Navigation Using a Single Camera." Computer Vision, Graphics and Image Processing vol. 42, no. 1, pp 112-129.
262. Sugiyama, H., 1993, "A Method for an Autonomous Mobile Robot to Recognize its Position in the Global Coordinate System when Building a Map." Proceedings of the 1993 IEEE/RSJ International Conference on Intelligent Robotics and Systems, Yokohama, Japan, July 26-30, pp. 2186-2191.
263. Sutherland, K. T. , 1993, "Landmark Selection for Accurate Navigation." Proc. Image Understanding Workshop 93, pp. 485-490.
264. Tai, S., Kojima, K., Noda, S., Kyuma, K., Hamanaka, K., and Nakayama, T., 1986, "All-Fibre Gyroscope Using Depolarized Superluminescent Diode." Electronic Letters, Vol. 22, p. 546.
265. Talluri, R. and Aggarwal, J.K., 1990, "Position Estimation for a Mobile Robot in an Unstructured Environment." Proc. IEEE Workshop on Intelligent Robots and Systems, IROS '90, pp 159-166.
266. Talluri, R. and Aggarwal, J.K., 1991, "Position Estimation of a Mobile Robot Using Edge Visibility Regions." Proc. IEEE Conf. on Computer Vision and PatternRecognition CVPR '91, pp. 714-715.
267. Talluri, R. and Aggarwal, J.K., 1992, "Transform Clustering for Model-Image Feature Correspondence." Proc. IAPR Workshop on Machine Vision Applications, MVA '92 pp 579-582.
268. Talluri, R., and Aggarwal, J., 1993, "Position Estimation Techniques for an Autonomous Mobile Robot - a Review." in Handbook of Pattern Recognition and Computer Vision World Scientific: Singapore, Chapter 4.4, pp. 769-801.
269. Takeda, T., Kato, A., Suzuki, T., and Hosoi, M., 1986, "Automated Vehicle Guidance Using Spotmark." Proceedings of IEEE International Conference on Robotics and Automation San Francisco, CA, Apr. 7-10, pp. 1349-1353.
270. Taylor, C., 1991, "Building Representations for the Environment of a Mobile Robot from Image Data." Proceedings of the 1991 SPIE Conference on Mobile Robots,Boston, MA, Nov. 14-15, pp. 331-339.
271. Thompson, W.B.,Henderson, T.C.,Colvin, T.L., Dick, L.B., and Valiquette, C.M., 1993, "Vision-Based Localization." Proc. Image Understanding Workshop 93, pp. 491-498.
272. Tonouchi, Y., Tsubouchi, T., and Arimoto, S., 1994, "Fusion of Dead-reckoning Positions With a Workspace Model for a Mobile Robot by Bayesian Inference." International Conference on Intelligent Robots and Systems (IROS '94). Munich, Germany, Sept. 12-16, pp. 1347-1354.
273. Tsai, R.Y., 1986, "A Versatile Camera Calibration Technique for High-Accuracy 3D Machine Vision Metrology Using Off-The-Shelf Cameras and Lenses." IEEE Transaction on Robotics and Automation, vol. 8, no. 2, pp. 129-139.
274. Tsumura, T. and Hashimoto, M., 1986, "Positioning and Guidance of Ground Vehicle by Use of Laser and Corner Cube." Proceedings of IEEE International Conference on Robotics and Automation, San Francisco, CA, Apr. 7-10, pp. 1335-1342.
275. Tsumura, T., 1986, "Survey of Automated Guided Vehicle in Japanese Factory." Proceedings of IEEE International Conference on Robotics and Automation San Francisco, CA, Apr. 7-10, pp. 1329-1334.
276. Tsumura, T., Fujiwara, N., Shirakawa, T., and Hashimoto, M., 1981, "An Experimental System for Automatic Guidance of Roboted Vehicle Following the Route Stored in Memory." Proc. of the 11th Int. Symp. on Industrial Robots Tokyo, Japan, pp. 18-193.
277. Tsumura, T., Hashimoto, M., and Fujiwara, N., 1988, "A Vehicle Position and Heading Measurement System Using Corner Cube and Laser Beam." Proceedings of IEEE International Conference on Robotics and Automation, Philadelphia, PA, Apr. 24-29, pp. 4753.
278. Turpin, D.R., 1986, "Inertial Guidance: Is It a Viable Guidance System for AGVs?" 4th International Conference on AGVs (AGVS4), June, pp. 301-320.
279. Udd, E., 1985, "Fiberoptic vs. Ring Laser Gyros: An Assessment of the Technology." in Laser Focus/Electro Optics, Dec.
280. Udd, E., 1991, "Fiberoptic Sensors Based on the Sagnac Interferometer and Passive Ring Resonator." in Fiber Optic Sensors: An Introduction for Engineers and Scientists E. Udd, Ed., John Wiley and Sons, Inc., New York, pp. 233-269.
281. Vaganay, J., Aldon, M.J., and Fournier, A., 1993a, "Mobile Robot Attitude Estimation by Fusion of Inertial Data." Proceedings of IEEE International Conference on Robotics and Automation, Atlanta, GA, May 10-15, pp. 277-282.
282. Vaganay, J., Aldon, M.J., and Fournier, A., 1993b, "Mobile Robot Localization by Fusing Odometric and Inertial Measurements." $5^{\text {th }}$ Topical Meeting on Robotics and Remote Systems, Knoxville, TN, Vol. 1, Apr., pp. 503-510.
283. Vestli, S.J., Tschichold-Gürman, N., Adams, M., and Sulzberger, S., 1993, "Amplitude Modulated Optical Range Data Analysis in Mobile Robotics." Proceedings of the 1993 IEEE International Conference on Robotics and Automation, Atlanta, GA, May 2-7, pp 3.243 3.248 .
284. Vuylsteke, P., Price, C.B., and Oosterlinck, A., 1990, "Image Sensors for Real-Time 3D Acquisition, Part 1." Traditional and Non-Traditional Robotic Sensors, T.C. Henderson, Ed., NATO ASI Series, Vol. F63, Springer-Verlag, pp. 187-210.
285. Wax, S.I. and Chodorow, M., 1972, "Phase Modulation of a Ring-Laser Gyro - Part II: Experimental Results," IEEE Journal of Quantum Electronics, March, pp. 352-361.
286. Weiß, G., Wetzler, C., and Puttkamer, E., 1994, "Keeping Track of Position and Orientation of Moving Indoor Systems by Correlation of Range-Finder Scans." 1994 International Conference on Intelligent Robots and Systems (IROS'94), Munich, Germany, Sept. 12-16, pp. 595-601.
287. Wienkop, U., Lawitzky, G., and Feiten, W., 1994, "Intelligent Low-cost Mobility." 1994 International Conference on Intelligent Robots and Systems (IROS '94). Munich, Germany, Sept. 12-16, pp. 1708-1715.
288. Wiley, C.M., 1964, "Navy Tries Solid-State Compass." Electronics, Feb. 14, pp. 57-58.
289. Wilkinson, J.R., 1987, "Ring Lasers." Progress in Quantum Electronics, edited by Moss, T.S., Stenholm, S., Firth, W.J., Phillips, W.D., and Kaiser, W., Vol. 11, No. 1, Pergamon Press, Oxford.
290. Wolf, P.R., 1983, "Elements of Photogrammetry." McGraw-Hill, New York, second edition.
291. Woll, J.D., 1993, "A Review of the Eaton VORAD Vehicle Collision Warning System." Reprinted from International Truck and Bus Meeting and Exposition Detroit, MI, SAE Technical Paper Series 933063, ISSN 0148-7191 Nov., pp. 1-4.
292. Wong, A. and Gan, S., "Vision Directed Path Planning, Navigation, and Control for An Autonomous Mobile Robot." Proceedings of the 1992 SPIE Conference on Mobile Robots, Boston, MA, Nov. 18-20, pp. 352-360.
293. Woodbury, N., Brubacher, M., and Woodbury, J.R., 1993, "Noninvasive Tank Gauging with Frequency-Modulated Laser Ranging." Sensors, Sept., pp. 27-31.
294. Wormley, S., 1994, "A Little GPS Background." Internet message, swormley@ thrl.cnde.iastate.edu to Newsgroup sci.geo.satellite-nav, March 15.
295. Wun-Fogle, M. and Savage, H.T., 1989, "A Tunneling-tip Magnetometer." Sensors and Actuators, Vol. 20, pp. 199-205.
296. Yuan, J.S.C., 1989, "A General Photogrammetric Method for Determining Object Position and Orientation." IEEE Transaction on Robotics and Automation vol. 5, no. 2, pp 129-142.

## Cited Product Information from Commercial Companies

297. ACUITY - Acuity Research, POC: Bob Clark, 20863 Stevens Creek Blvd, Cupertino, CA 95014-2115, 415-369-6782.
298. ADL - Applied Design Laboratories, P. O. Box 2405, Grass Valley, CA 95945, 916-272-8206
299. AECL - Atomic Energy of Canada Ltd., Sheridan Research Park, 2251 Speakman Drive, Mississauga, Ontario, L5K 1B2, Canada. POC Narindar Baines, 905-823-9060
300. ANDREW Andrew Corporation, 10500 W. 153rd Street, Orland Park, IL 60462. 708-3495294 or 708-349-3300.
301. BENTHOS - Benthos, Inc., 49 Edgerton Drive, North Falmouth, MA 02556-2826,508-563-1000.
302. CATERPILLAR - Caterpillar Industrial, Inc., Product Literature, SGV-1106/91, Caterpillar Self Guided Vehicle Systems, 5960 Heisley Rd, Painesville, OH 44077, 216-357-2246.
303. CONTROL - Control Engineering Company, 8212 Harbor Spring Road, Harbor Spring, MI 49740, 616-347-3931.
304. CYBERMOTION - Cybermotion, Inc., 115 Sheraton Drive, Salem, VA 24153, 703-562-7626.
305. CYBERWORKS - Cyberworks, Inc., "Camera Vision Robot Position and Slippage Control System." Product Literature, 31 Ontario Street, Orillia, Ontario, L3V 6H1 Canada, 705-325-6110.
306. DBIR - Denning Branch International Robotics, 1401 Ridge Avenue, Pittsburgh PA 15233, 412-322-4412.
307. DINSMORE - Dinsmore Instrument Company, Product Literature, 1490 and 1525 Magnetic Sensors, Flint, MI, 313-744-1330.
308. ERIM - Environmental Research Institute of Michigan, Box 8618, Ann Arbor, MI 48107, 313-994-1200.
309. EATON - Eaton-Kenway, Inc., 515 East 100 South, 515 E 100 S, Salt Lake City, UT 84102, 801-530-4688.
310. ESP - ESP Technologies, Inc., "ORS-1 Optical Ranging System." Product Literature, ESP Technologies, Inc., 21 Le Parc Drive, Lawrenceville, NJ 08648, 609-275-0356.
311. FUTABA - Futaba Corporation of America, 4 Studebaker, Irvine, CA 92718, 714-455-9888.
312. GEC - GEC Avionics, Kent, U.K.
313. GPS - GPS Report, 1992, Phillips Business Information, Potomac, MD, Nov.
314. GREYHOUND - 1994, "Accident Rate Keeps Falling." Greyhound Connections, Vol. 4, No. 2, March/April.
315. GYRATION - Gyration, Inc., 12930 Saratoga Ave., Building C, Saratoga, CA 95070-4600, 408-255-3016.
316. HITACHI - Hitachi Cable America, Inc., New York Office, 50 Main Street, 12th floor, White Plains, NY 10606, 914-993-0990.
317. HP - Hewlett Packard Components, "Optoelectronics Designer's Catalog, 1991-1992, 19310 Pruneridge Ave., Cupertino, CA, 800-752-9000.
318. HTI - Harris Technologies, Inc., PO Box 6, Clifton, VA 22024, 703-266-0904.
319. ILC - ILC Data Device Corporation, 1982, "Synchro Conversion Handbook," Bohemia, NY.
320. ISI - Intelligent Solutions, Inc., EZNav Position Sensor, One Endicott Avenue, Marblehead, MA 01945, 617-646-4362.
321. ISR - IS Robotics, Inc., RR-1/BS-1 System for Communications and Positioning. Preliminary Data Sheet." IS Robotics, Twin City Office Center, Suite 6, 22 McGrath Highway, Somerville, MA 02143, 617-629-0055.
322. KAMAN - Kaman Sciences Corporation, "Threat Array Control and Tracking Information Center." Product Literature, PM1691, Colorado Springs, CO, 719-599-1285.
323. KVH - KVH Industries, C100 Compass Engine Product Literature, 110 Enterprise Center, Middletown, RI 02840, 401-847-3327.
324. MAGELLAN - Magelan Systems Corp., 960 Overland Court, San Dimas, CA 91773, 909-3946062.
325. MAGNAVOX - Magnavox Advanced Products and Systems, 2829 Maricopa Street, Torrance, CA 90503, 310-618-1200.
326. MASSA - Massa Products Corporation, "E-201B \& E-220B Ultrasonic Ranging Module Subsystems Product Selection Guide." Product Literature 891201-10M, Hingham, MA 02043, 617-749-4800.
327. MICRO-TRAK - Micro-Trak Systems, Inc., "Trak-Star Ultrasonic Speed Sensor." Product Information. P.O. Box 3699, Mankato, MN 56002, 507-257-3600.
328. MTI - MTI Research, Inc., "Computerized Opto-electronic Navigation and Control (CONAC ${ }^{\mathrm{TM}}$ )" and "What You Can Expect From CONAC ${ }^{\mathrm{TM}}$ Products." Product literature. 313 Littleton Road, Chelmsford, MA 01824., 508-250-4949.
329. MOTOROLA - Mini-Ranger Falcon, Product Literature, Motoroloa Government and Systems Tech. Group, 8220 E. Roosevelt Road, PO Box 9040, Scottsdale, AZ 85252, 602-441-7685.
330. MURATA - Murata Erie North America, 2200 Lake Park Drive, Smyrna, GA 30080, 800-8319172.
331. NAMCO - Namco Controls, 7567 Tyler Blvd. Mentor, OH 44060, 800-626-8324.
332. NASA - 1977, "Fast, Accurate Rangefinder." NASA Tech Brief, NPO-13460.
333. NIKE - NIKE, Dept. of Fitness Electronics, 9000 South-West Nimbus, Beaverton, Oregon 97005, 503-644-9000.
334. POLAROID - 1981, "Polaroid Ultrasonic Ranging System User's Manual." Publication No. P1834B, Polaroid Corporation, 784 Memorial Drive, Cambridge, MA 02139, 617-386-3964.
335. POLAROID - 1987, "Technical Specifications for Polaroid Electrostatic Transducer." 7000Series Product Specification ITP-64, Polaroid Corporation, 784 Memorial Drive, Cambridge, MA 02139, 617-386-3964.
336. POLAROID - 1990, "6500-Series Sonar Ranging Module." Product Specifications PID 615077,Polaroid Corporation, 784 Memorial Drive, Cambridge, MA 02139, 617-386-3964.
337. POLAROID - 1991, "Ultrasonic Ranging System." Product Literature, Polaroid Corporation, 784 Memorial Drive, Cambridge, MA 02139, 617-386-3964.
338. POLAROID - 1993, "Polaroid Ultrasonic Ranging Developer's Kit." Publication No. PXW6431 6/93, Polaroid Corporation, 784 Memorial Drive, Cambridge, MA 02139, 617-3863964.
339. REMOTEC - Remotec, 114 Union Valley Road, Oak Ridge, TN 37830, 615-483-0228
340. RIEGL - 1994, "Laser Distance, Level, and Speed Sensor LD90-3." Product Data Sheet 3/94, RIEGL Laser Measurement Systems, RIEGL USA, 4419 Parkbreeze Court, Orlando, FL 32808, 407-294-2799.
341. ROCKWELL - Rockwell International, 3200 East Renner Road, MS 461-235, Richardson, TX 75082, 214-705-1704.
342. SFS - Safety First Systems, Ltd., POC: Allen Hersh, Safety First Systems Inc, 550 Stewart Ave, Garden City, NY 11530-4700, 516-681-3653.
343. SEO - 1991a, Schwartz Electro-Optics, Inc, "Scanning Laser Rangefinder." Product Literature, 3404 N. Orange Blossom Trail, Orlando, FL 32804, 407-297-1794.
344. SEO-1991b, Schwartz Electro-Optics, Inc, Process Report for US Army Contract DAAJ02-91-C-0026, 3404 N. Orange Blossom Trail, Orlando, FL 32804, 407-297-1794.
345. SEO - 1995a, Schwartz Electro-Optics, Inc, "LRF-200 Laser Rangefinder Series." Product Literature, Schwartz Electro-Optics, Inc., 3404 N. Orange Blossom Trail, Orlando, FL 32804, 407-297-1794.
346. SEO - 1995b, Schwartz Electro-Optics, Inc., "SHIELD Scanning Helicopter Interference Envelope Laser Detector" Product Literature, 3404 N. Orange Blossom Trail, Orlando, FL 32804, 407-297-1794.
347. SIMAN - Siman Sensors \& Intelligent Machines Ltd., MTI-Misgav, D.N. Misgav 20179, Israel, +972-4-906888.
348. SPERRY - Sperry Marine Inc., Seminole Trail, Charlottesville, VA, 22901, POC: Peter Arnold, Head of Engineering, ext. 2213, 804-974-2000.
349. SPSi - Spatial Positioning Systems, inc., 12007 Sunrise Valley Drive, Suite 200, Reston, VA 22091-3406, 703-648-9400.
350. TOWER - Tower Hobbies, Mail Order Catalog, P.O. Box 9078, Champaign, IL 61826-9078, 217-398-1100.
351. TRC - Transitions Research Corp., "TRC Light Ranger," Product Literature, Danbury, CT 06810, 203-798-8988.
352. TRC - Transitions Research Corp., "Beacon Navigation System," Product Literature, Shelter Rock Lane, Danbury, CT 06810, 203-798-8988.
353. TRIMBLE - Trimble Navigation, 645 North Mary Avenue, Building 5, Sunnyvale, CA 94088, 408-481-2865.
354. UNIQUE -Unique Mobility, Inc., Product Literature, 425 Corporate Circle, Golden, CO 80401, 303-278-2002.
355. VORAD-1 - VORAD Safety Systems, Inc., "The VORAD Vehicle Detection and Driver Alert System." Product Literature, 10802 Willow Ct, San Diego, CA 92127, 619-674-1450.
356. VORAD-2 - Eaton VORAD Technologies, L.L.C., Eaton Center, Cleveland, OH 44114-2584, 216-523-5000
357. WATSON - Watson Industries, Inc., Melby Rd., Eau Claire, WI 54703, 715-839-0628.
358. ZEMCO - Zemco Group, Inc., 3401 Crow Canyon Road, Suite 201, San Ramon, CA 94583, 415-866-7266.

Relevant Research Articles on Mobile Robot Positioning, for Further Reading
359. Adams, M., 1993, "Amplitude Modulated Optical Range Data Analysis in Mobile Robots." Proceedings of IEEE International Conference on Robotics and Automation Atlanta, GA, May 10-15, pp. 8-13.
360. Bhanu, B., Roberts, B., and Ming, J., 1990, "Inertial Navigation Sensor Integrated Motion Analysis for Obstacle Detection." Proceedings of IEEE International Conference on Robotics and Automation, Cincinnati, OH, May 13-18, pp. 954-959.
361. Blais, F., Rioux, M., and Domey, J., 1991, "Optical Range Image Acquisition for the Navigation of a Mobile Robot." Proceedings of IEEE International Conference on Robotics and Automation, Sacramento, CA, Apr. 9-11, pp. 2574-2580.
362. Bourbakis, N., 1988, "Design of an Autonomous Navigation System." IEEE Control Systems Magazine, Oct., pp. 25-28.
363. Chen, Q., Asada, M., and Tsuji, S., 1988, "A New 2-D World Representation System for Mobile Robots." Proceedings of IEEE International Conference on Robotics and Automation, Philadelphia, Apr. 24-29, pp. 604-606.
364. Crowley, J., 1986, "Navigation for an Intelligent Mobile Robot." IEEE Journal of Robotics and Automation, Vol. RA-1, No. 1, pp. 31-41.
365. Curran, A. and Kyriakopoulos, K., 1993, "Sensor-based Self-localization for Wheeled Mobile Robots." Proceedings of IEEE International Conference on Robotics and Automation Atlanta, GA, May 10-15, pp. 8-13.
366. Drake, K., McVey, E., and Inigo, R., 1985, "Sensing Error for a Mobile Robot Using Line Navigation." IEEE Transactions on Pattern Analysis and Mchine Intelligence, Vol. PAMI-7, No. 4, pp. 485-490.
367. Drake, K., McVey, E., and Inigo, R., 1987, "Experimental Position and Ranging Results for a Mobile Robot." IEEE Journal of Robotics and Automation Vol. RA-3, No. 1, pp. 31-42.
368. Fennema, C., Hanson, A., Riseman, E., Beveridge, J., and Kumar, R., 1990, "Model-Directed Mobile Robot Navigation." IEEE Transactions on Systems, Man, and Cybernetics Vol. 20, No. 6, pp. 1352-1369.
369. Harmon, S.Y., 1987, "The Ground Surveillance Robot (GSR): An Autonomous Vehicle Designed to Transit Unknown Terrain." IEEE Journal of Robotics and Automation, Vol. RA3, No. 3, pp. 266-279.
370. Holcombe, W., Dickerson, S., Larsen, J., and Bohlander, R., 1988, "Advances in Guidance Systems for Industrial Automated Guided Vehicle." Proceedings of the 1988 SPIE Conference on Mobile Robots, Cambridge, MA, Nov. 10-11, pp. 288-297.
371. Huang, Y., Cao, Z., Oh, S., Katten, E., and Hall, E., 1986, "Automatic Operation for a Robot Lawn Mower." Proceedings of the 1986 SPIE Conference on Mobile Robts, Cambridge, MA, Oct. 30-31, pp. 344-354.
372. Kanbara, T., Miura, J., and Shirai, Y., 1993, "Selection of Efficient Landmarks for an Autonomous Vehicle." Proceedings of the 1993 IEEE/RSJ International Conference a Intelligent Robotics and Systems, Yokohama, Japan, July 26-30, pp. 1332-1338.
373. Kortenkamp, D., 1993, "Cognitive Maps for Mobile Robots: A Representation for Mapping and Navigation." Ph.D. Thesis, The University of Michigan.
374. Krotkov, E., 1991a, "Laser Rangefinder Calibration for a Walking Robot." Proceedings of IEEE International Conference on Robotics and Autonation, Sacramento, CA, Apr. 9-11, pp. 2568-2573.
375. Kuipers, B. and Byun, Y., 1988, "A Robust Qualitative Method for Robot Spatial Learning." The Seventh National Conference on Artificial Intelligence pp. 774-779.
376. Kurazume, R. and Nagata, S., 1994, "Cooperative Positioning with Multiple Robots." Proceedings of IEEE International Conference on Robotics and Automation, San Diego, CA, May 8-13, pp. 1250-1257.
377. Lebegue, X. and Aggarwal, J., 1994, "Generation of Architectural CAD Models Using a Mobile Robot." Proceedings of IEEE International Conference on Robotics and Automation, San Diego, CA, May 8-13, pp. 711-717.
378. Levitt, T., Lawton, D., Chelberg, D., and Nelson, P., 1987, "Qualitative Navigation." Proc. DARPA Image Understanding Workshop pp. 447-465.
379. Lu, Z., Tu, D., Li, P., Hong, Z., and Wu, B., 1992, "Range Imaging Sensor for Auto - Vehicle Guidance Applying an Optical Radar." Proceedings of the 1992 SPIE Conference on Mobile Robots, Boston, MA, Nov. 18-20, pp. 456-465.
380. MacKenzie, P. and Dudek, G., 1994, "Precise Positioning Using Model-Based Maps." Proceedings of IEEE International Conference on Robotics and Automation, San Diego, CA, May 8-13, pp. 1615-1621.
381. Malik, R. and Polkowski, E., 1990, "Robot Self-Location Based on Corner Detection." Proceedings of the 1990 SPIE Conference on Mobile Robots, Boston, MA, Nov. 8-9, pp. 306-316.
382. Malik, R. and Prasad, S., 1992, "Robot Mapping with Proximity Detectors." Proceedings of the 1992 SPIE Conference on Mobile Robots,Boston, MA, Nov. 18-20, pp. 614-618.
383. McGillem, C. and Rappaport, T., 1989, "A Beacon Navigation Method for Autonomous Vehicles." IEEE Transactions on Vehicular Technology, Vol. 38, No. 3, pp. 132-139.
384. McKendall, R., 1988, "Robust Fusion of Location Information." Proceedings of IEEE International Conference on Robotics and Automation Philadelphia, PA, April 24-29, pp. 1239-1243.
385. McVey, E., Drake, K., and Inigo, R., 1986, "Range Measurements by a Mobile Robot Using a Navigation Line." IEEE Transactions on Pattern Analysis and Machine Intelligence Vol. PAMI-8, No. 1, pp. 105-109.
386. Ohya, A., Nagashima, Y., and Yuta, S., 1994, "Exploring Unknown Environment and Map Construction Using Ultrasonic Sensing of Normal Direction of Walls." Proceedings of IEEE International Conference on Robotics and Automation San Diego, CA, May 8-13, pp. 485492.
387. Parker, K., 1993, "'Bots Struggle to Learn Basics." Manufacturing Systems, Oct. 12, pp. 1314.
388. Partaatmadja, O., Benhabib, A., Sun, A., and Goldenberg, A., 1992, "An Electrooptical Orientation Sensor for Robotics." IEEE Transactions on Robotics and Automation Vol. 8, No. 1, pp. 111-119.
389. Pears, N. and Probert, P., 1993, "An Optical Range Sensor for Mobile Robot Guidance." Proceedings of IEEE International Conference on Robotics and Automation Altanta, GA, May 10-15, pp. 659-664.
390. Roth-Tabak, Y. and Jain, R., 1989, "Building an Environment Model Using Depth Information." Computer, June, pp. 85-90.
391. Roth-Tabak, Y. and Weymouth, T., 1990, "Environment Model for Mobile Robot Indoor Navigation." Proceedings of the 1990 SPIE Conference on Mobile Rdots, Boston, MA, Nov. 8-9, pp. 453-463.
392. Safaee-Rad, R., Tchoukanov, I., Smith, K., and Benhabib, B., 1992, "Three-dimensional Location Estimation of Circular Features for Machine Vision." IEEE Transactions on Robotics and Automation, Vol. 8, No. 5, pp. 624-640.
393. Santos, V., Goncalves, J., and Vaz, F., 1994, "Perception Maps for the Local Navigation of a Mobile Robot: a Neural Network Approach." Proceedings of IEEE Intemational Conference on Robotics and Automation, San Diego, CA, May 8-13, pp. 2193-2198.
394. Schwind, G., 1994, "Controls Offer Non-Wire Guidance Without a Costly Premium." Material Handling Engineering, March, p. 31.
395. Shertukde, H. and Bar-Shalom, Y., 1988, "Target Parameter Estimation in the Near Field with Two Sensors." IEEE Transactions on Acoustics, Speech, and Signal Processing Vol. 36, No. 8, pp. 1357-1360.
396. Singh, K. and Fujimura, K., 1993, "Map Making by Cooperating Mobile Robots." Proceedings of IEEE International Conference on Robotics and Automation, Atlanta, GA, May 10-15, pp. 254-259.
397. Sutherland, K.T. and Thompson, W.B., 1993, "Inexact Navigation." Proceedings of the IEEE International Conference on Robotics and Automation May, pp. pages?
398. Xu, H. and Chi, X., 1993, "Calibration and Parameter Identification for Laser Scanning Sensor." Proceedings of IEEE International Conference on Robotics and Automation, Atlanta, GA, May 10-15, pp. 665-670.
399. Yoo, J. and Sethi, 1991, "Mobile Robot Localization with Multiple Stationary Cameras." Proceedings of the 1991 SPIE Conference on Mobile Robots,Boston, MA, Nov. 14-15, pp. 155-170.
400. Zheng, J., Barth, M., and Tsuji, S., 1991, "Autonomous Landmark Selection for Route Recognition by a Mobile Robot." Proceedings of IEEE International Conference on Robotics and Automation, Sacramento, CA, April 9-11, pp. 2004-2009.

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Paper 01 Borenstein, J. and Koren, Y., 1985, "A Mobile Platform For Nursing Robots." IEEE Transactions on Industrial Electronics Vol. 32, No. 2, pp. 158-165.

Paper 02 Borenstein, J. and Koren, Y., 1987, "Motion Control Analysis of a Mobile Robot." Transactions of ASME, Journal of Dynamics, Measurement and Control, Vol. 109, No. 2, pp. 73-79.

Paper 10 Borenstein, J. and Koren, Y., 1989, "Real-time Obstacle Avoidance for Fast Mobile Robots." IEEE Transactions on Systems, Man, and Cybernetics Vol. 19, No. 5, Sept./Oct., pp. 1179-1187.
Paper 16 Borenstein, J. and Koren, Y., 1991, "The Vector Field Histogram - Fast Obsta-cle-Avoidance for Mobile Robots." IEEE Journal of Robotics and Automation, Vol. 7, No. 3., June 1991, pp. 278-288.
Paper 18 Borenstein, J, and Koren, Y., 1991, "Histogramic In-motion Mapping for Mobile Robot Obstacle Avoidance." IEEE Journal of Robotics and Automation Vol. 7, No. 4, 1991, pp. 535-539.

Paper 30 Borenstein, J. and Raschke, U., 1992, "Real-time Obstacle Avoidance for Non-Point Mobile Robots." SME Transactions on Robotics Research Vol. 2, pp. 2.1-2.10, 1992.
Paper 32 Borenstein, J. and Koren, Y., 1995, "Error Eliminating Rapid Ultrasonic Firing for Mobile Robot Obstacle Avoidance." IEEE Transactions on Robotics and Automation, February 1995, Vol. 11, No. 1, pp 132-138.
Paper 34 Borenstein, J., 1995, "Control and Kinematic Design for Multi-degree-of-freedom Mobile Robots With Compliant Linkage." IEEE Transactions on Robotics and Automation, February 1995, Vol. 11, No. 1, pp. 21-35

Paper 35 Borenstein, J., 1992, "Compliant-linkage Kinematic Design for Multi-degree-of-freedom Mobile Robots ." Proceedings of the SPIE Symposium on Advances in Intelligent Systems, Mobile Robots VII, Boston, MA, Nov. 15-20, 1992, pp. 344-351.

Paper 48 Borenstein, J., 1995, "Internal Correction of Dead-reckoning Errors With the Compliant Linkage Vehicle." Journal of Robotic Systems, Vol. 12, No. 4, April 1995, pp. 257-273.
Paper 49 Borenstein, J., 1994b, "The CLAPPER: a Dual-Drive Mobile Robot with Internal Correction of Dead-reckoning Errors." Proceedings of the 1994 IEEE International

Conference on Robotics and Automation, San Diego, CA, May 8-13, 1994, pp. 30853090.

Paper 52 Shoval, S., Borenstein, J., and Koren, Y., 1994f, "Mobile Robot Obstacle Avoidance in a Computerized Travel Aid for the Blind." Proceedings of the 1994 IEEE International Conference on Robotics and Automation, San Diego, CA, May 8-13, 1994, pp. 20232029.

Paper 53 Borenstein, J, 1994g, "Internal Correction of Dead-reckoning Errors With the Smart Encoder Trailer." 1994 International Conference on Intelligent Robots and Systens (IROS '94). Muenchen, Germany, September 12-16, 1994, pp. 127-134.

Paper 56 Borenstein, J., Wehe, D., Feng, C., Koren, Y., 1995, "Mobile Robot Navigation in Narrow Aisles with Ultrasonic Sensors." Presented at the ANS 6th Topical Meeting on Robotics and Remote Systems," Monterey, California, February 5-10, 1995.

Paper 59 Borenstein, J. and Feng. L., 1995b, "Correction of Systematic Dead-reckoning Errors in Mobile Robots." Proceedings of the 1995 International Conference on Intelligert Robots and Systems (IROS '95), Pittsburgh, Pennsylvania, August 5-9, 1995, pp. 569574.

Paper 60 Borenstein, J. and Feng. L., 1995c, "UMBmark: A Benchmark Test for Measuring Deadreckoning Errors in Mobile Robots." Presented at the 1995 SPIE Conference on Mobile Robots, Philadelphia, October 22-26, 1995.

Tech. Report Borenstein, J. and Feng, L., 1994, "UMBmark - A Method for Measuring, Comparing, and Correcting Dead-reckoning Errors in Mobile Robots." Technical Report, The University of Michigan UM-MEAM-94-22, December 1994.


[^0]:    Apparent Drift Calculation
    (Reproduced with permission from [Sammarco, 1990].)

    Apparent drift is a change in the output of the gyroscope as a result of the Earth's rotation. This change in output is at a constant rate; however, this rate depends on the location of the gyroscope on the Earth. At the North Pole, a gyroscope encounters a rotation of $360^{\circ}$ per 24 -h period or $15^{\circ} / h$. The apparent drift will vary as a sine function of the latitude as a directional gyroscope moves southward. The direction of the apparent drift will change once in the southern
    hemisphere. The equations for Northern and Southern Hemisphere apparent drift follow. Counterclockwise (ccw) drifts are considered positive and clockwise (cw) drifts are considered negative.

    Northern Hemisphere: $15^{\circ} / \mathrm{h}$ [sin (latitude)] ccw.
    Southern Hemisphere: $15^{\circ} / \mathrm{h}[\sin$ (latitude,)] cw .

    The apparent drift for Pittsburgh, PA (40.443 ${ }^{\circ}$ latitude) is calculated as follows: $15^{\circ} / \mathrm{h}[\sin (40.443)]=9.73^{\circ} / \mathrm{h}$ CCW or apparent drift $=0.162^{\circ} / \mathrm{min}$. Therefore, a gyroscope reading of $52^{\circ}$ at a time period of 1 minute would be corrected for apparent drift where
    corrected reading $=52^{\circ}-\left(0.162^{\circ} / \mathrm{min}\right)(1 \mathrm{~min})=51.838^{\circ}$.
    Small changes in latitude generally do not require changes in the correction factor. For example, a $0.2^{\circ}$ change in latitude ( 7 miles) gives an additional apparent drift of only $0.00067^{\circ} / \mathrm{min}$.

[^1]:    ${ }^{1}$ CONAC is a trademark of MTI.

[^2]:    ${ }^{1}$ relating to, or contributing to the sense of smell (The American Heritage Dictionary of the English Language, Third Edition is licensed from Houghton Mifflin Company. Copyright © 1992 by Houghton Mifflin Company. All rights reserved).

